

QCD in Heavy Ion Collisions

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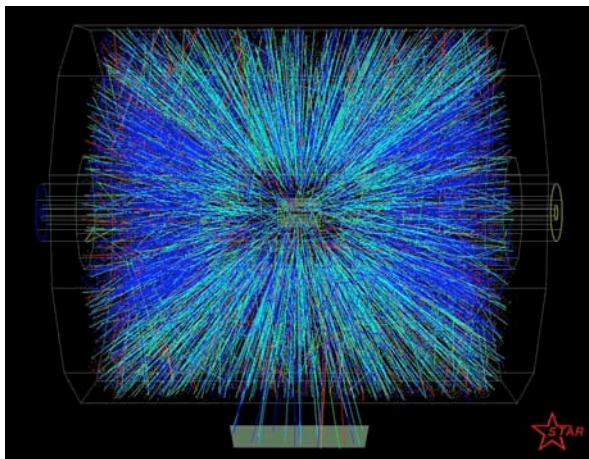
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Heavy Ion Collisions @ RHIC & the LHC

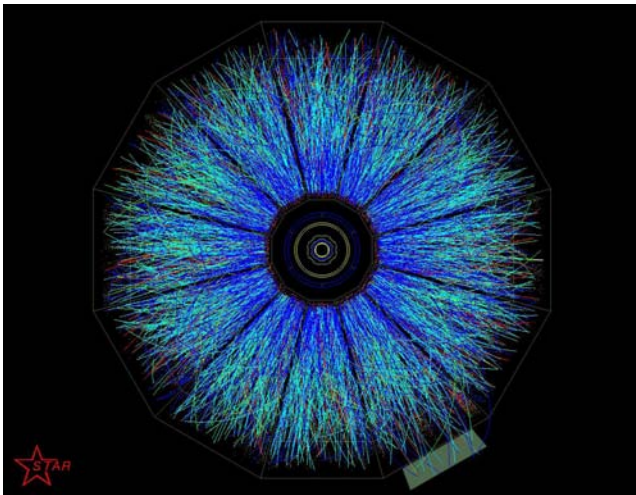


Au+Au collisions at RHIC



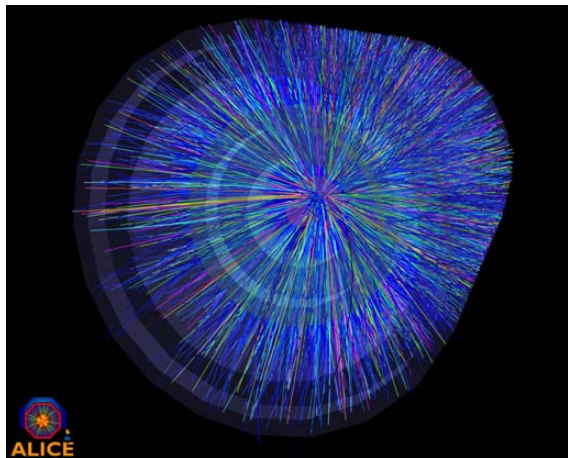
- Au+Au collision at STAR: longitudinal projection
- ~ 3000 produced particles streaming into the detector

Au+Au collisions at RHIC

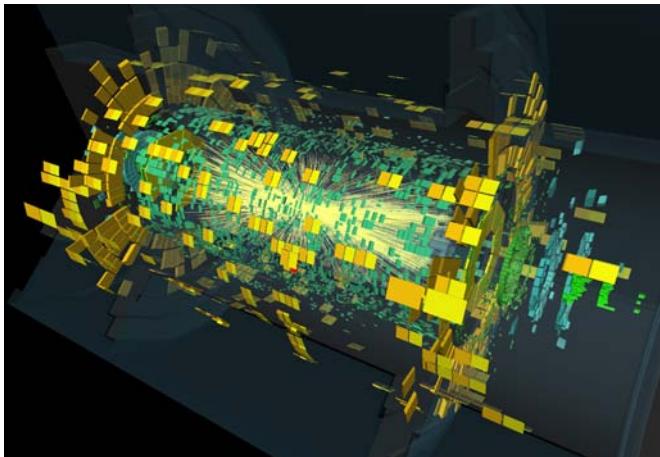


- Au+Au collision at STAR: **transverse projection**

Pb+Pb collisions at the LHC: ALICE

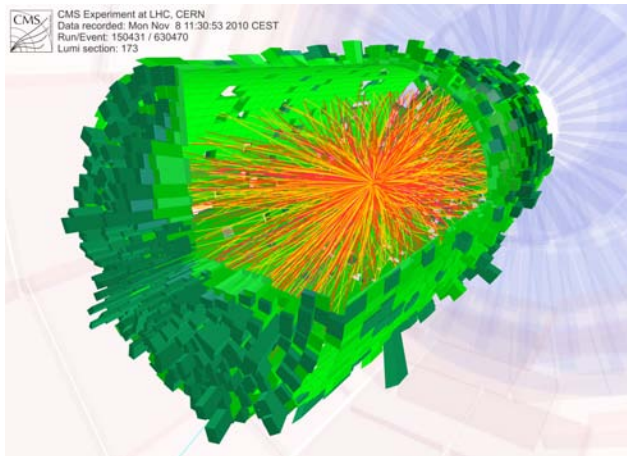


- Pb+Pb collision at ALICE: ~ 1600 hadrons per unit rapidity
- How to describe/understand such a complex system ?



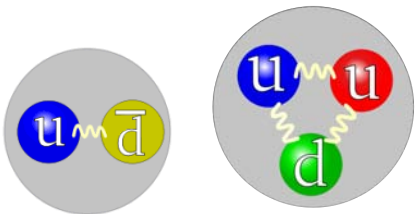
- Traditional **perturbative** methods become inappropriate (collective phenomena, multiple scattering ...)

Pb+Pb collisions at the LHC: CMS

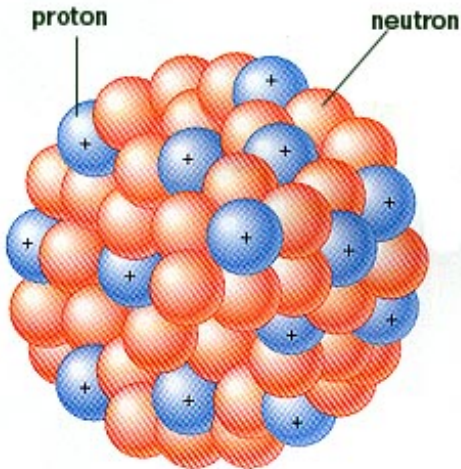


- The concept of **particle** is not so useful anymore ...
- One should rather speak about **QCD matter**

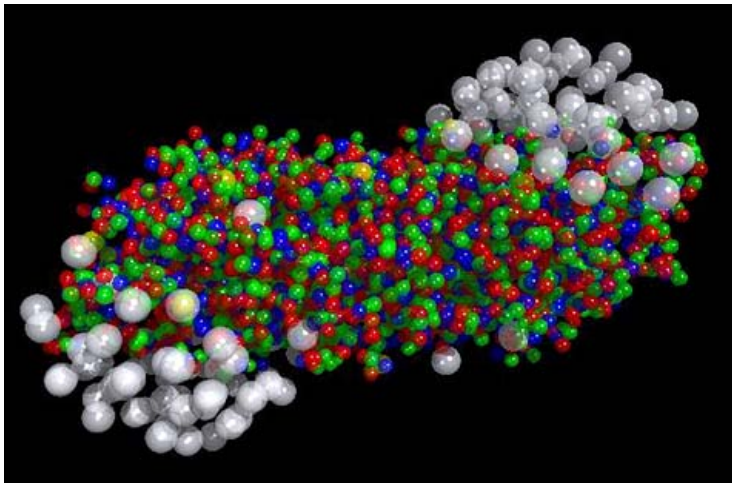
QCD matter: from hadrons ...



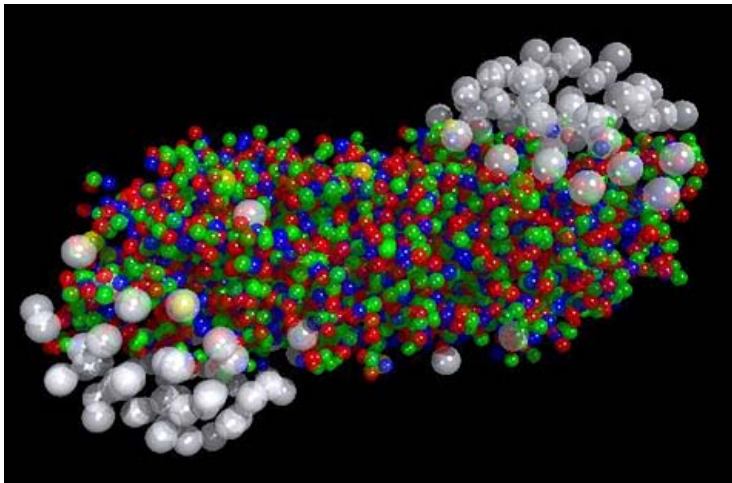
Quark composition of a pion



- At low energies, QCD matter exists only in the form of **hadrons** (mesons, baryons, nuclei)

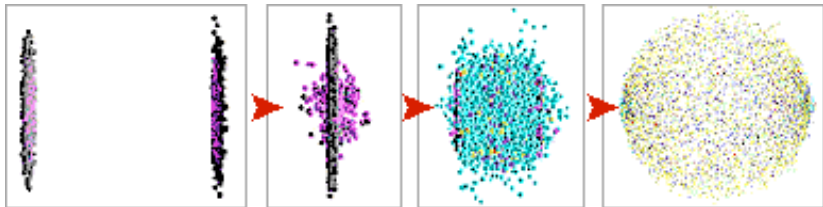


- At sufficiently high energies, the relevant degrees of freedom are **partonic** (quarks & gluons)
- True for both p+p collisions and A+A collisions ...



