

# Probes of high-energy heavy-ion collisions

Nicolas BORGHINI

Universität Bielefeld

# Probes of high-energy heavy-ion collisions

## Physical aspects

- Mandatory motivation slides
- Time evolution of an ultra-relativistic heavy-ion collision
- Hard probes
- Collective probes

# Hints from lattice QCD

Volume 113B, number 5

PHYSICS LETTERS

1 July 1982

## THE HIGH-TEMPERATURE BEHAVIOUR OF LATTICE QCD WITH FERMIONS

J. ENGELS, F. KARSCH and H. SATZ

*Fakultät für Physik, Universität Bielefeld, Bielefeld, Germany*

Received 29 March 1982

By Monte Carlo simulation on the lattice, we calculate the high-temperature behaviour of the energy density  $\epsilon$  in SU(2) and SU(3) QCD with Wilson fermions. From the leading term of the hopping parameter expansion, we find that  $\epsilon$  converges very rapidly to the Stefan–Boltzmann limit of an asymptotically free quark–gluon gas. ...

# Hints from lattice QCD

PHYSICAL REVIEW D 77, 014511 (2008)

## QCD equation of state with almost physical quark masses

M. Cheng,<sup>1</sup> N. H. Christ,<sup>1</sup> S. Datta,<sup>2</sup> J. van der Heide,<sup>3</sup> C. Jung,<sup>4</sup> F. Karsch,<sup>3,4</sup> O. Kaczmarek,<sup>3</sup> E. Laermann,<sup>3</sup>  
R. D. Mawhinney,<sup>1</sup> C. Miao,<sup>3</sup> P. Petreczky,<sup>4,5</sup> K. Petrov,<sup>6</sup> C. Schmidt,<sup>4</sup> W. Soeldner,<sup>4</sup> and T. Umeda<sup>7</sup>

<sup>1</sup>*Physics Department, Columbia University, New York, New York 10027, USA*

<sup>2</sup>*Department of Theoretical Physics, Tata Institute of Fundamental Research, Homi Bhabha Road, Mumbai 400005, India*

<sup>3</sup>*Fakultät für Physik, Universität Bielefeld, D-33615 Bielefeld, Germany*

<sup>4</sup>*Physics Department, Brookhaven National Laboratory, Upton, New York 11973, USA*

<sup>5</sup>*RIKEN-BNL Research Center, Brookhaven National Laboratory, Upton, New York 11973, USA*

<sup>6</sup>*Niels Bohr Institute, University of Copenhagen, Blegdamsvej 17, DK-2100 Copenhagen, Denmark*

<sup>7</sup>*Graduate School of Pure and Applied Sciences, University of Tsukuba, Tsukuba, Ibaraki 305-8571, Japan*

(Received 2 October 2007; published 22 January 2008)

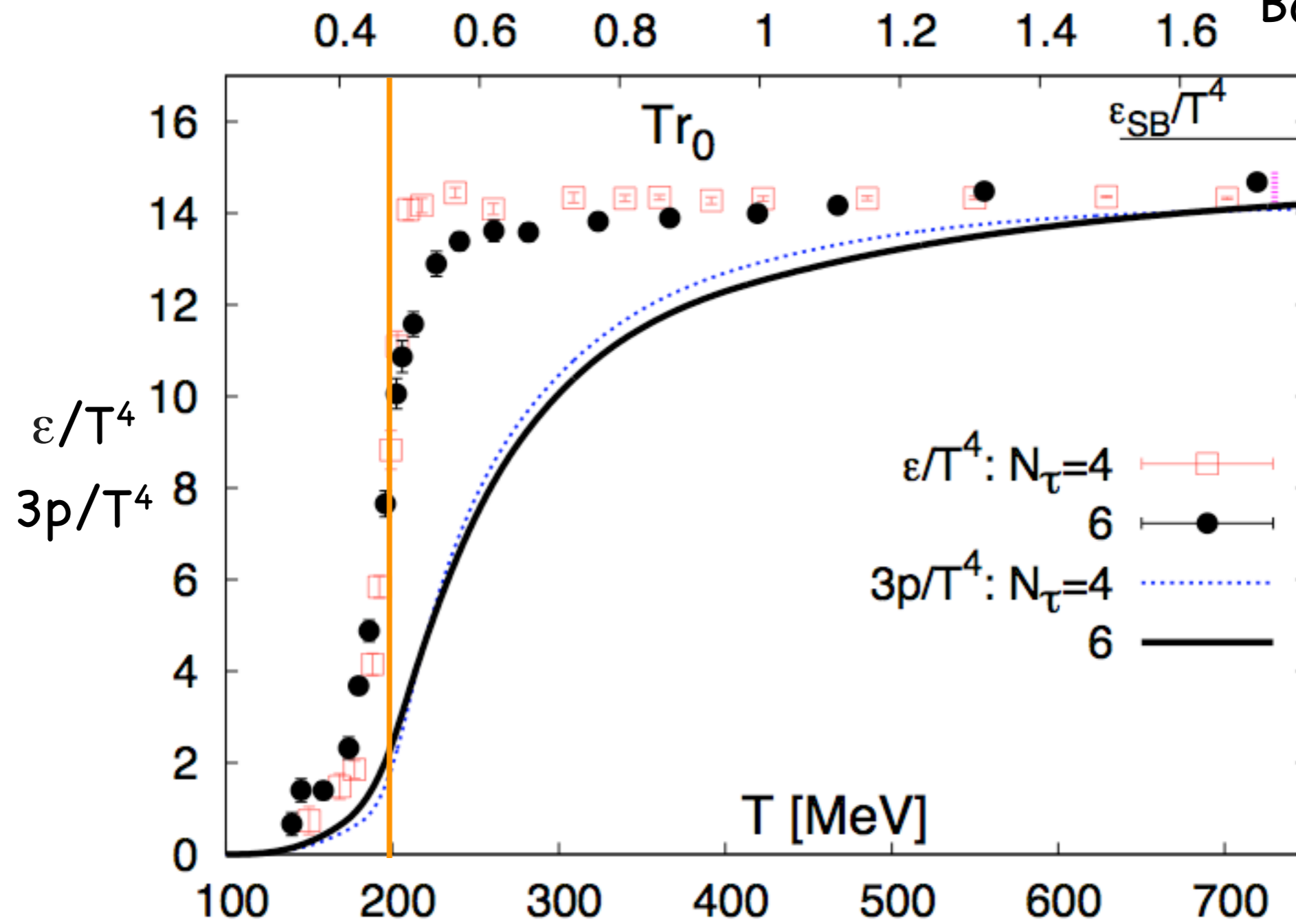
We present results on the equation of state in QCD with two light quark flavors and a heavier strange quark. Calculations with improved staggered fermions have been performed on lattices ...

“2+1” flavors,  $m_\pi \approx 220$  MeV,  $m_K \approx 500$  MeV

# Hints from lattice QCD

Energy density  $\varepsilon$  & pressure  $p$ :