- At sufficiently high energies, the relevant degrees of freedom are **partonic** (quarks & gluons)
- ... but HIC give us access to **new forms of partonic matter**

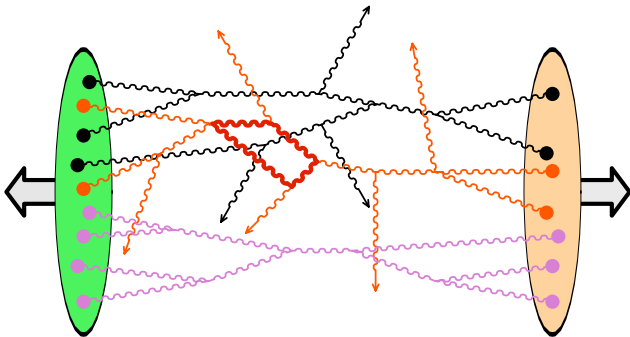
New forms of QCD matter produced in HIC



- Prior to the collision: 2 Lorentz-contracted nuclei ('pancakes')
 - 'Color Glass Condensate' (CGC)
- Right after the collision: non-equilibrium partonic matter
 - 'Glasma' (from 'Glass' + 'Plasma')
- At later stages ($\Delta t \gtrsim 1 \text{ fm}/c$) : local thermal equilibrium
 - 'Quark-Gluon Plasma' (QGP)
- Final stage ($\Delta t \gtrsim 6 \text{ fm}/c$) : hadrons
 - 'final event', or 'particle production'

How to study these new forms of matter ?

- Standard **perturbation theory in QCD** (= expansion in powers of the coupling 'constant' α_s) fails **even at weak coupling**, because of the **high parton density**.



- High-density effects (**multiple scattering, parton saturation, Debye screening etc**) must be **resummed to all orders in α_s** .
- This results into **effective theories**.

The possibility of a strong coupling

- Besides, there is no guarantee that the coupling is weak !

RHIC Scientists Serve Up "Perfect" Liquid

New state of matter more remarkable than predicted -- raising many new questions

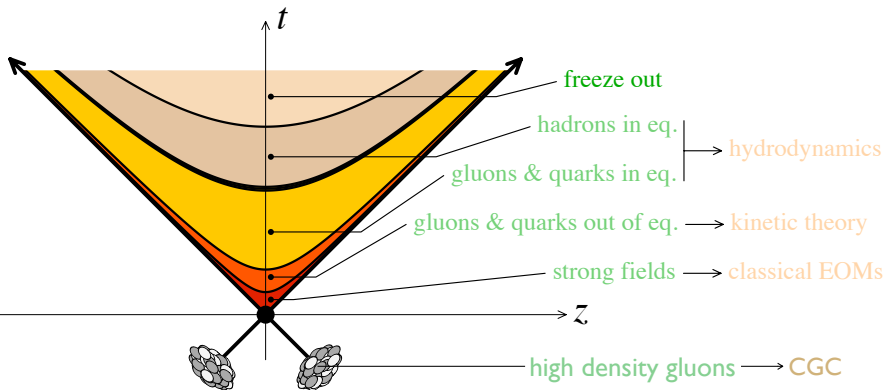
Monday, April 18, 2005

TAMPA, FL -- The four detector groups conducting research at the [Relativistic Heavy Ion Collider](#) (RHIC) -- a giant atom "smasher" located at the U.S. Department of Energy's Brookhaven National Laboratory -- say they've created a new state of hot, dense matter out of the quarks and gluons that are the basic particles of atomic nuclei, but it is a state quite different and even more remarkable than had been predicted. In [peer-reviewed papers](#) summarizing the first three years of RHIC findings, the scientists say that instead of behaving like a gas of free quarks and gluons, as was expected, the matter created in RHIC's heavy ion collisions appears to be more like a *liquid*.

- 'Perfect fluid' = $\alpha_s \rightarrow \infty$
- Interesting connection with string theory ('AdS/CFT correspondence').

Effective theories for Heavy Ion Collisions

- A space-time picture of a heavy ion collision



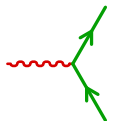
- Different effective theories apply at different stages.
- **But they refer all to QCD !**

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu}^a F_a^{\mu\nu} + \sum_f \bar{\psi}_f (i\gamma^\mu D_\mu - m) \psi_f$$

QCD: Quarks & Gluons

- Electromagnetic interactions: **Quantum Electrodynamics (QED)**

- matter : electron; interaction carrier : photon
- interaction vertex :

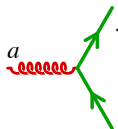


A Feynman diagram showing a red wavy line (photon) entering from the left and splitting into two green straight lines with arrows (electrons) exiting to the right. The diagram is followed by a tilde symbol and the letter 'e'.

$$\sim e \quad (\text{electric charge of the electron})$$

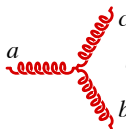
- Strong interactions: **Quantum Chromodynamics (QCD)**

- matter : quarks; interaction carriers : gluons
- interaction vertices :



A Feynman diagram showing a red wavy line (gluon) entering from the left and splitting into two green straight lines with arrows (quarks) exiting to the right. The gluon line is labeled 'a', the top quark line 'j', and the bottom quark line 'i'. The diagram is followed by a tilde symbol and the expression $g(t^a)_{ij}$.

$$\sim g (t^a)_{ij}$$



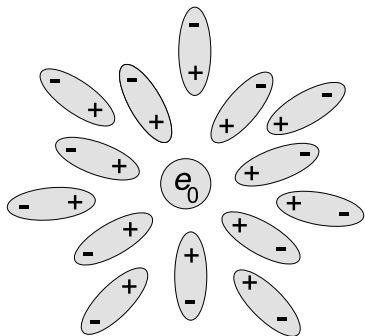
A Feynman diagram showing a red wavy line (gluon) entering from the left and splitting into two red wavy lines (gluons) exiting to the right. The gluon line is labeled 'a', the top gluon line 'c', and the bottom gluon line 'b'. The diagram is followed by a tilde symbol and the expression $g(T^a)_{bc}$.

$$\sim g (T^a)_{bc}$$



- i, j : color indices of the quarks ($N_c = 3$ possible values)
- a, b, c : color indices of the gluons ($N_c^2 - 1 = 8$ possible values)

- An electric charge polarizes the surrounding medium:

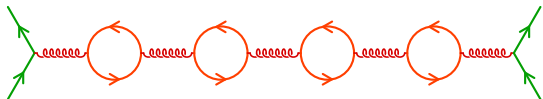


$$V(R) = \frac{e_{\text{eff}}(R)}{R}$$

- The **effective charge** depends upon the distance R from the **bare** one.
- Normally this leads to **screening**: $e_{\text{eff}}(R)$ decreases with R .

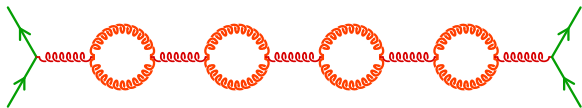
Running coupling: from QED to QCD

- The **vacuum** itself is a polarisable 'medium' !



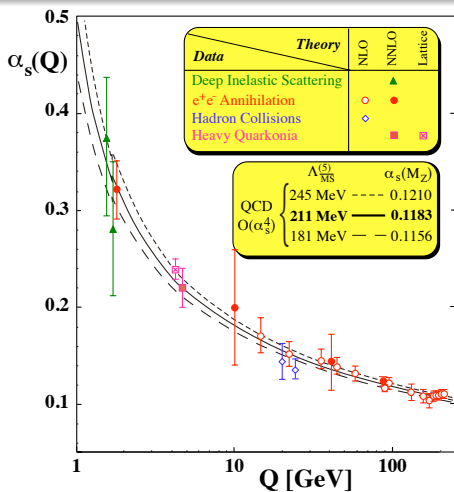
$$QED : \quad \alpha_{\text{eff}}(R) = \frac{\alpha}{1 - \frac{2\alpha}{3\pi} \ln(1/mR)}, \quad \alpha \equiv \frac{e^2}{\hbar c} \approx \frac{1}{137}$$

- In QCD, the (longitudinal) gluons yield **antiscreening** !



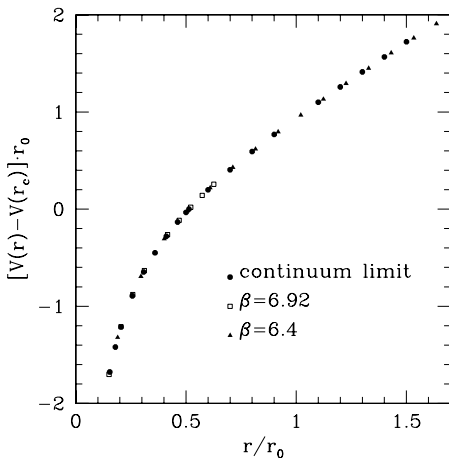
$$QCD : \quad \alpha_s(R) \equiv \frac{g^2(R)}{4\pi} = \frac{2\pi N_c}{(11N_c - 2N_f) \ln(1/\Lambda_{\text{QCD}}R)}$$

Asymptotic freedom



- The coupling is weak at short distances, or large transferred momenta:

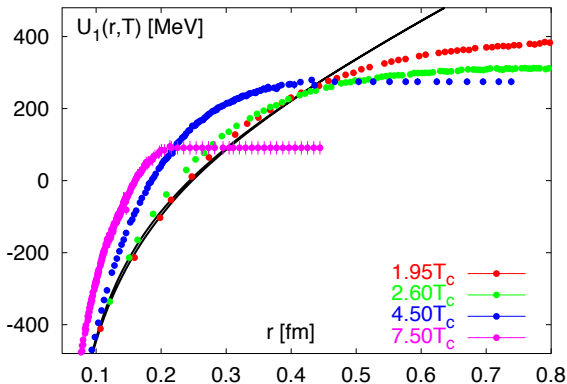
$$Q \sim 1/R \gg \Lambda_{\text{QCD}} \simeq 200 \text{ MeV}$$



- The quark–antiquark potential increases linearly with the distance.
- Quarks (and gluons) are confined into colorless hadrons

Quark–antiquark potential at finite T

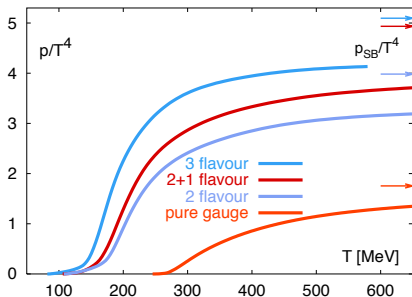
- With increasing the temperature T , the potential flattens at shorter and shorter distances.



- This eventually leads to a **phase transition** at some **critical temperature T_c**

Quark–Gluon Plasma

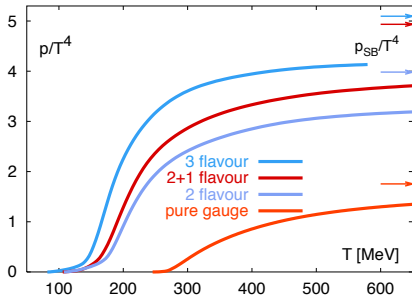
- Lattice calculations of the pressure in QCD at finite T



- Rapid increase of the pressure
 - at $T \simeq 270$ MeV with gluons only
 - at $T \simeq 150$ to 180 MeV with light quarks
- Interpreted as a rise in the number of active degrees of freedom due to the liberation of quarks and gluons

Quark–Gluon Plasma

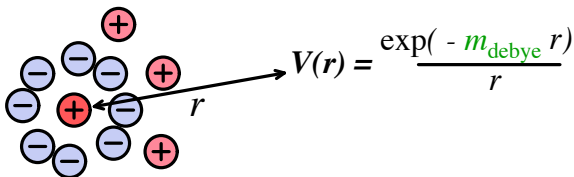
- Lattice calculations of the pressure in QCD at finite T



- Rapid increase of the pressure
 - at $T < T_c$: 3 light mesons (π^0, π^\pm)
 - at $T < T_c$: 52 d.o.f. (gluons: $8 \times 2 = 16$; quarks: $3 \times 3 \times 2 \times 2 = 36$)
- Interpreted as a rise in the number of active degrees of freedom due to the liberation of quarks and gluons

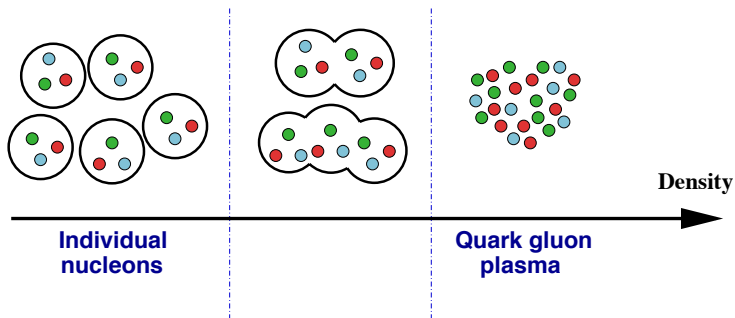
Debye screening

- **Quark–Gluon Plasma (QGP)** : a system of quarks and gluons which got free of confinement !
- How is that possible ???



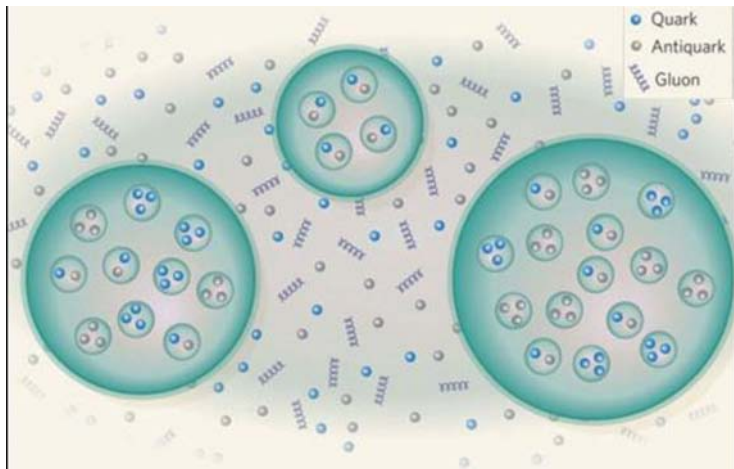
- In a dense medium, color charges are **screened by their neighbors**
- The interaction potential decreases exponentially beyond the **Debye radius** $r_{\text{Debye}} = 1/m_{\text{Debye}}$
- Hadrons whose sizes are larger than r_{Debye} cannot bind anymore

Deconfinement phase transition



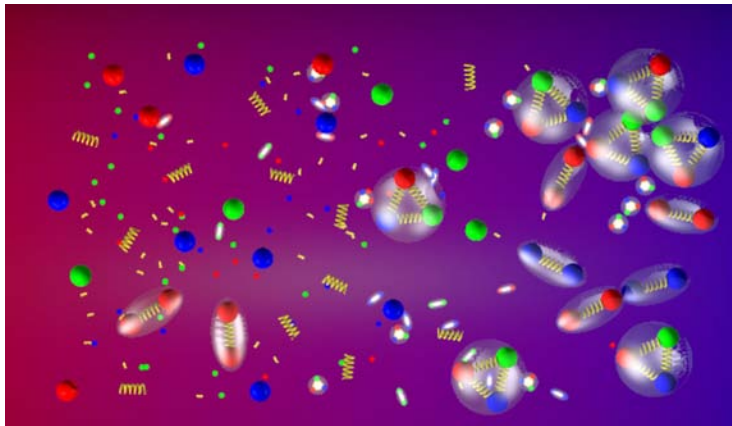
- When the nucleon density increases, **they merge**, enabling quarks and gluons to hop freely from a nucleon to its neighbors
- This phenomenon extends to **the whole volume** when the phase transition ends
- Note: **if** the transition was **first-order**, it would go through a mixed phase containing a mixture of nucleons and plasma

Possible first-order scenario with critical bubbles



... but this is not what really happens !

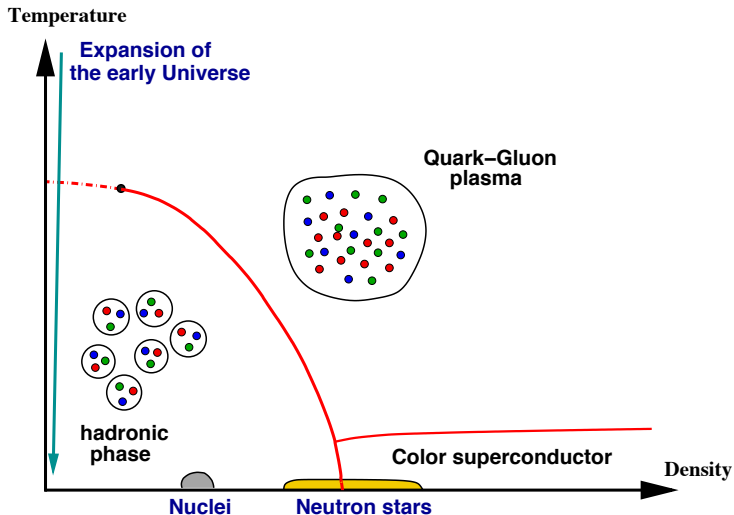
The actual scenario is a 'cross-over'



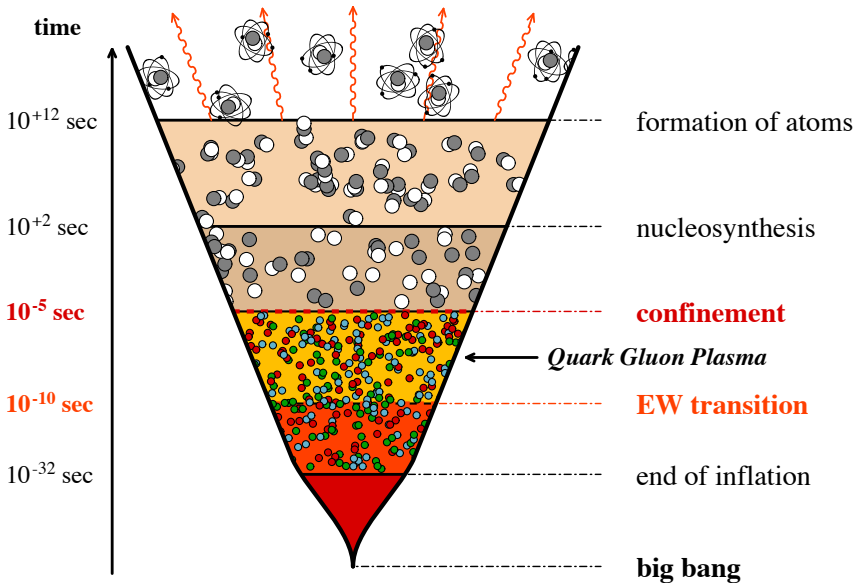
- ▷ This was firmly established by the Wuppertal–Budapest lattice group
(*Aoki et al., Nature, 443 (2006) 675*)

Phase–diagram for QCD

- ... as explored by the expansion of the Early Universe ...