ideal Stefan-Boltzmann limit



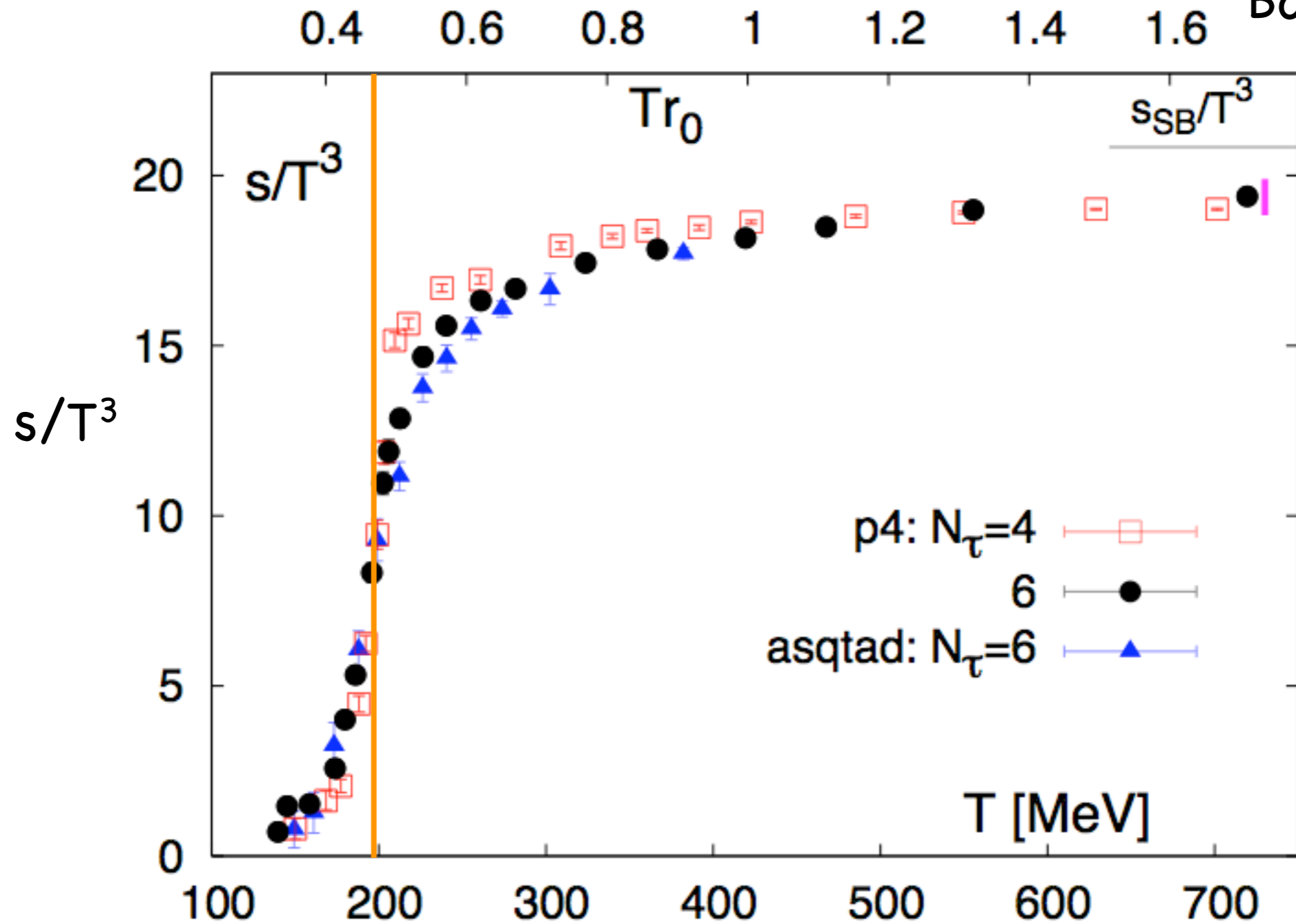
PRD 77 (2008) 045511



# Hints from lattice QCD

Entropy density  $s$

ideal Stefan-Boltzmann limit

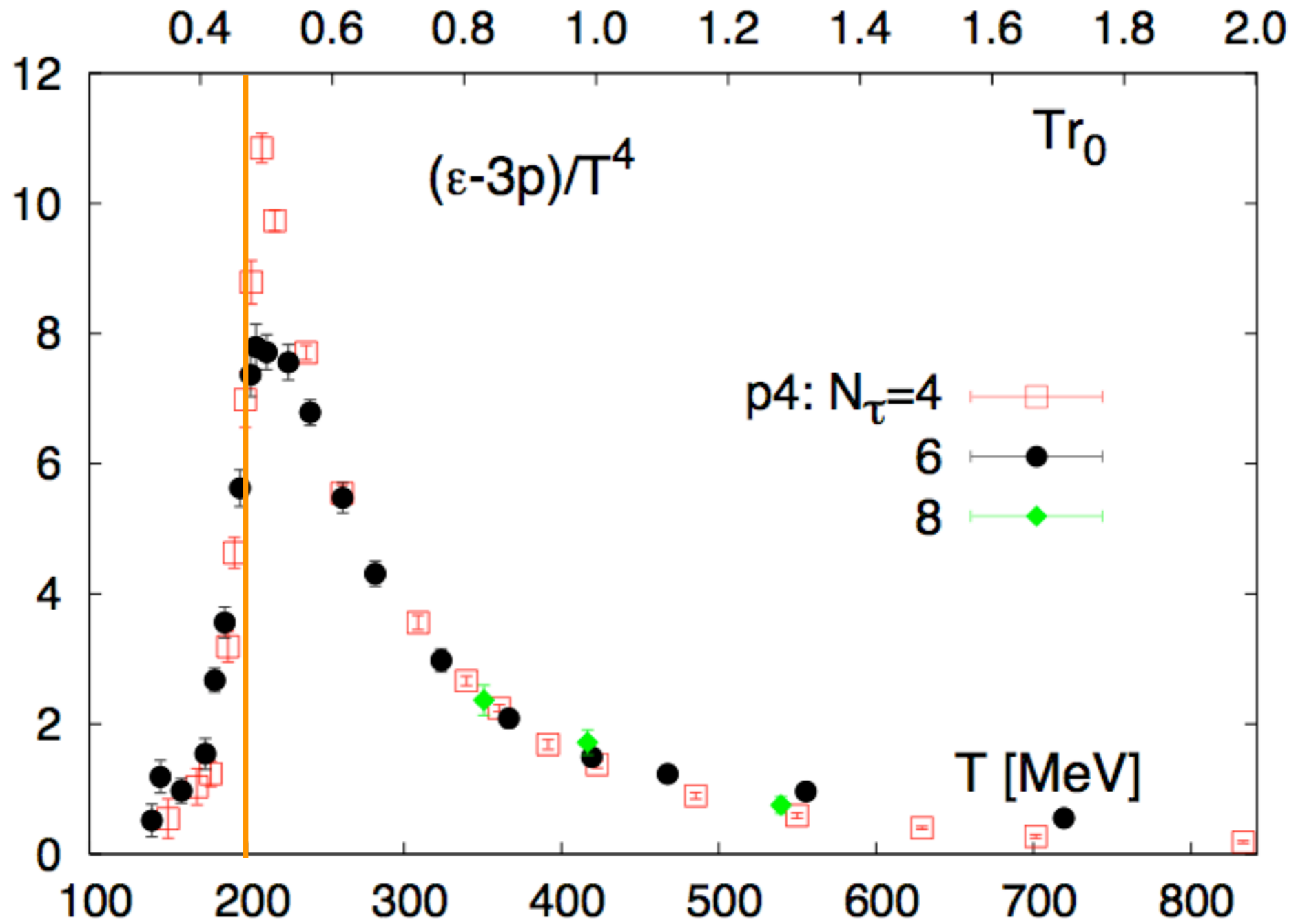


PRD 77 (2008) 045511



# Hints from lattice QCD

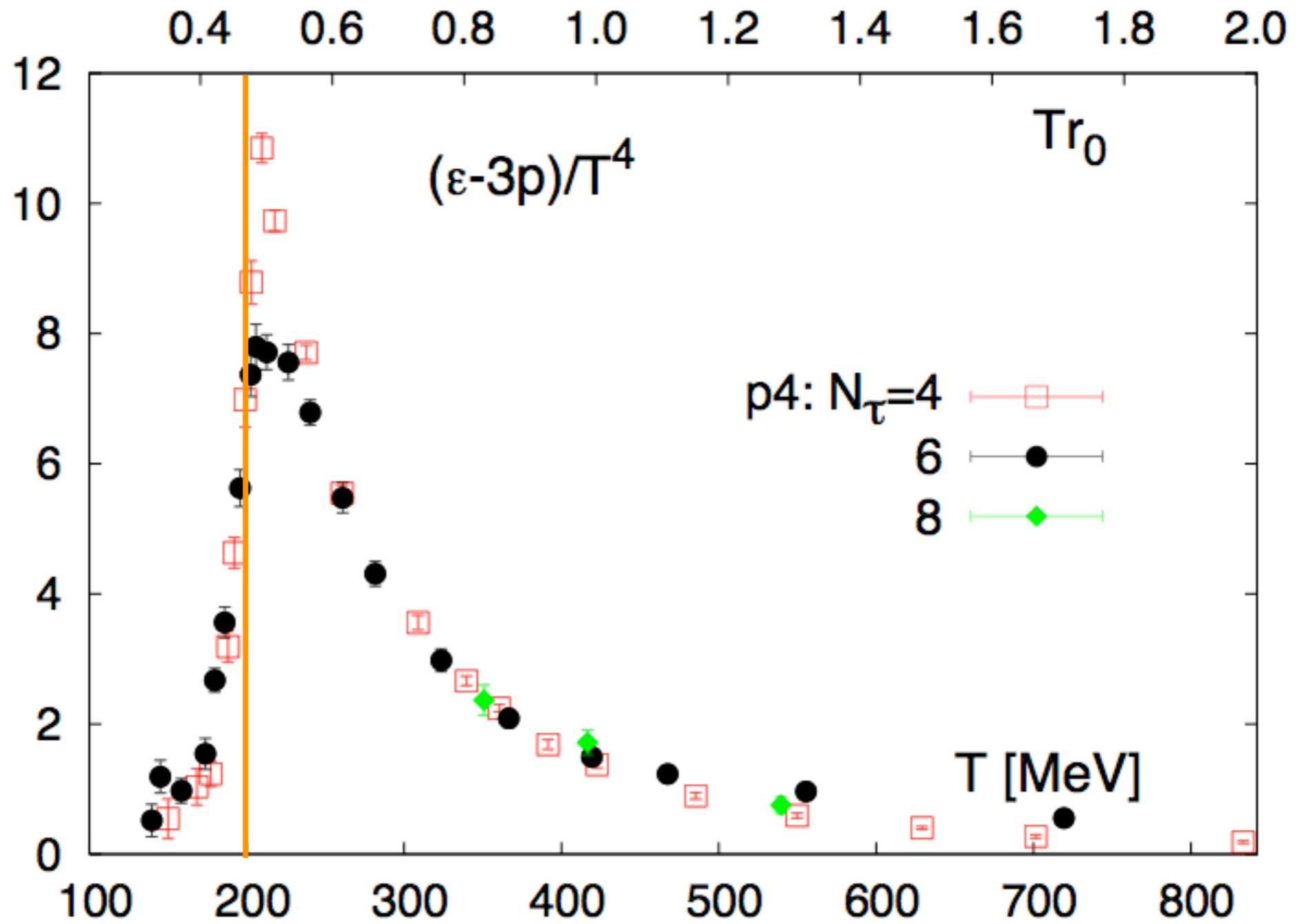
Critical temperature  $T_c = 196 \pm 4$  MeV



PRD 77 (2008) 045511

# Hints from lattice QCD

Critical temperature  $T_c \approx 150-200$  MeV

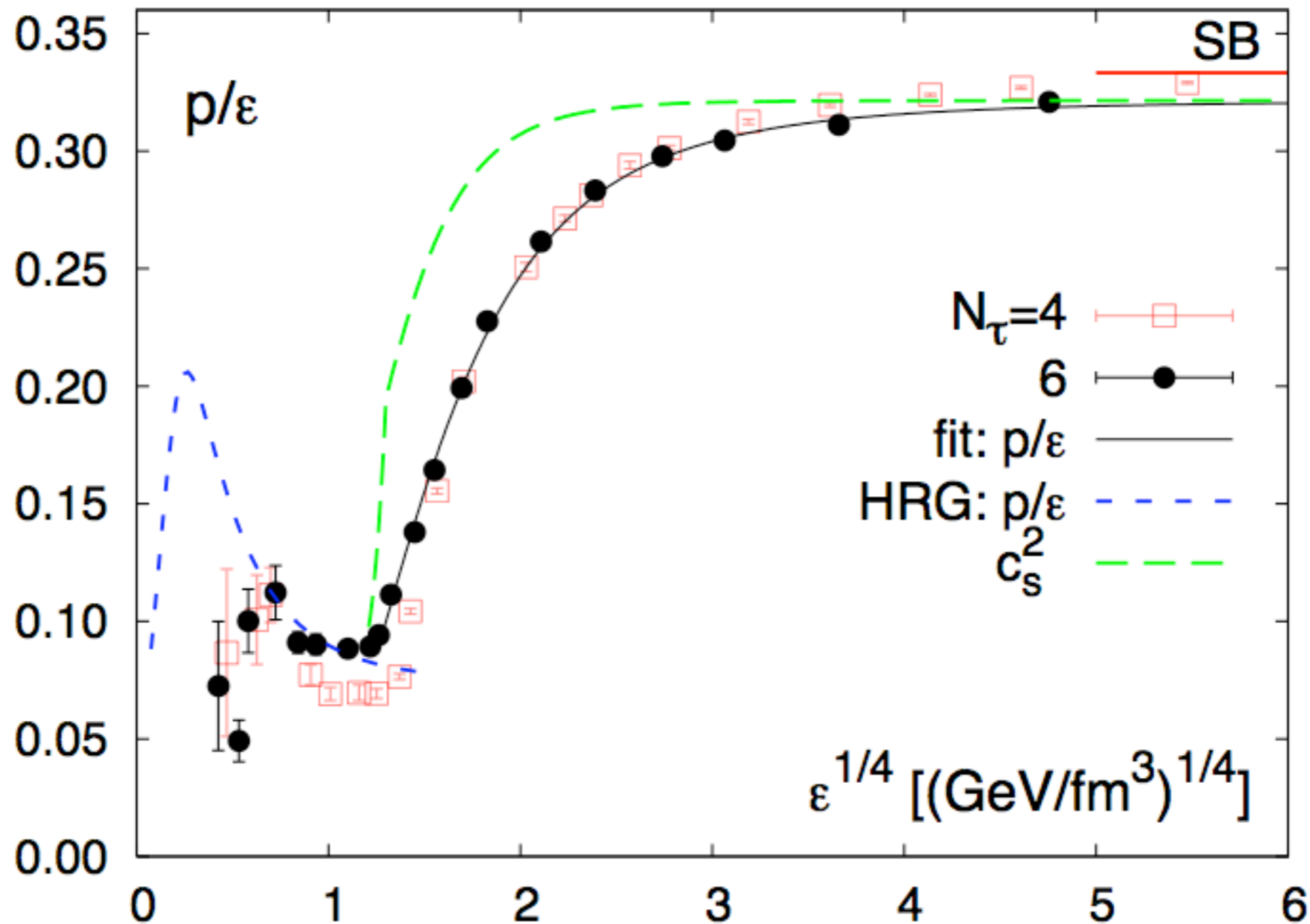


PRD 77 (2008) 045511



# Hints from lattice QCD

$\frac{dp}{d\varepsilon}$   sound velocity  $c_s$ :  $c_s^2 = \frac{dp}{d\varepsilon} = \varepsilon \frac{d(p/\varepsilon)}{d\varepsilon} + \frac{dp}{d\varepsilon}$

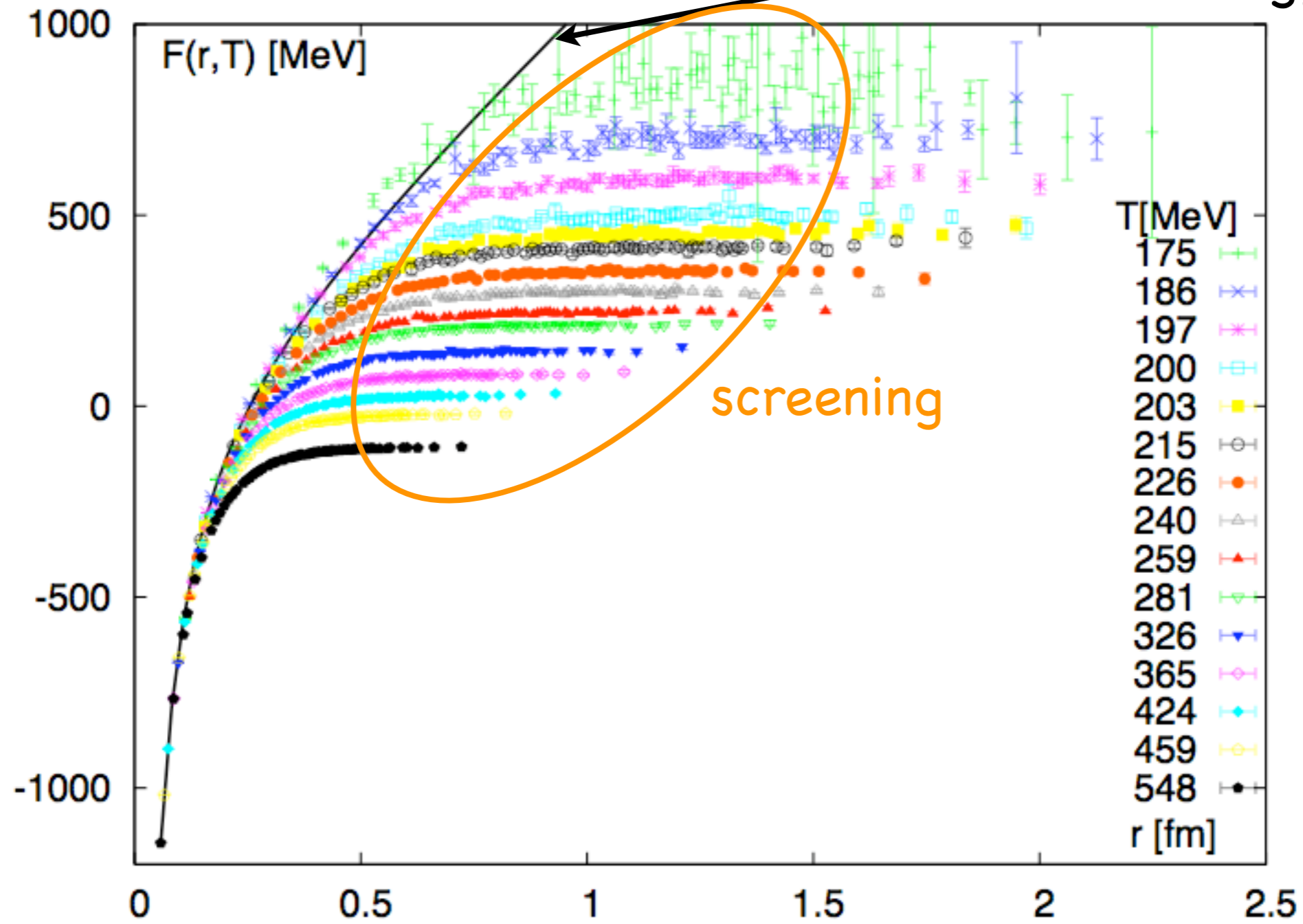


PRD 77 (2008) 045511

# Hints from lattice QCD

Heavy quark free energy

vacuum free energy



O.Kaczmarek, PoS CPOD07 (2007) 043



# Hints from lattice QCD

- Rapid change of **thermodynamic quantities** (energy density, pressure, entropy density...) ➡ transition / crossover between two states:

**hadron gas** vs. **Quark-Gluon Plasma**

- Screening of the **heavy-quark** potential in the high-temperature phase.
- Equation of state, **sound velocity**...

# Hints from lattice QCD

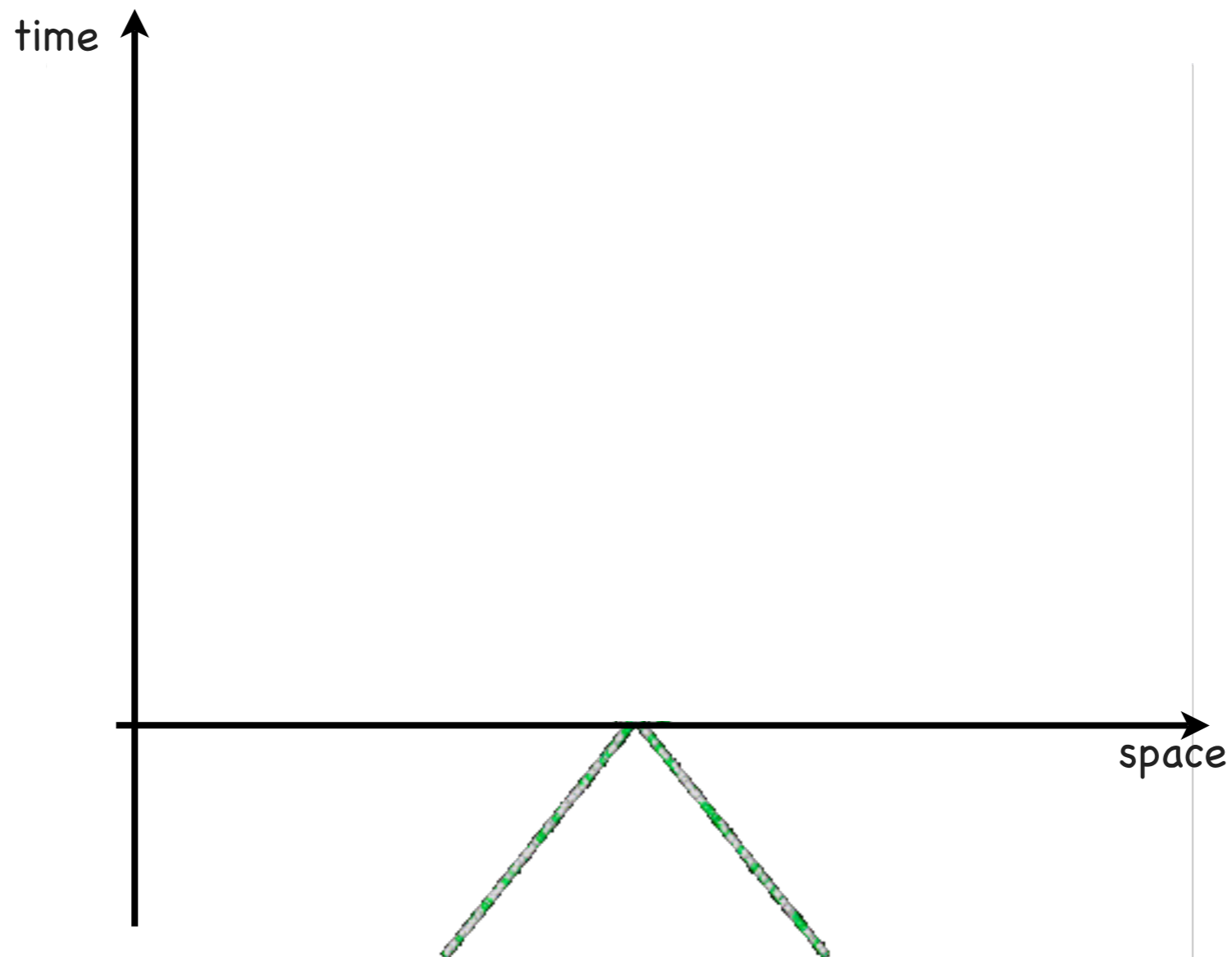
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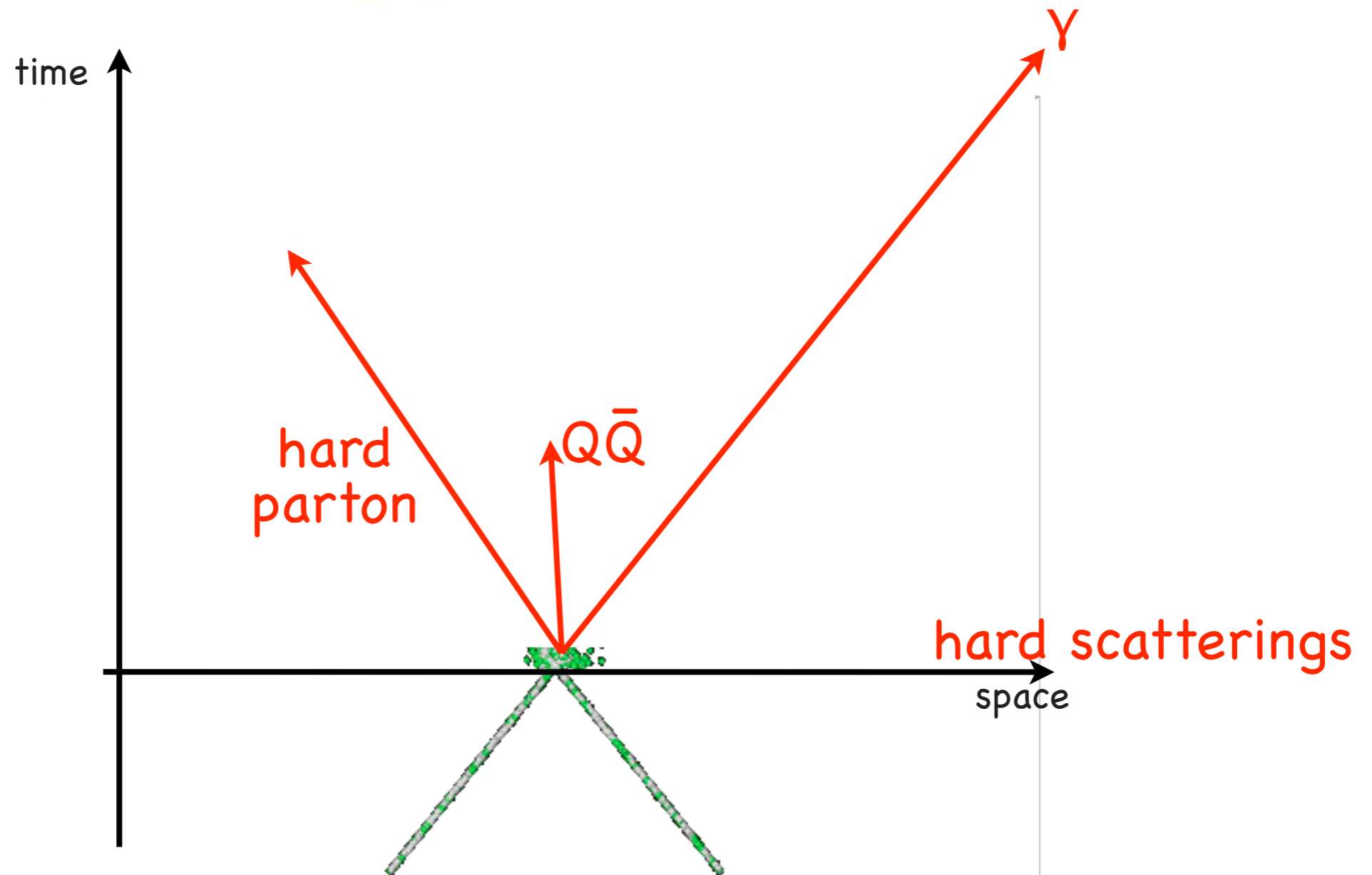
- Screening of the **heavy-quark** potential in the high-temperature phase.
- Equation of state, **sound velocity**...
- However lattice simulations of **QCD** at finite temperature are not (yet) performed with “physical” light-quark masses.
- They do not provide any phase diagram,
- nor **transport coefficients**.