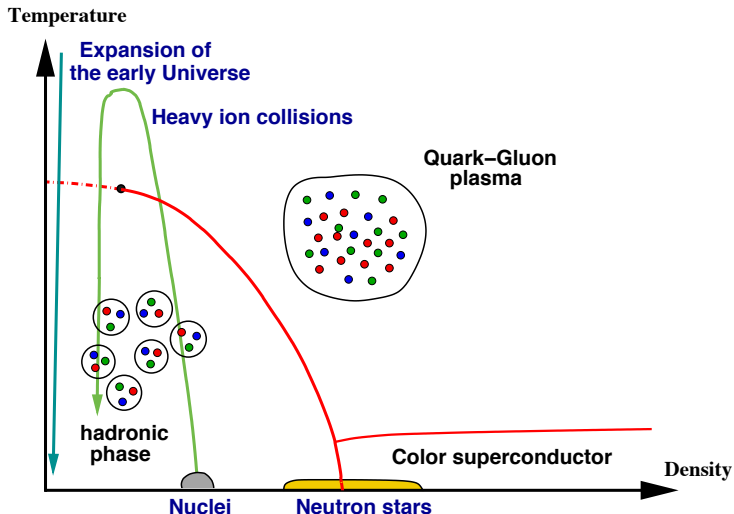


The Big Bang

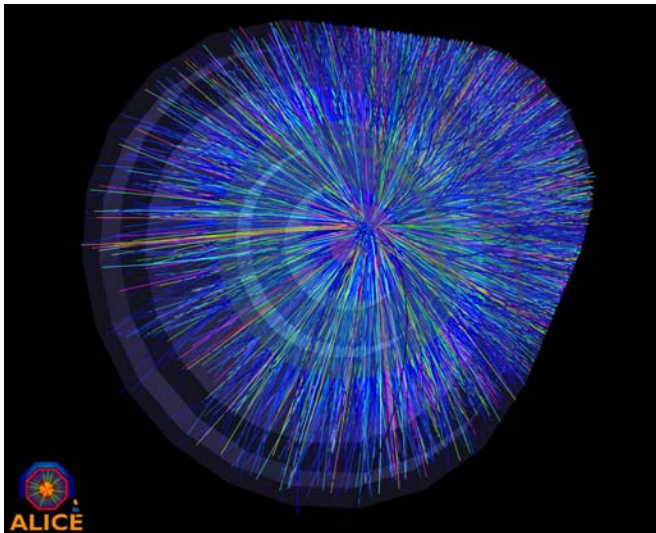


Phase–diagram for QCD

- ... as explored by the expansion of the Early Universe ...

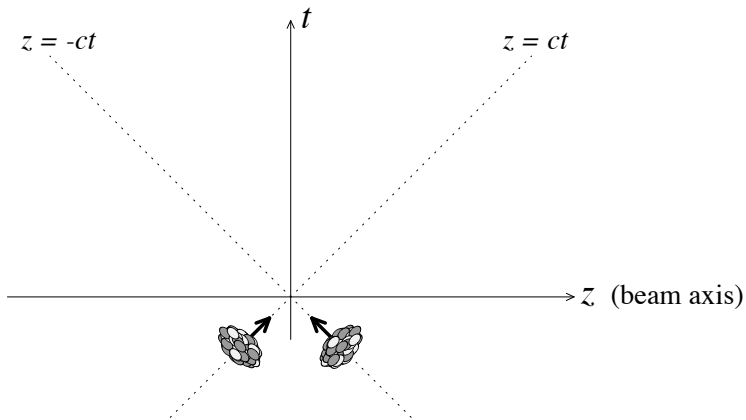


- ... and in the ultrarelativistic heavy ion collisions.



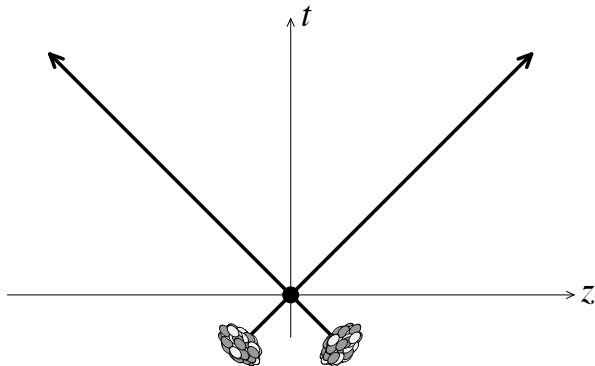
- The subject of these lectures

Lecture I: Initial conditions



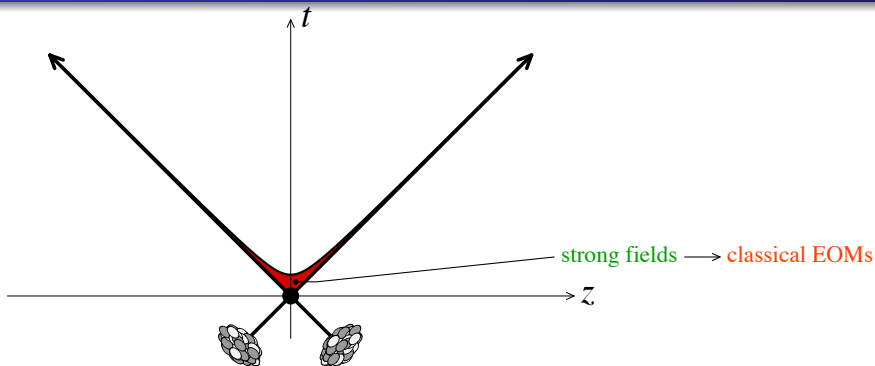
- $\tau < 0$: hadronic wavefunctions prior to the collision
 - high-energy evolution & the Color Glass Condensate
 - it applies to any highly energetic hadron (proton or nucleus)

Lecture I: Initial conditions

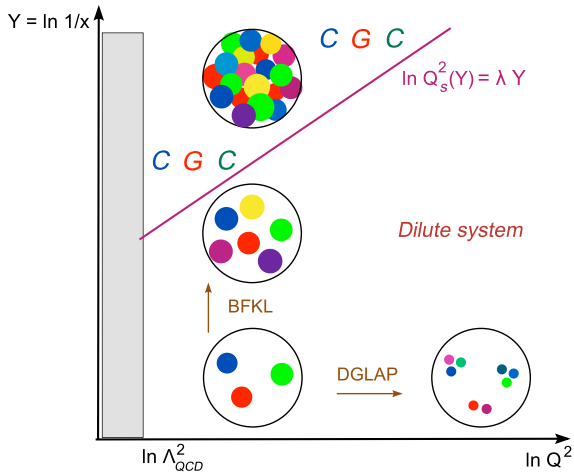
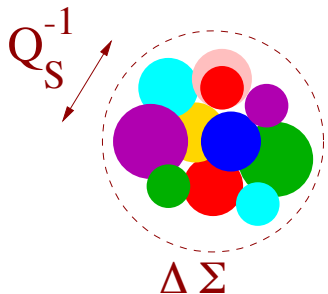


- $\tau < 0$: hadronic wavefunctions prior to the collision
- $\tau \sim 0 \text{ fm}/c$: the hard scattering
 - production of hard particles: jets, direct photons, heavy quarks
 - calculable within (standard) perturbative QCD ('leading twist')

Lecture I: Initial conditions



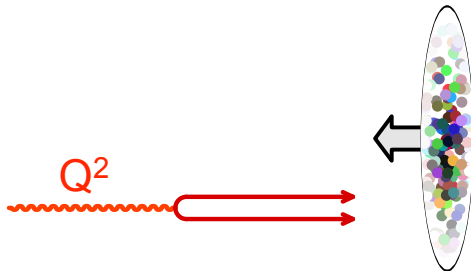
- $\tau < 0$: hadronic wavefunctions prior to the collision
- $\tau \sim 0 \text{ fm}/c$: the hard scattering
- $\tau \sim 0.2 \text{ fm}/c$: strong color fields (or 'glasma')
 - semi-hard quanta ($p_{\perp} \lesssim 2 \text{ GeV}$): gluons, light quarks
 - make up for most of the multiplicity
 - sensitive to the physics of saturation ('higher twist')



Parton picture

- When an **energetic hadron** is probed on a **hard resolution scale** (momentum transfer $Q^2 \gg \Lambda_{\text{QCD}}^2$), one sees a bunch of **partons** ...

- with transverse area $\sim 1/Q^2$...
- and longitudinal momentum fraction $x = k_z/P$ fixed by the kinematics

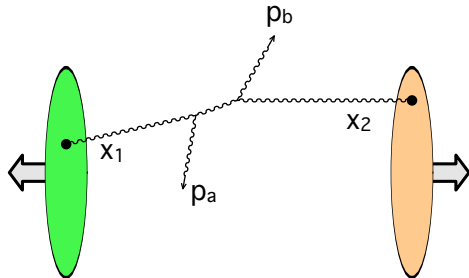


- E.g. : in Deep Inelastic Scattering (DIS)

$$x = \frac{Q^2}{s} \quad s = \text{center-of-mass energy squared}$$

- **N.B.:** high energy \iff small x

Particle production in hadron–hadron collisions

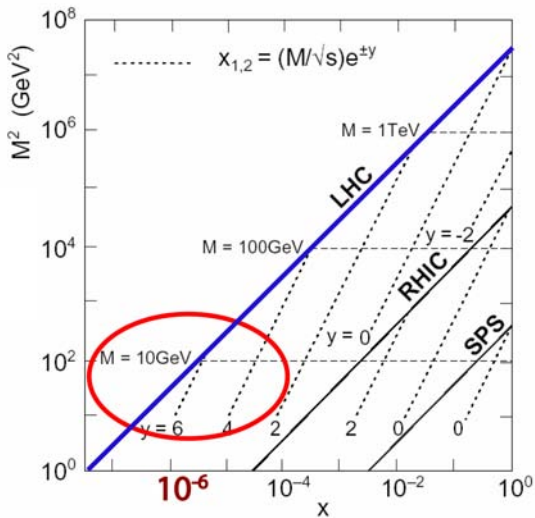


- The partons relevant for the process under consideration carry the longitudinal momentum fractions