(yet?)

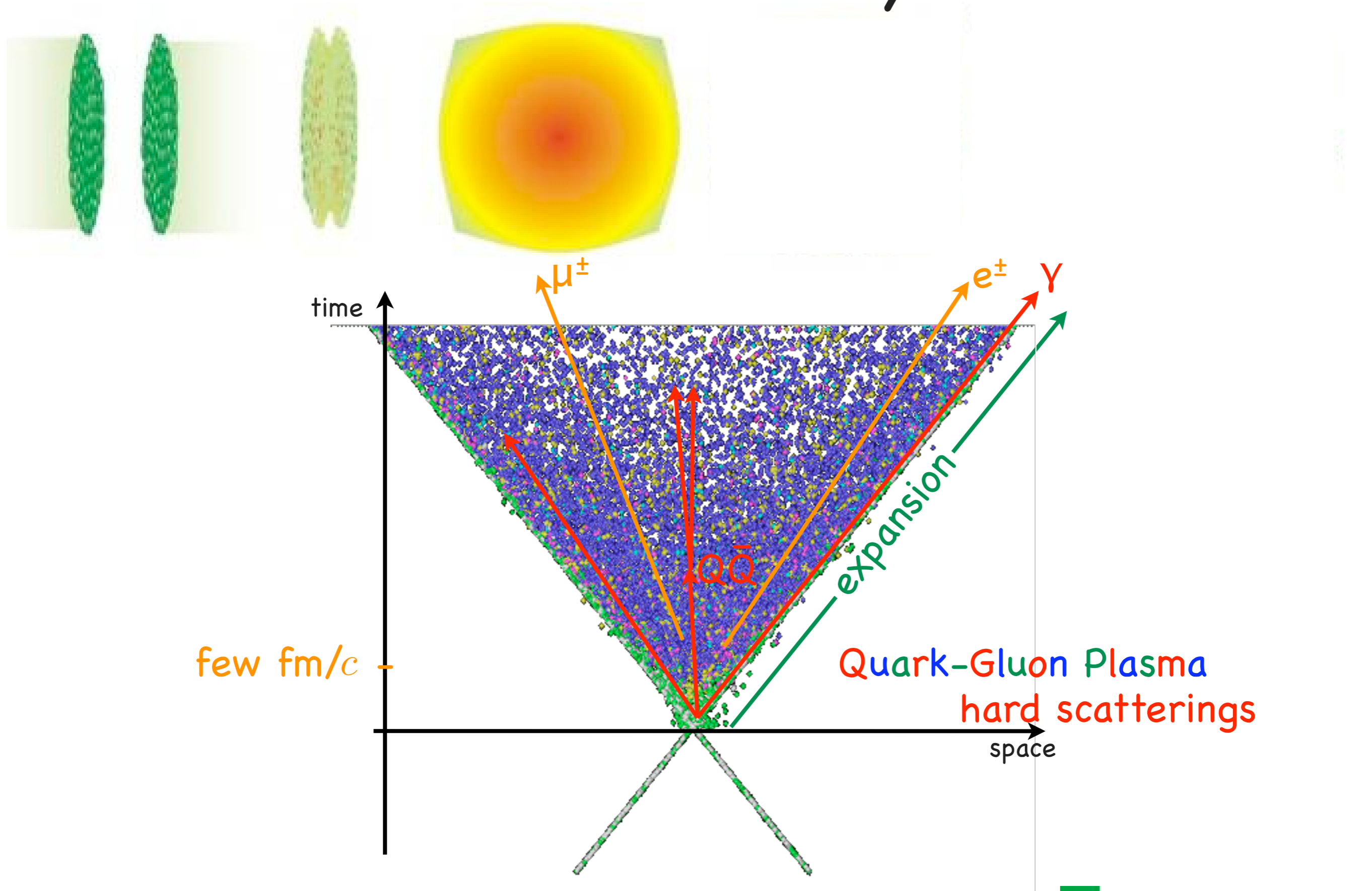
# Time evolution of a heavy-ion collision



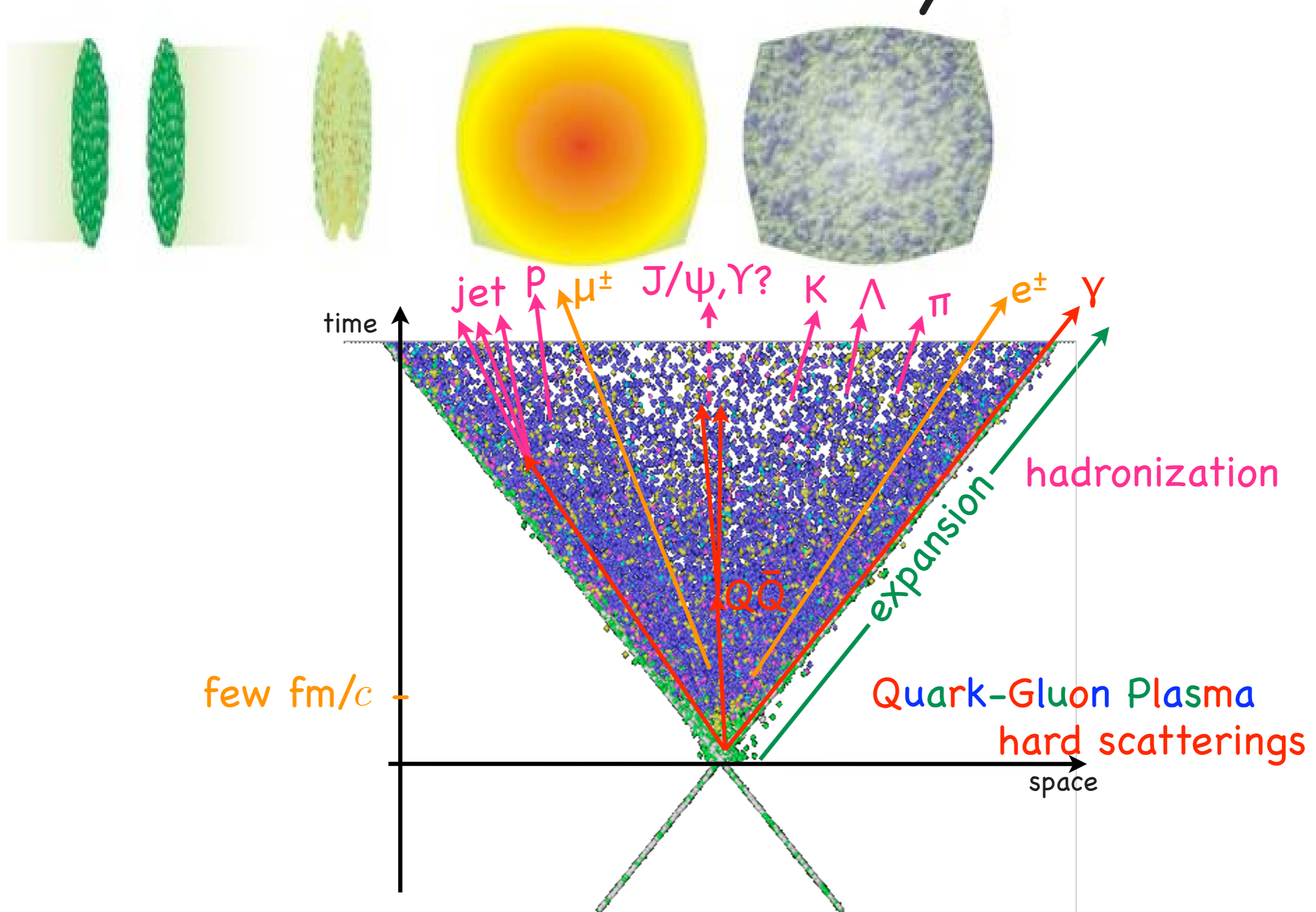
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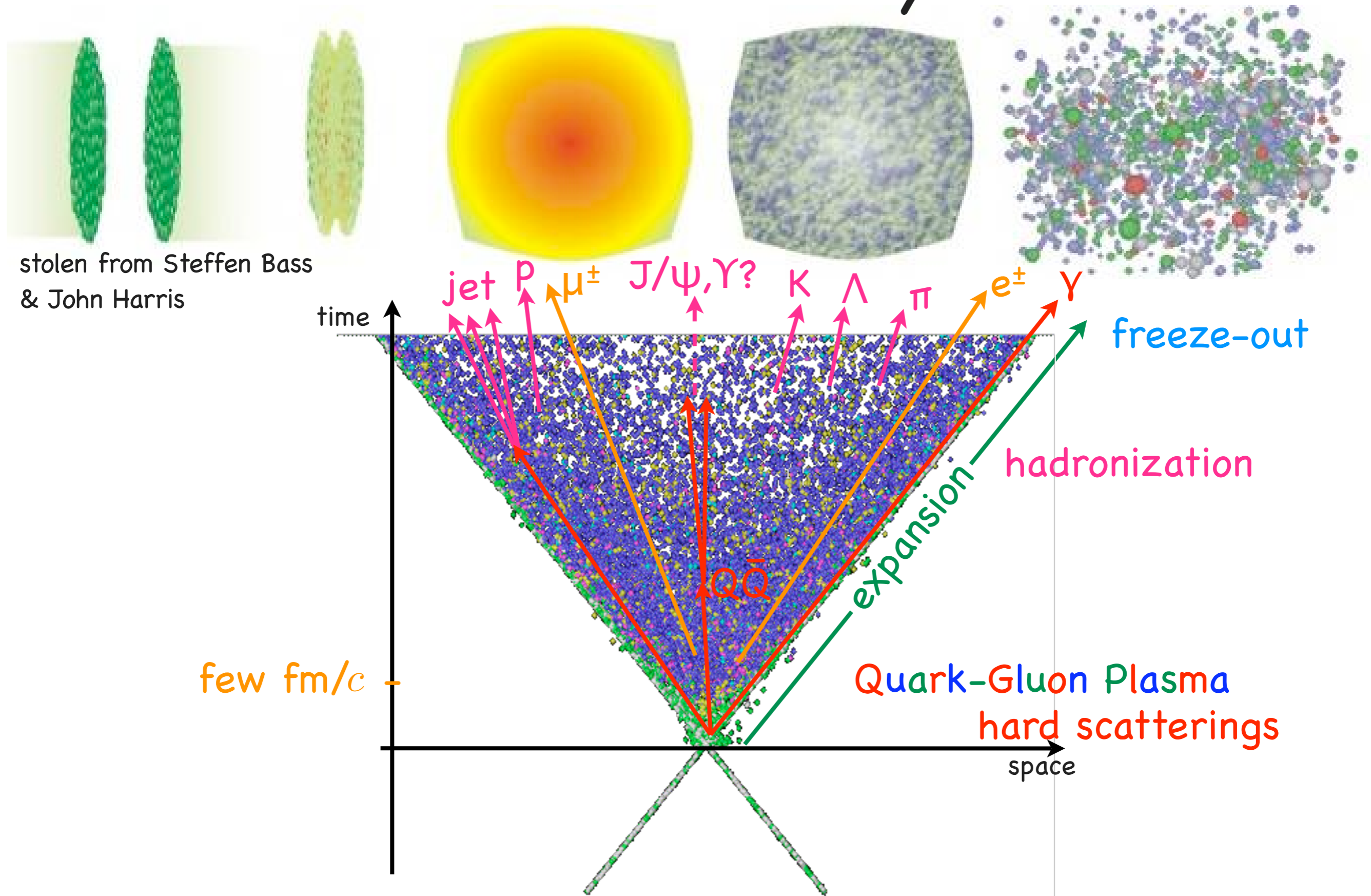


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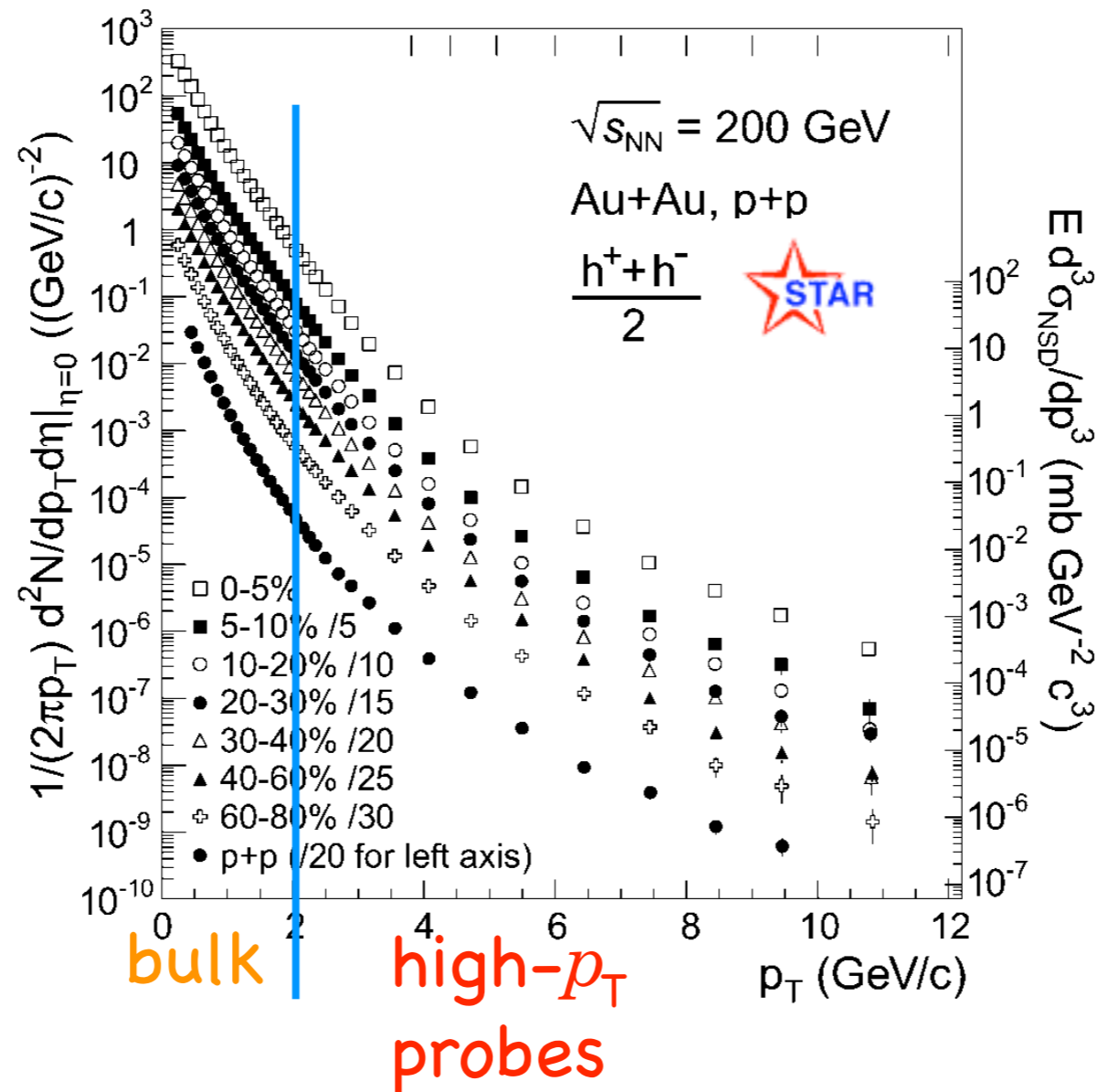




# Time evolution of a heavy-ion collision



# Bulk observables vs. hard probes



Only few particles with **high transverse momenta** (or containing **heavy quarks**), but their production mechanism is a priori better understood (perturbative **QCD**): can **probe** the **bulk**.

# Hard probes (1): quarkonia suppression

Volume 178, number 4

PHYSICS LETTERS B

9 October 1986

## **$J/\psi$ SUPPRESSION BY QUARK–GLUON PLASMA FORMATION** ☆

**T. MATSUI**

*Center for Theoretical Physics, Laboratory for Nuclear Science, Massachusetts Institute of Technology,  
Cambridge, MA 02139, USA*

and

**H. SATZ**

*Fakultät für Physik, Universität Bielefeld, D-4800 Bielefeld, Fed. Rep. Germany  
and Physics Department, Brookhaven National Laboratory, Upton, NY 11973, USA*

Received 17 July 1986

If high energy heavy ion collisions lead to the formation of a hot quark–gluon plasma, then colour screening prevents  $c\bar{c}$  binding in the deconfined interior of the interaction region.

It is concluded that  $J/\psi$  suppression in nuclear collisions should provide an unambiguous signature of quark–gluon plasma formation.

# Hard probes (1): quarkonia suppression

Screening of the heavy-quark-antiquark potential (cf. lattice results)

☞ suppression of heavy quarkonia.

Life is unfortunately not so easy...