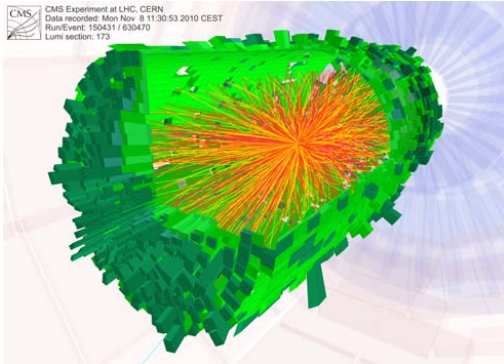
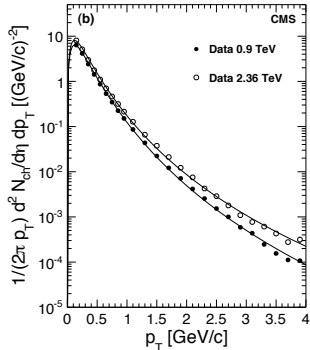
$$x_1 = \frac{p_{a\perp}}{\sqrt{s}} e^{Y_a} + \frac{p_{b\perp}}{\sqrt{s}} e^{Y_b}, \quad x_2 = \frac{p_{a\perp}}{\sqrt{s}} e^{-Y_a} + \frac{p_{b\perp}}{\sqrt{s}} e^{-Y_b}$$

- p_{\perp} : transverse momenta of the produced particles
- Y : their rapidities
- \sqrt{s} : collision energy

Kinematical domain for the LHC

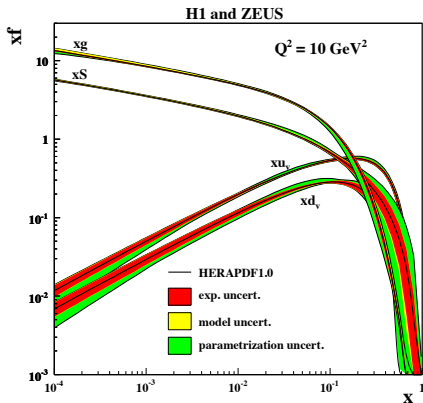


AA collisions at RHIC & LHC



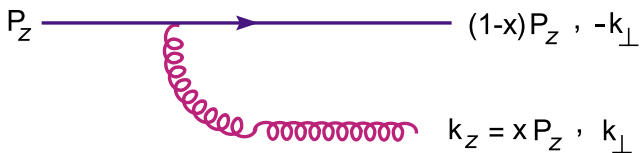
- 99% of the total multiplicity lies below $p_{\perp} = 2 \text{ GeV}$
 - $x \sim 10^{-2}$ at RHIC ($\sqrt{s} = 200 \text{ GeV}$)
 - $x \sim 4 \times 10^{-4}$ at the LHC ($\sqrt{s} = 5.5 \text{ TeV}$)
- ▷ partons at small x are the most important

Parton distributions at HERA



The gluon distribution rises very fast with increasing energy

- Gluon distribution $xg(x, Q^2)$: # of gluons with transverse size $\Delta x_{\perp} \sim 1/Q$ and longitudinal momentum $k_z = xP$



$$d\mathcal{P}_{\text{Brem}} \sim \alpha_s(k_\perp^2) C_R \frac{d^2 k_\perp}{k_\perp^2} \frac{dx}{x}$$

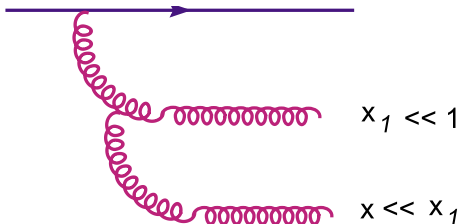
- Phase-space enhancement for the emission of
 - **collinear** ($k_\perp \rightarrow 0$)
 - and/or **soft (low-energy)** ($x \rightarrow 0$) gluons

- The parent parton can be either a **quark** or a **gluon**

$$C_F = t^a t^a = \frac{N_c^2 - 1}{2N_c} = \frac{4}{3}, \quad C_A = T^a T^a = N_c = 3$$

- The **daughter gluon** can in turn radiate an even **softer gluon** !

2 gluons



- The 'cost' of the addition gluon:

$$\alpha_s \int_x^1 \frac{dx_1}{x_1} = \alpha_s \ln \frac{1}{x}$$

Formally, a process of higher order in α_s , but which is enhanced by the available rapidity interval

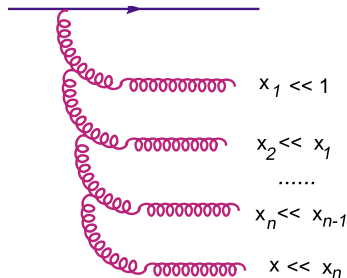
- $Y \equiv \ln(1/x)$: rapidity difference between the parent quark and the last emitted gluon
- When $\alpha_s Y \gtrsim 1 \implies$ need for resummation !

Gluon cascades

- n gluons strictly ordered in x
- The n -gluon cascade contributes

$$\frac{1}{n!} (\alpha_s Y)^n$$

- The sum of all the cascades exponentiates :



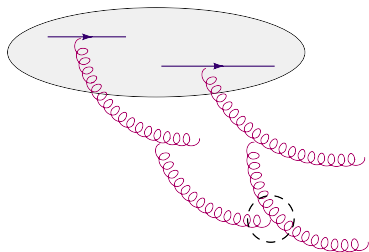
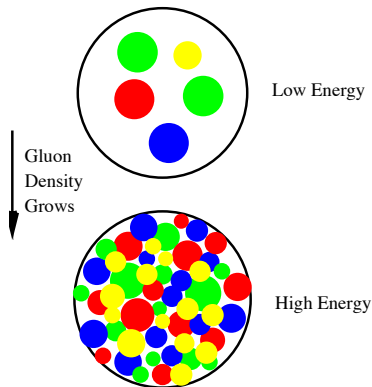
$$xg(x, Q^2) \propto e^{\omega \alpha_s Y} \quad \text{BFKL evolution}$$

(Balitsky, Fadin, Kuraev, Lipatov, 75–78)

- This evolution is **linear** :
the emitted gluons do not interact with each other

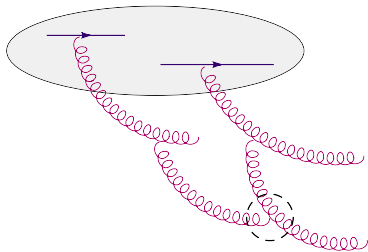
Gluon recombination

- The **gluon density** rises with decreasing x (increasing energy)



- Eventually gluons **start overlapping** with each other and then they interact: $2 \rightarrow 1$ **gluon recombination**
- These interactions stop the growth: **saturation**

Saturation momentum



- Number of gluons per unit area:

$$\mathcal{N} \sim \frac{x g_A(x, Q^2)}{\pi R_A^2}$$

- Recombination cross-section

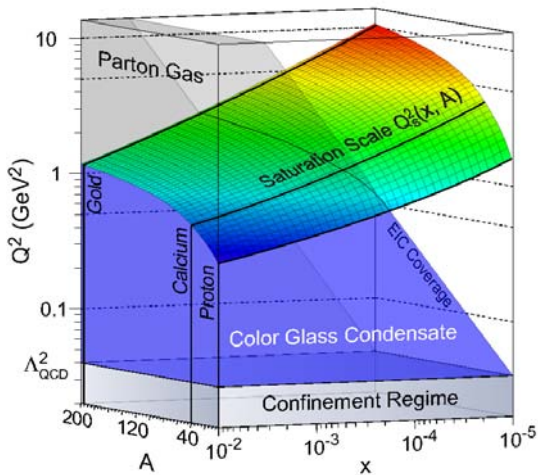
$$\sigma \sim \frac{\alpha_s}{Q^2}$$

- Recombination happens if $\mathcal{N}\sigma \gtrsim 1$, i.e. $Q^2 \lesssim Q_s^2$, with

$$Q_s^2(x, A) \simeq \alpha_s \frac{x g_A(x, Q_s^2)}{\pi R_A^2} \sim A^{1/3} \frac{1}{x^{0.25}}$$

- Low $Q^2 \implies$ large area $\sim 1/Q^2 \implies$ strong overlapping

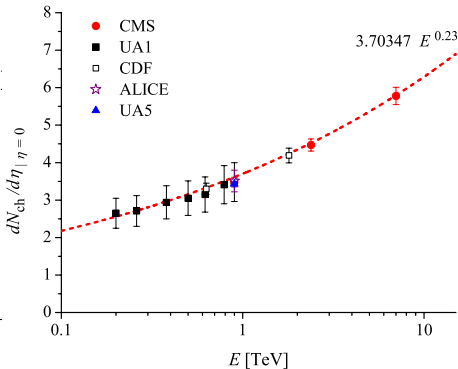
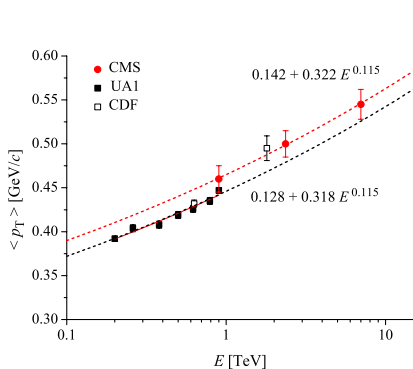
Saturation scale as a function of x and A



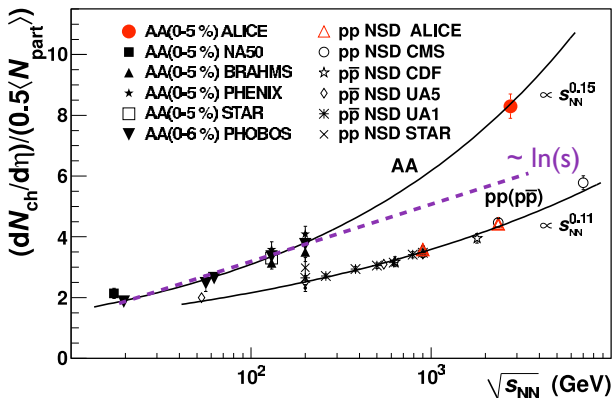
- $x \sim 10^{-5}$: $Q_s \sim 1$ GeV for proton and ~ 3 GeV for Pb or Au