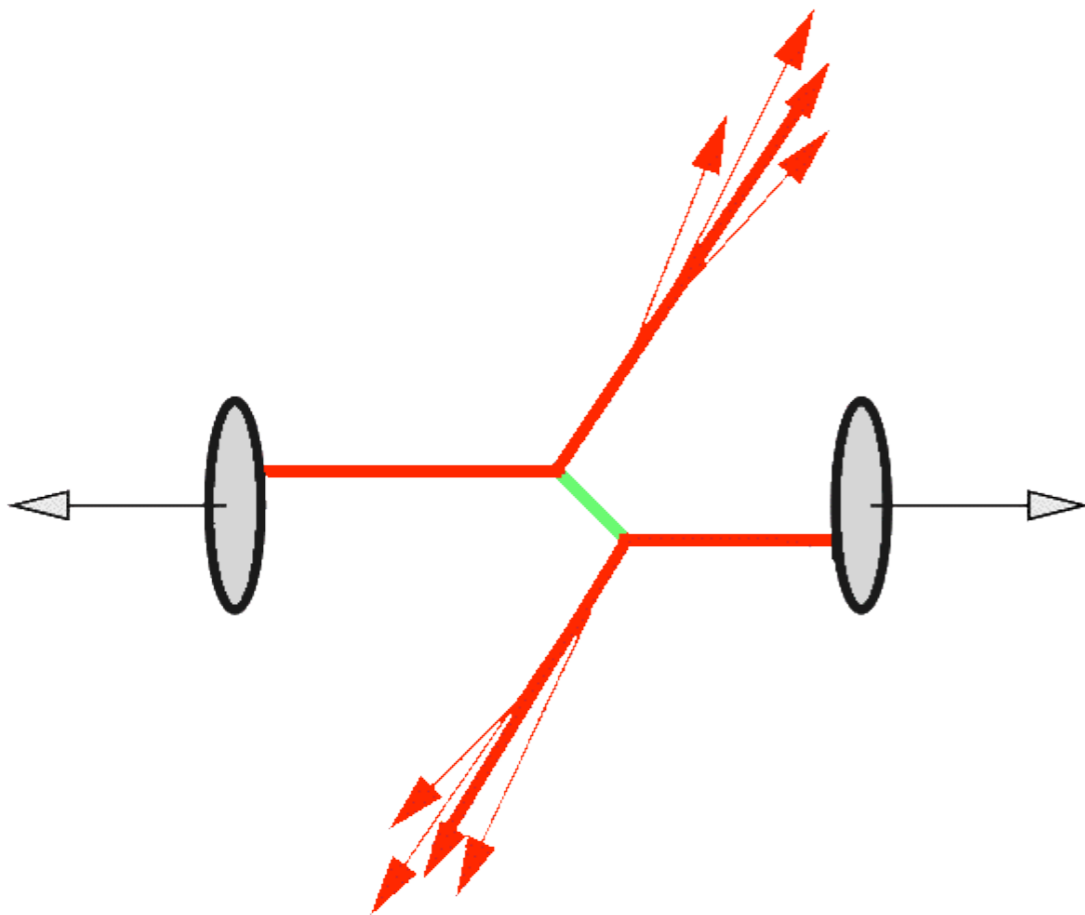
# Hard probes (2): “jet quenching”

A **fast parton** propagating through a **dense medium** will “lose” part of its energy-momentum.

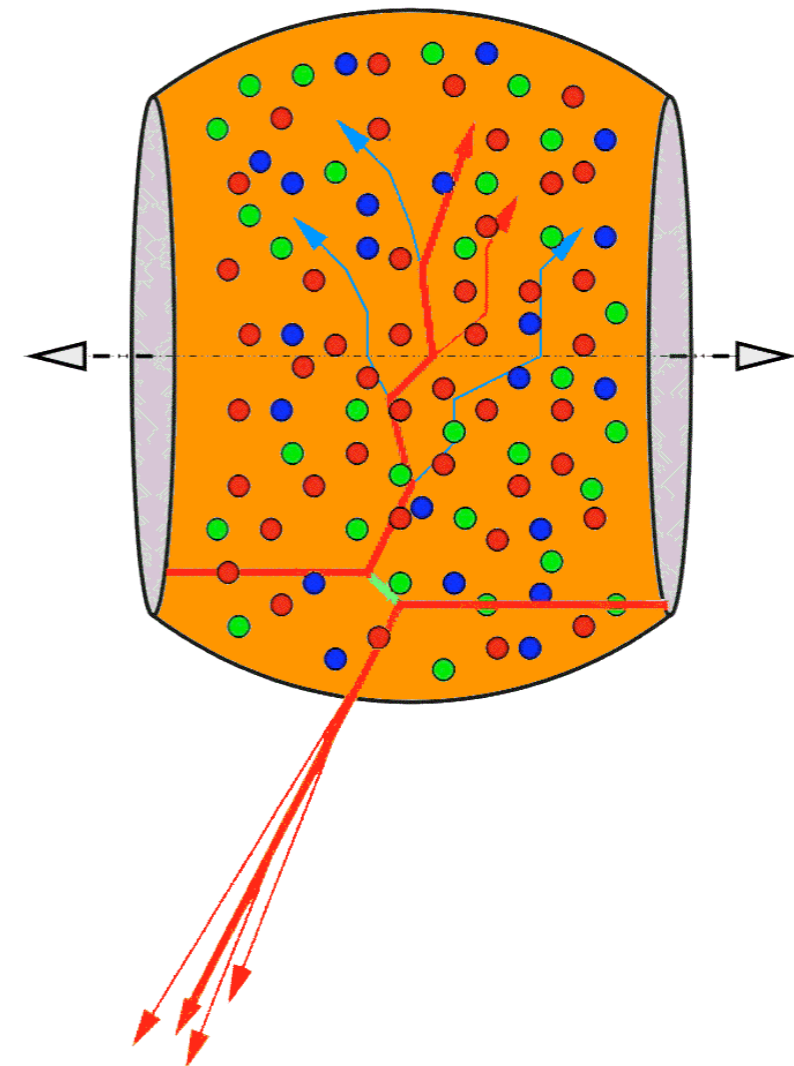
(cf. energy loss of electrically charged particles in matter: Bethe-Bloch...)

The resulting **jet** of **hadrons** (if any!) is distorted: “**quenching**”.

in vacuum



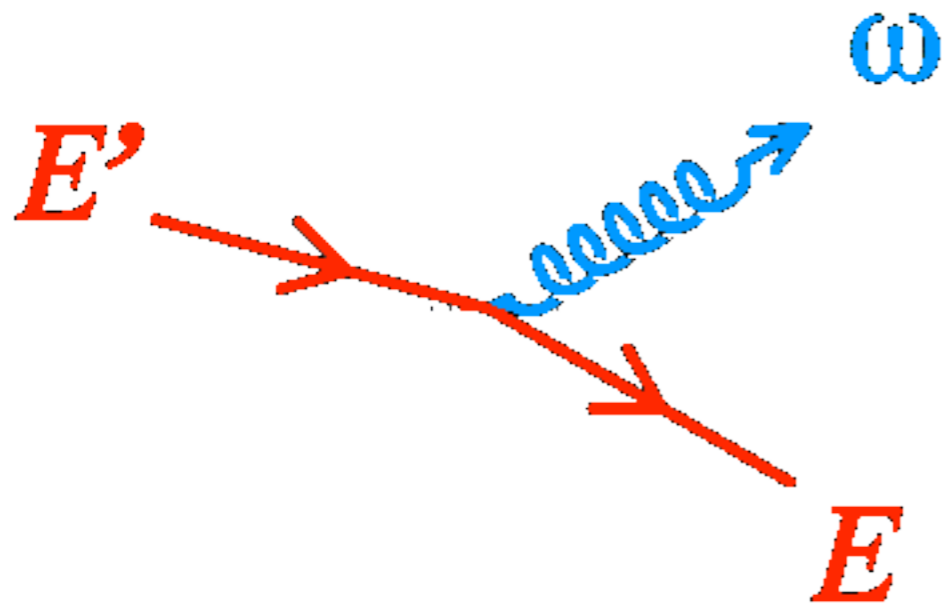
in medium



# Hard probes (2): "jet quenching"

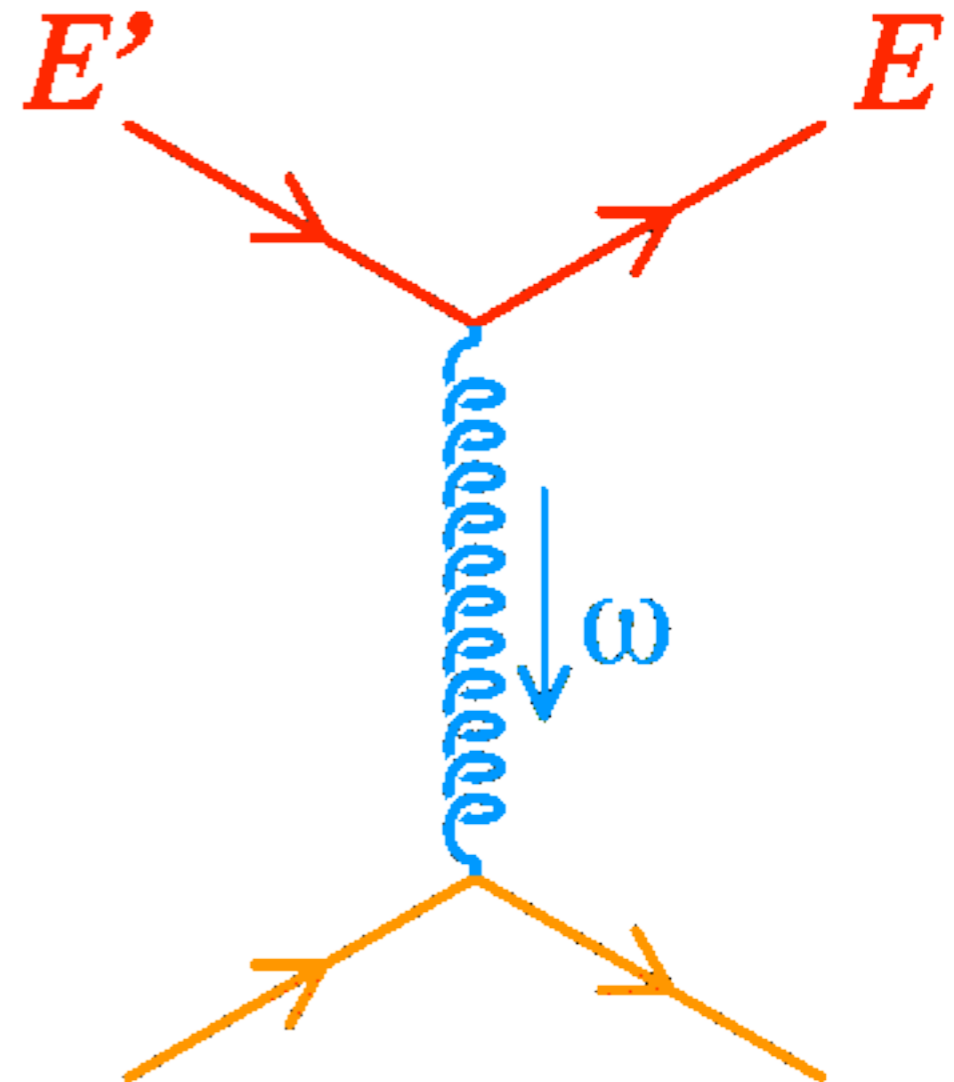
Two different processes leading to the **loss of energy** by a **fast parton**:

"radiative" process (Bremsstrahlung)



also "in vacuum" (DGLAP evolution),  
yet modified by the presence of a  
**(colored) medium**

"collisional" process



# Hard probes (2): "jet quenching"

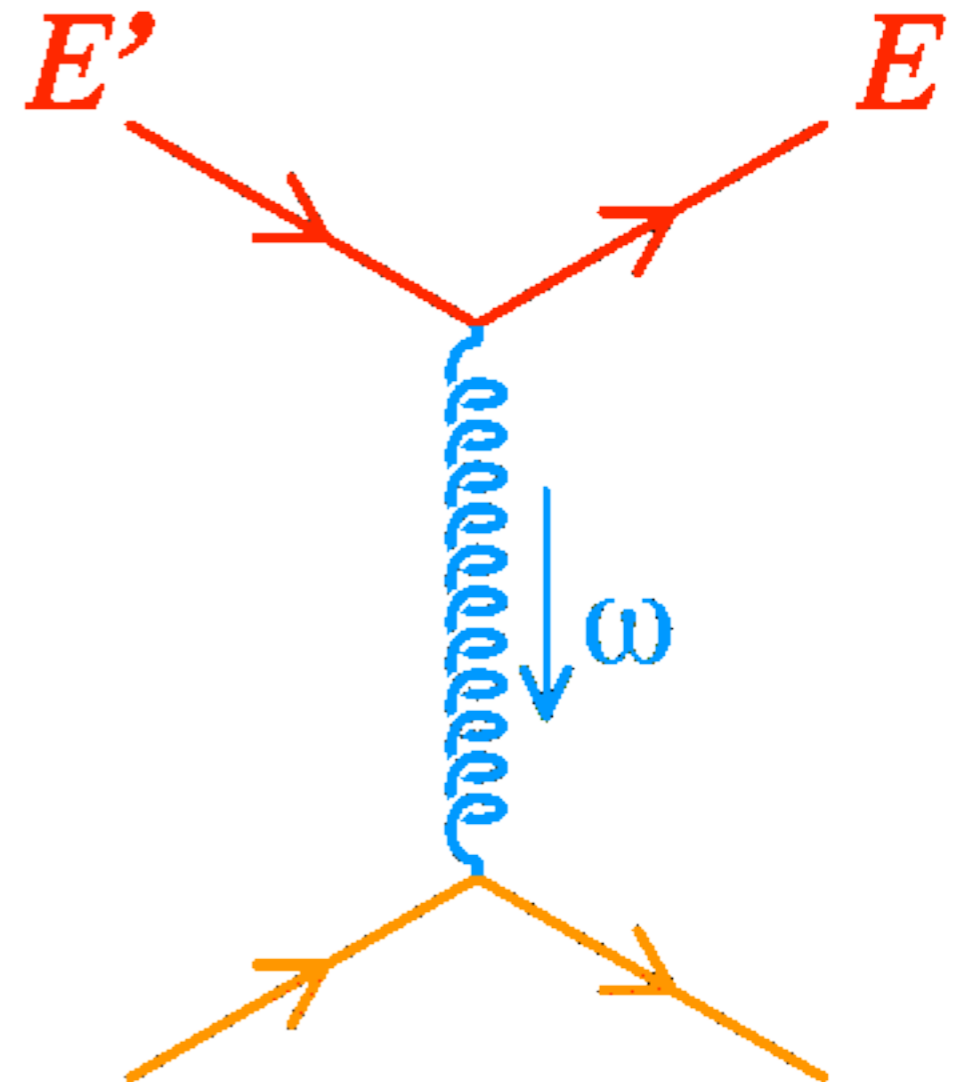
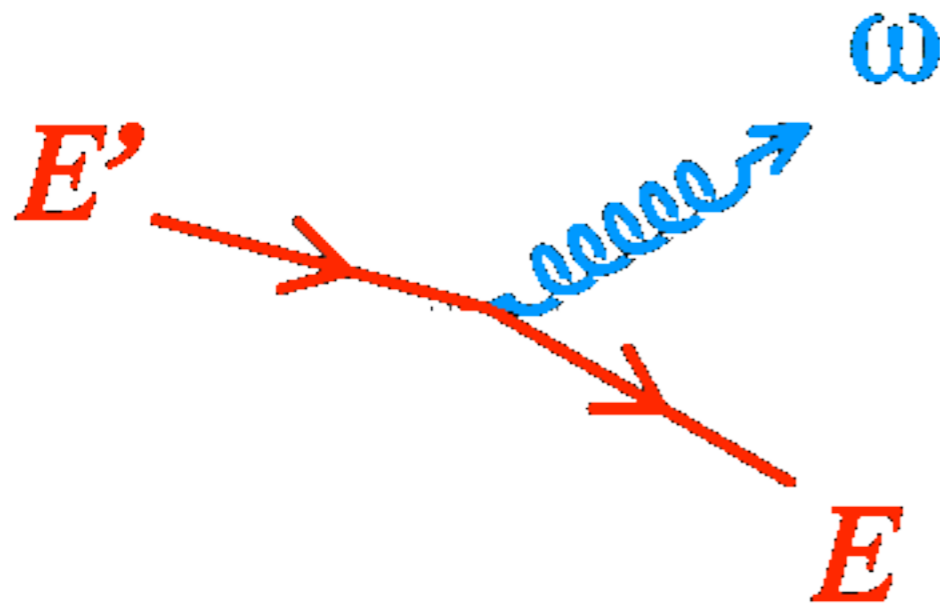
Two different processes leading to the loss of energy by a fast parton:

inelastic

elastic

"radiative" process (Bremsstrahlung)

"collisional" process



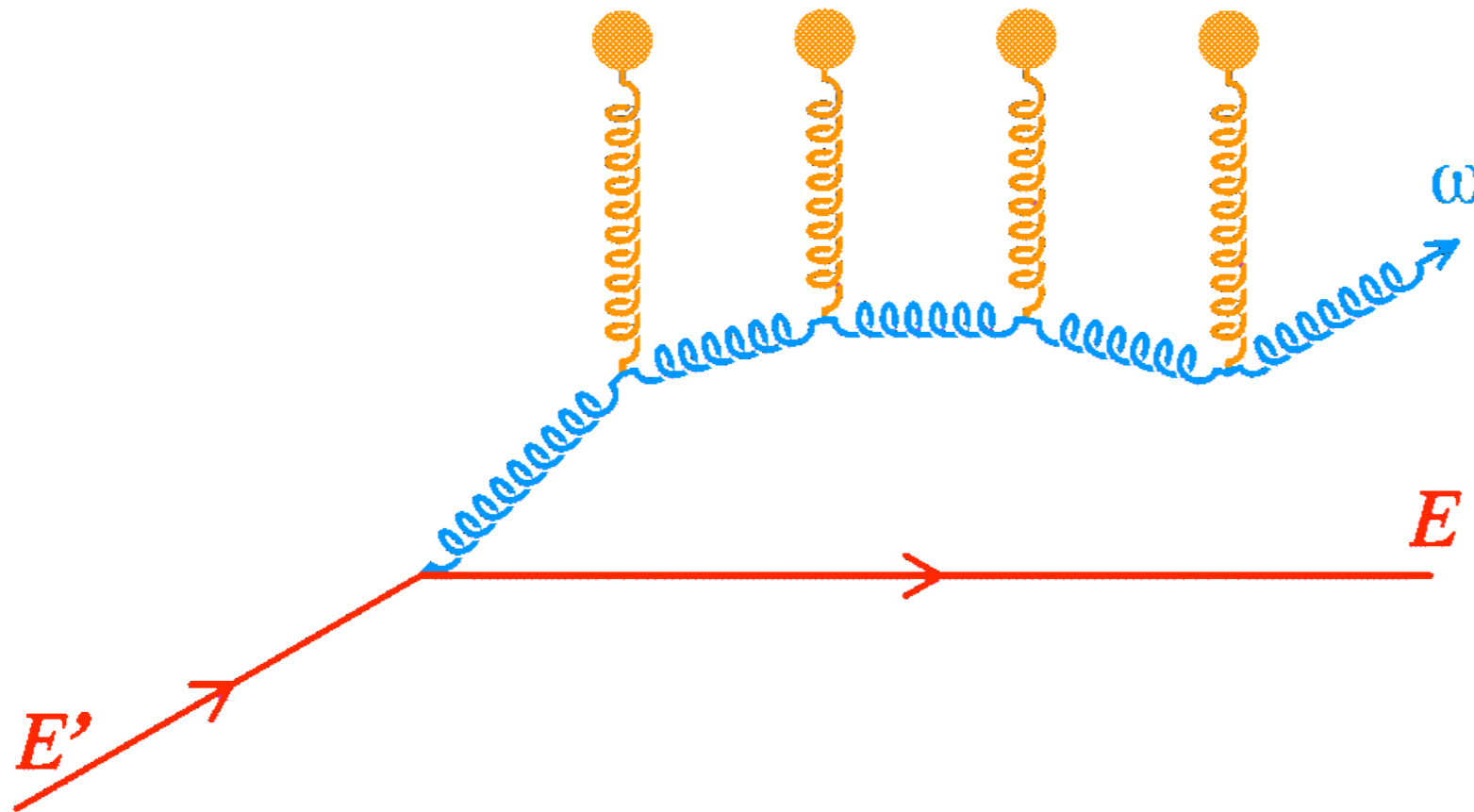
also "in vacuum" (DGLAP evolution),  
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(colored) medium

collisions!

# Hard probes (2): "jet quenching"

Landau-Pomeranchuk-Migdal effect: Multiple soft scattering limit

The propagating high- $p_T$  parton traverses a thick target.