Multiplicities at the LHC: $p+p$

- In a high-energy scattering, the saturated gluons are released in the final state
 - typical transverse momentum $\langle p_T \rangle \sim Q_s(E)$
 - average multiplicity $dN/d\eta \sim Q_s^2(E)$



Multiplicities in HIC: RHIC & LHC



- Logarithmic growth ($\ln s$) excluded by the LHC data
- Larger energy exponent (E^λ) for A+A than for p+p
 - ▷ this difference is theoretically understood

- A very robust, qualitative, prediction of saturation:
DIS at HERA, Au+Au at RHIC, p+p at the LHC ...
(looking forward to the relevant Pb+Pb data at the LHC)
- The single-inclusive spectra for particle production depend...
 - ... upon the particle transverse momentum p_T
 - ... and the COM energy of the collision \sqrt{s}

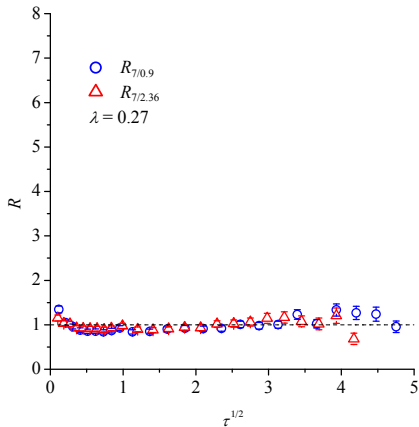
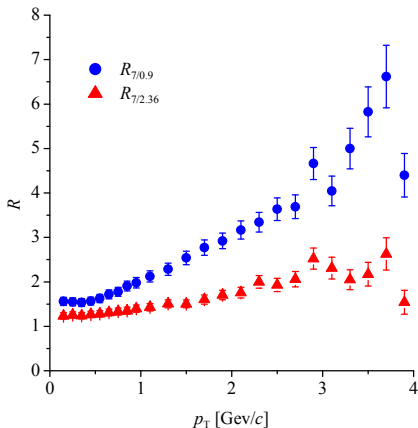
... only via the **ratio** of p_T to the saturation momentum Q_s :

$$\frac{dN}{d\eta d^2p_T} \simeq F(\tau) \quad \text{with} \quad \tau \equiv \frac{p_T^2}{Q_s^2(p_T/\sqrt{s})}$$

- At high energy, Q_s is the only intrinsic scale in the problem !

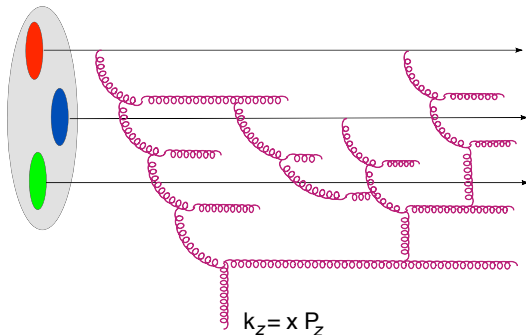
Geometric scaling at the LHC: p+p

$$R_{s_1/s_2} = \frac{(dN/d\eta d^2p_T)|_{s_1}}{(dN/d\eta d^2p_T)|_{s_2}} \rightarrow 1 \quad \text{as a function of } \tau \dots \text{ if scaling}$$



The need for an effective theory

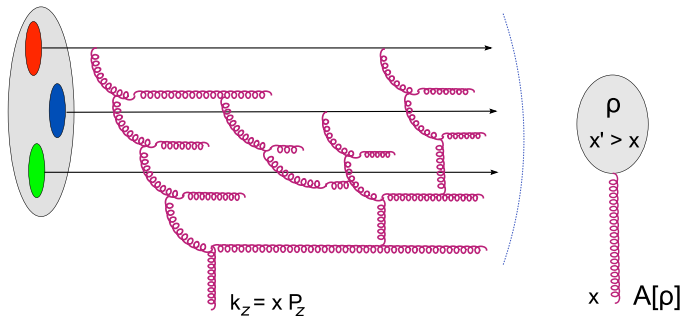
- How to compute the saturation scale from first principle ?



- Relatively hard scale ($Q_s \gg \Lambda_{\text{QCD}}$) \implies weak coupling !
- ... but high density \implies strong non-linear effects
- Solution: a reorganization of perturbation theory !

(McLerran and Venugopalan, 94; E.I., McLerran, and Leonidov, 00)

Color Glass Condensate



- **Small- x gluons:** classical color fields A_a^μ radiated by fast color charges ρ_a with $x' \gg x$, frozen in some random configuration
- $W_Y[\rho]$: probability distribution for the charge density at Y
- **Evolution equation** for $W_Y[\rho]$ with increasing $Y = \ln 1/x$

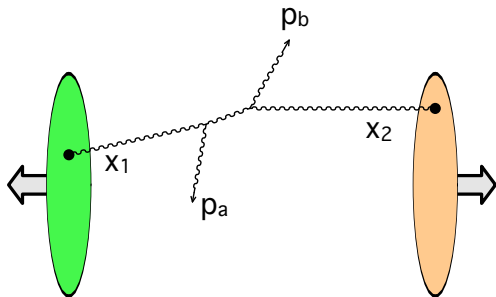
$$\frac{\partial}{\partial Y} W_Y[\rho] = H W_Y[\rho] \quad (\text{JIMWLK})$$

- A heavy ion collision at high energy



- Main difficulty: How to treat collisions involving a large number of partons ?

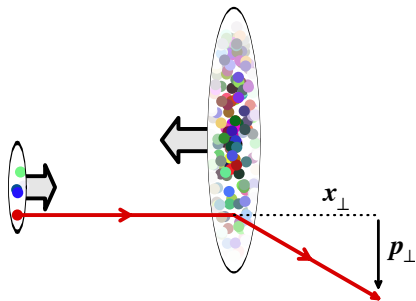
Proton–proton collisions



$$x_1 \sim \frac{p_{\perp}}{\sqrt{s}} e^Y$$
$$x_2 \sim \frac{p_{\perp}}{\sqrt{s}} e^{-Y}$$

- **Dilute–Dilute:** one parton from each projectile interact
 - **Collinear factorization** scheme of perturbative QCD
 - usual pdf's + DGLAP evolution
 - partonic cross–sections
- ▷ Caution: forward rapidity ($Y \gg 1$) & not too hard $p_{\perp} \Rightarrow x_2 \ll 1$

Proton–nucleus collisions (1)

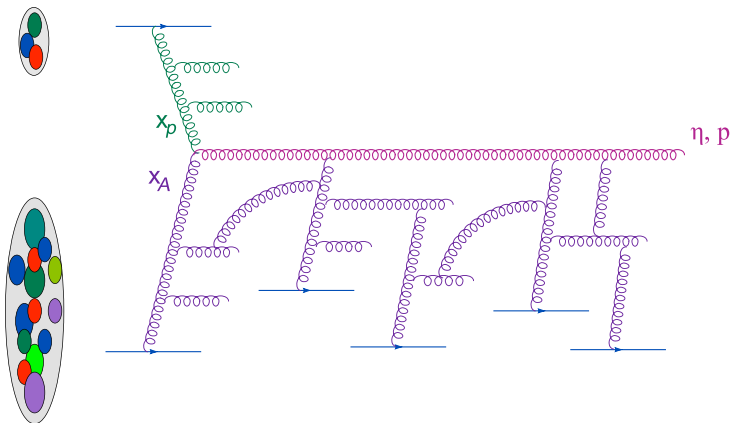


$$x_1 \sim \frac{p_{\perp}}{\sqrt{s}} e^Y \sim \mathcal{O}(1)$$

$$x_2 \sim \frac{p_{\perp}}{\sqrt{s}} e^{-Y} \ll 1$$

- **Most interesting situation:** forward particle production ($Y \gtrsim 3$) at 'semi-hard' momenta ($p_{\perp} \sim 1 \div 5$ GeV)
 - very small $x_2 \ll 1$ in the nucleus
 - p_{\perp} comparable to $Q_s(A, x_2)$
- **Dilute–Dense:** new factorization scheme needed
 - ▷ similar to deep inelastic scattering at small x

Proton–nucleus collisions (2)



- How to include both **multiple scattering** and **saturation** ?
 - proton = collinear factorization (large x_1)
 - nucleus = described as a CGC
 - parton—CGC cross-section to all orders in the gluon density

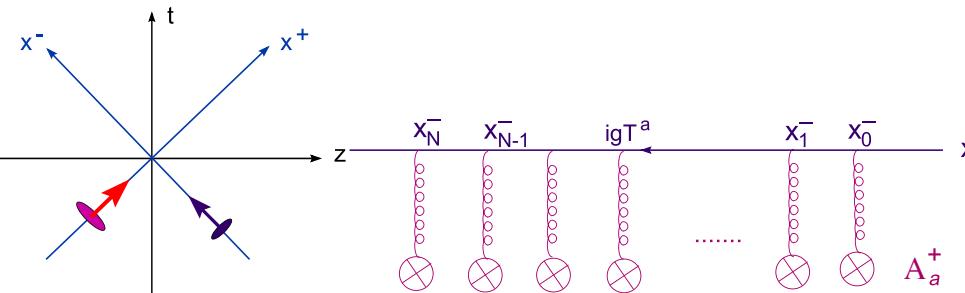
- The color charges in the target (ρ_a) are 'frozen' during the collision (by Lorentz time dilation)
 - compute the scattering between the parton and a fixed configuration of color charges
 - average over all the configurations by integrating over ρ_a with the CGC weight function

$$\left\langle \frac{dN}{dY d^2p_\perp} \right\rangle_Y = \int [\mathcal{D}\rho] W_Y[\rho] \frac{dN}{dY d^2p_\perp}[\rho]$$

- The target color field A_a^μ (as generated by ρ_a) is strong and must be resummed to all orders

Eikonal approximation

- A very energetic particle is **not deflected** by its interactions



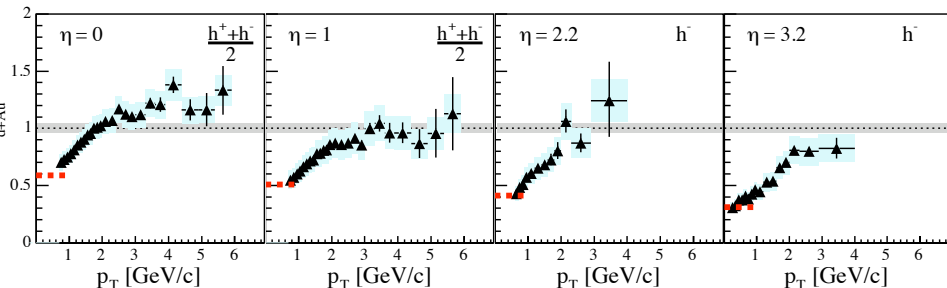
- The sum of all the interactions simply **exponentiates**
- The single-particle state gets multiplied by a complex exponential known as **Wilson line**

$$\Psi_i(x_\perp) \rightarrow U_{ij}(x_\perp) \Psi_j(x_\perp), \quad U(x_\perp) = \text{T exp} \left\{ i \int dx^- A_a^+(x^-, x_\perp) t^a \right\}$$

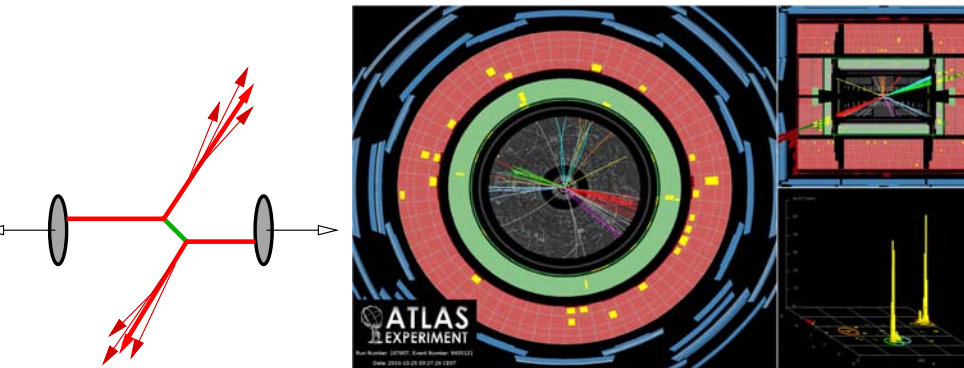
Nuclear modification factor in d+Au at RHIC

$$R_{d+Au} \equiv \frac{1}{2A} \frac{dN_{d+Au}/d^2p_{\perp}d\eta}{dN_{pp}/d^2p_{\perp}d\eta}$$

- R_{d+Au} would be one in the absence of nuclear effects

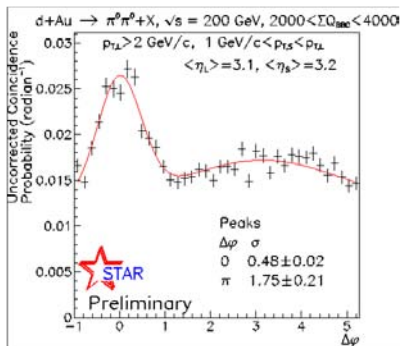
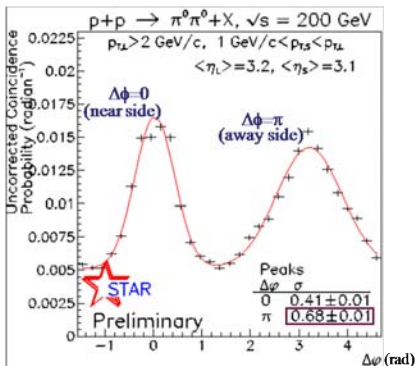
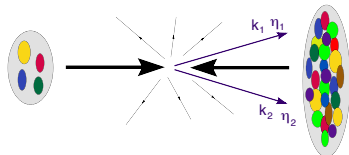
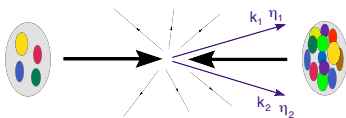


- R_{d+Au} decreases with increasing rapidity
- Strong suppression ($R \sim 0.5$) for $\eta = 3$: coherent scattering



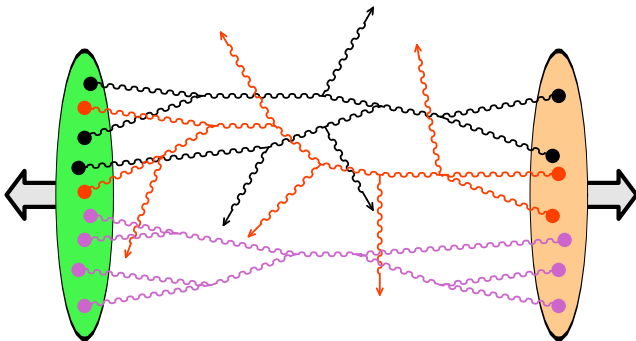
- Two back-to-back jets in the transverse plane:
visible via 2-particle azimuthal correlations

Di-jet correlations at RHIC: p+p vs. d+Au



- d+Au : the 'away jet' gets smeared out = saturation in Au

Nucleus–nucleus collisions

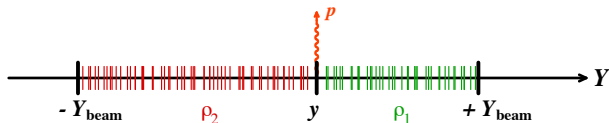


- Non-linear effects in the wavefunctions: **gluon saturation**
 - 2 CGC weight functions: $W_{Y_1}[\rho_1]$, $W_{Y_2}[\rho_2]$
 - generalized pdf's : **multi-parton correlations**
- ... and in the scattering: **multiple interactions**
 - **classical Yang–Mills equations with 2 sources**

The CGC factorization

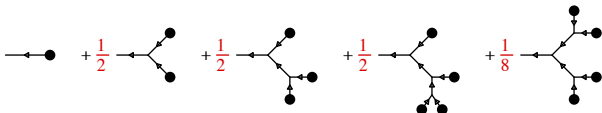
- Gluon production in the scattering between 2 CGC's :

$$\left\langle \frac{dN}{dY d^2p_\perp} \right\rangle = \int [D\rho_1 D\rho_2] W_{Y_{\text{beam}-y}[\rho_1]} W_{Y_{\text{beam}+y}[\rho_2]} \left. \frac{dN}{dY d^2p_\perp} \right|_{\text{class}}$$



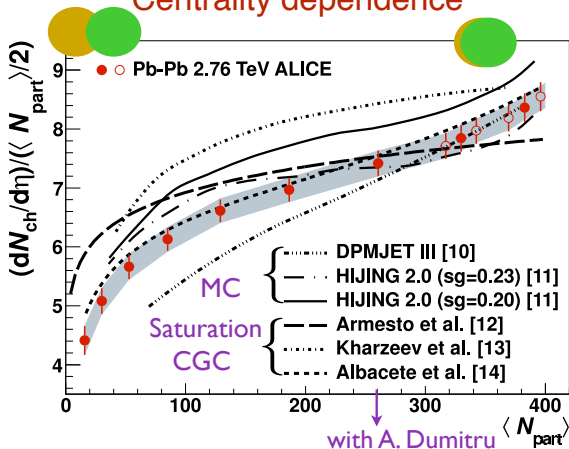
- The classical solution is **non-linear** to all orders in ρ_1 and ρ_2 :

$$D_\nu F^{\nu\mu}(x) = \delta^{\mu+} \rho_1(x) + \delta^{\mu-} \rho_2(x)$$



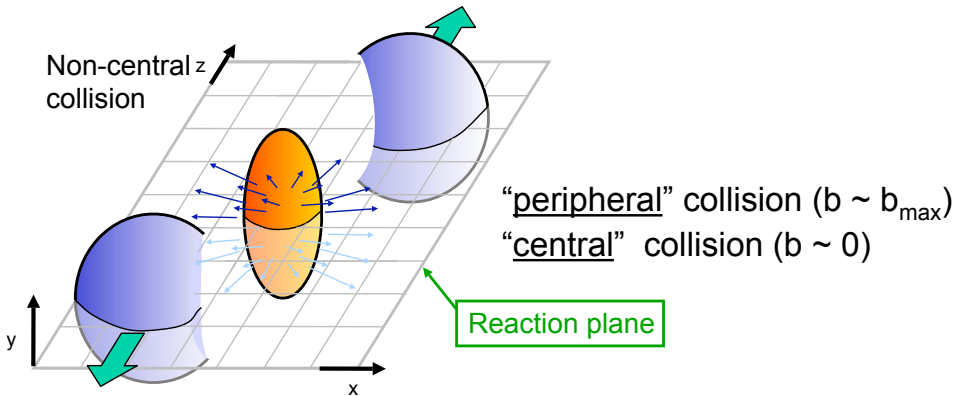
- All the leading logs of $1/x_{1,2}$ are absorbed in the W 's.

Centrality dependence



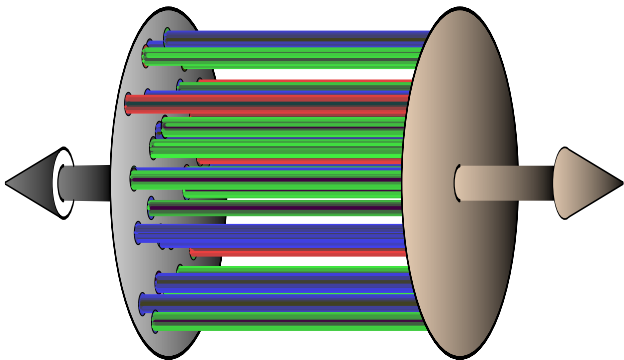
- Excellent fit by the CGC approach
- All the models include some form of saturation
 - ▷ HIJING : energy dependent low- p_T cutoff

The geometry of a HIC



Number of participants (N_{part}): number of incoming nucleons (participants) in the overlap region

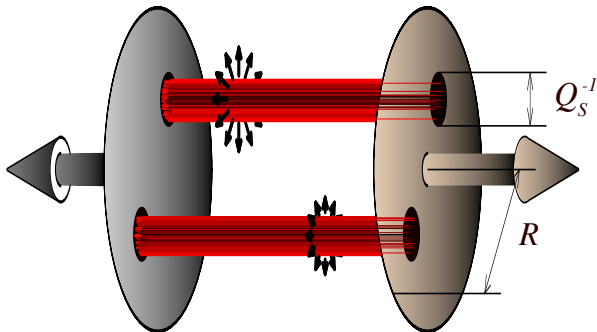
- Immediately after the collision, the **chromo-electric** and **chromo-magnetic** fields are **purely longitudinal**
- They form **flux tubes** extending between the projectiles



- **Glasma** : the intermediate stage between the **CGC** and the Quark Gluon Plasma (*McLerran and Lappi, 06*)

Color flux tubes

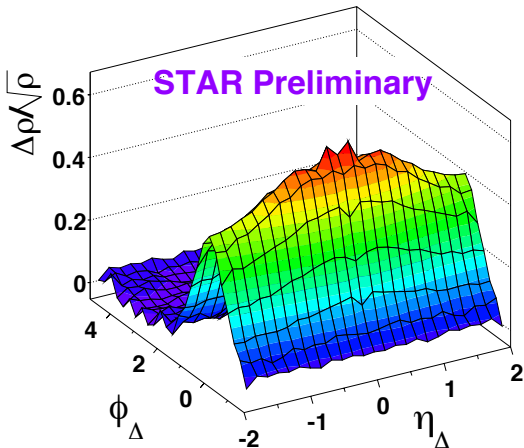
- Correlation length in the transverse plane: $\Delta r_{\perp} \sim 1/Q_s$
- Correlation length in rapidity (y or η): $\Delta \eta \sim 1/\alpha_s$



- The color fluxes eventually **break into 'particles'** (gluons)
- Gluons emitted from **different** flux tubes are **not** correlated

The ridge in HIC at RHIC

- A natural explanation for the the 'ridge'



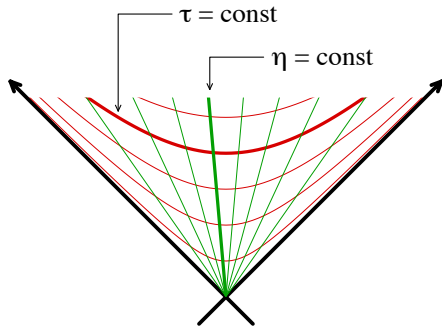
- Long-range correlations in rapidity $\Delta\eta$
- Narrow correlation in azimuthal angle $\Delta\phi$

Di-hadron correlations

- In a given event count the number of particles N_1 in a given bin centered at (η_1, ϕ_1) and similarly N_2 .

$$\mathcal{R} \equiv \frac{\langle N_1 N_2 \rangle - \langle N_1 \rangle \langle N_2 \rangle}{\langle N_1 \rangle \langle N_2 \rangle}$$

$$\Delta\eta = \eta_1 - \eta_2, \quad \Delta\phi = \phi_1 - \phi_2$$



- Recall: pseudo-rapidity

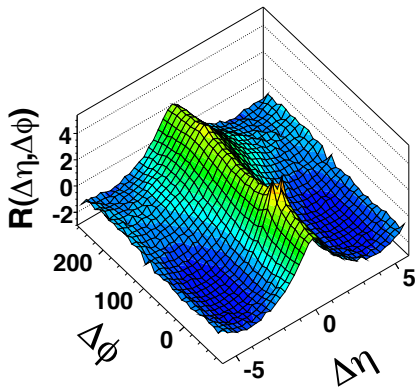
$$\eta = \frac{1}{2} \ln \frac{p + p_z}{p - p_z}$$

$$\eta = -\ln \tan \frac{\theta}{2}, \quad \theta = \frac{p_z}{p}$$

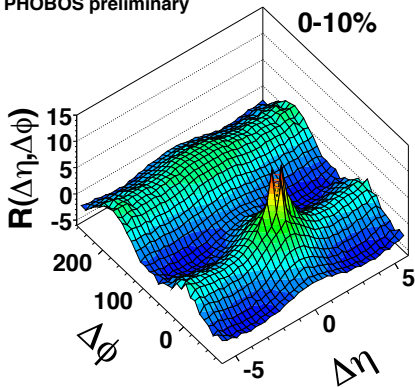
$$\tau = \sqrt{t^2 - z^2}$$

Di-hadron correlations: p+p vs Au+Au

- **p+p** : peak around $\Delta\eta = 0$ & flat in $\Delta\phi$
 - ▷ correlated particles make similar angles with the beam axis



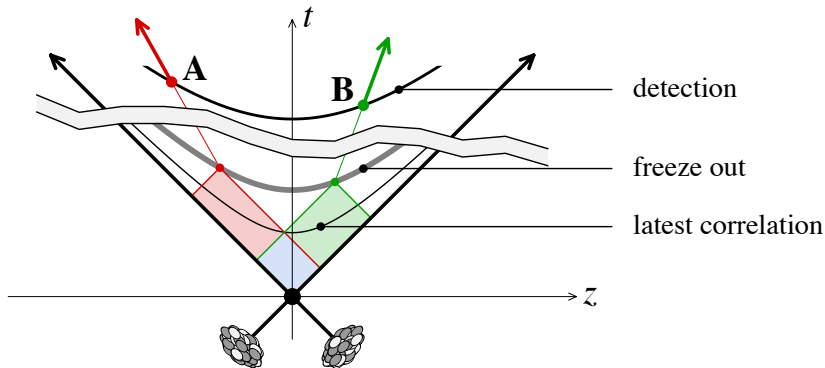
PHOBOS preliminary



- **Au+Au** :
 - almost flat over $\Delta\eta \simeq 10$ & 2 peaks at $\Delta\phi = 0$ and $\Delta\phi = \pi$

Long-range rapidity correlations probe early times

- Generated at **early stages**, where particles with different longitudinal velocities were still **causally connected**

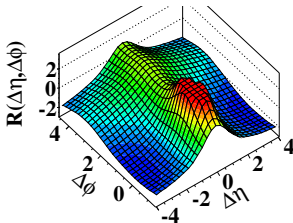


$$\tau_{\text{correlation}} \leq \tau_{\text{freeze-out}} e^{-|\eta_A - \eta_B|/2}$$

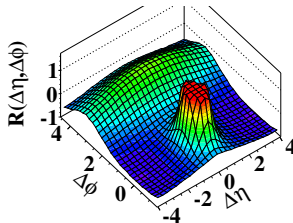
The ridge in p+p at CMS (1)

- A small ridge has been seen in **p+p collisions** at the LHC

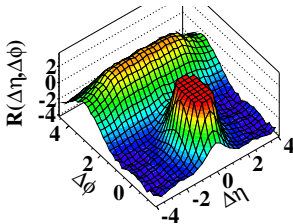
(a) CMS MinBias, $p_T > 0.1 \text{ GeV}/c$



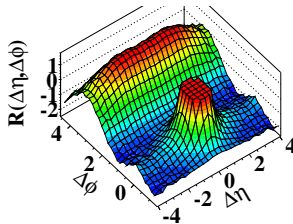
(b) CMS MinBias, $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



(c) CMS $N \geq 110$, $p_T > 0.1 \text{ GeV}/c$



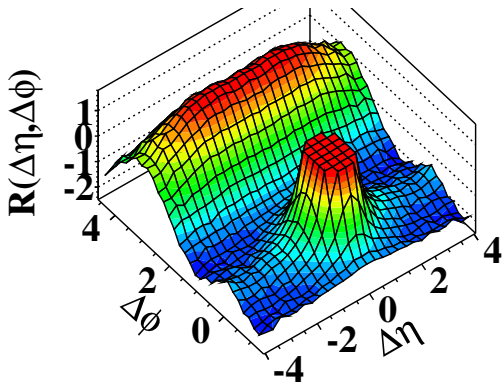
(d) CMS $N \geq 110$, $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



The ridge in p+p at CMS (2)

- ... but only in **specially selected events** !

(d) CMS $N \geq 110$, $1.0 \text{ GeV}/c < p_{\perp} < 3.0 \text{ GeV}/c$

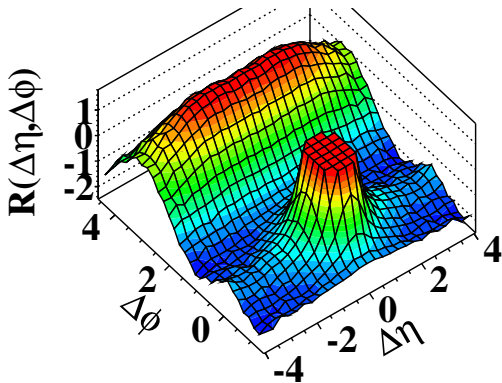


- High-multiplicity (\implies very central): $N \geq 110$ particles
- Narrow interval in transverse momentum: $1 \leq p_{\perp} \leq 3 \text{ GeV}$

The ridge in p+p at CMS (2)

- ... but only in **specially selected events** !

(d) CMS $N \geq 110$, $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



- ... which look a lot like a heavy ion collision !!

▷ N.B. $1 \leq p_{\perp} \leq 3 \text{ GeV}$ is similar to the proton Q_s at LHC