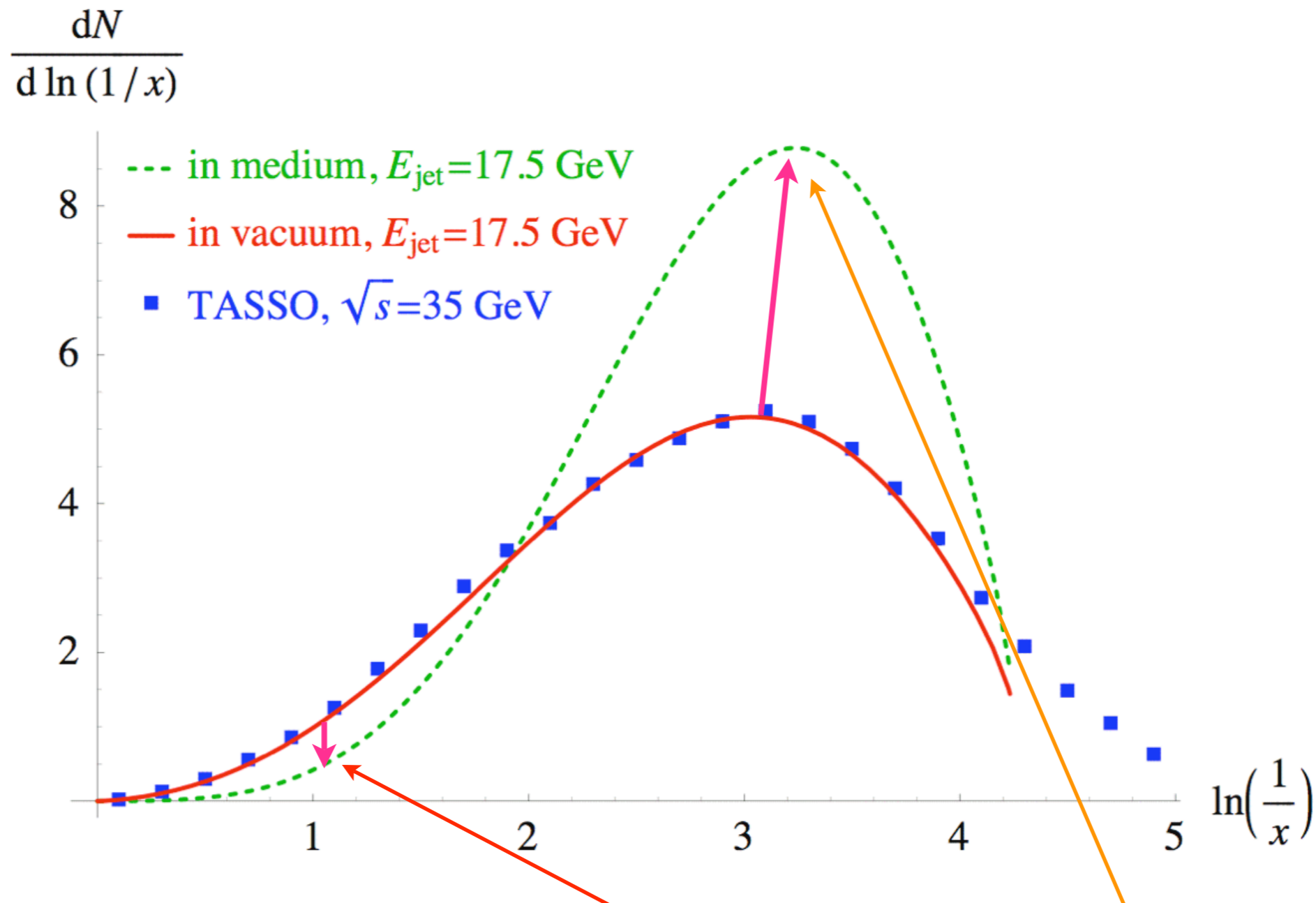
It radiates soft gluons, which scatter coherently on independent color charges in the medium, resulting in a medium-modified gluon spectrum.

👉 transport coefficient  $\hat{q}$

Baier, Dokshitzer, Mueller, Peigné, Schiff (BDMPS); Zakharov



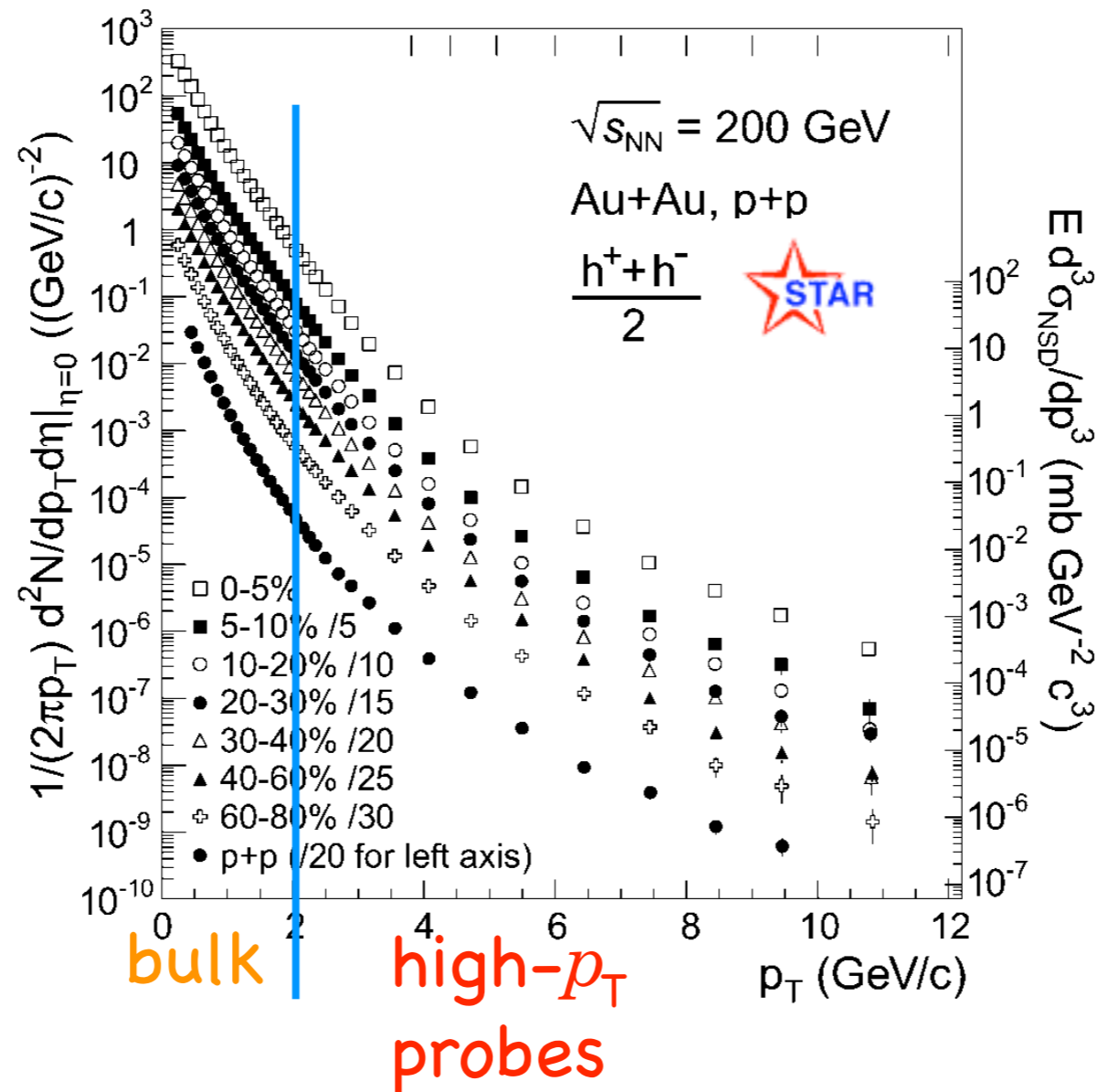
# Parton distribution inside a jet in the presence of a medium



Partons are redistributed from **high  $p_T$  (large  $x$ )** to **low  $p_T$  (small  $x$ )**

NB, U.A.Wiedemann, hep-ph/0506218

# Bulk observables vs. hard probes



The **bulk** represents at least 99% of the **hadrons**!

It should be possible to extract some information with high statistical significance.

# Heavy-ion collisions: fluid-dynamics description

- ① Creation of a dense “collection” of particles.

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👉 fireball can be described by fluid dynamics

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③ The fluid expands: density decreases,  $\lambda$  increases (system size also).

④ At some time, the mean free path is of the same order as the system size: fluid dynamics is no longer a valid description:

(kinetic) “freeze-out”

usually parameterized in terms of a temperature  $T_{f.o.}$ .

# Fluid dynamics: various types of flows

- **Thermodynamic** equilibrium?

- $Kn \gg 1$ : free-streaming limit
- $Kn \ll 1$ : **liquid** (hydro) limit

- **Viscous** or inviscid (“ideal”)?

- $Re \gg 1$ : **ideal** (non-viscous) **flow**
- $Re \lesssim 1$ : **viscous flow**

- **Compressible** or incompressible?

- $Ma \ll 1$ : **incompressible flow**
- $Ma \gtrsim 1$ : **compressible flow**

mean free path  $\lambda$

Knudsen number  $Kn \equiv \frac{\lambda}{L}$

system size  $L$

Reynolds number  $Re \equiv \frac{\varepsilon L v_{\text{fluid}}}{\eta}$

$\eta \sim \varepsilon \lambda c_s$

shear viscosity

Mach number  $Ma \equiv \frac{v_{\text{fluid}}}{c_s}$

# Fluid dynamics: various types of flows

Three dimensionless numbers:

$$\text{Kn} \equiv \frac{\lambda}{L}, \quad \text{Re} \equiv \frac{\varepsilon L v_{\text{fluid}}}{\eta}, \quad \text{Ma} \equiv \frac{v_{\text{fluid}}}{c_s}$$

An important relation:

$$\text{Kn} \times \text{Re} = \frac{\varepsilon \lambda v_{\text{fluid}}}{\eta} \sim \frac{v_{\text{fluid}}}{c_s} = \text{Ma}$$

In a heavy-ion collision, the **created matter** expands into the vacuum

$\Rightarrow$  **compressible flow**

**compressible liquids** are **ideal**  $\Leftrightarrow$  **viscosity**  $\equiv$  departure from equilibrium

👉 To access the **shear viscosity**, try to estimate **Kn** ( $\Leftrightarrow$  mean number of collisions per particle): find an **observable** that depends on the latter.



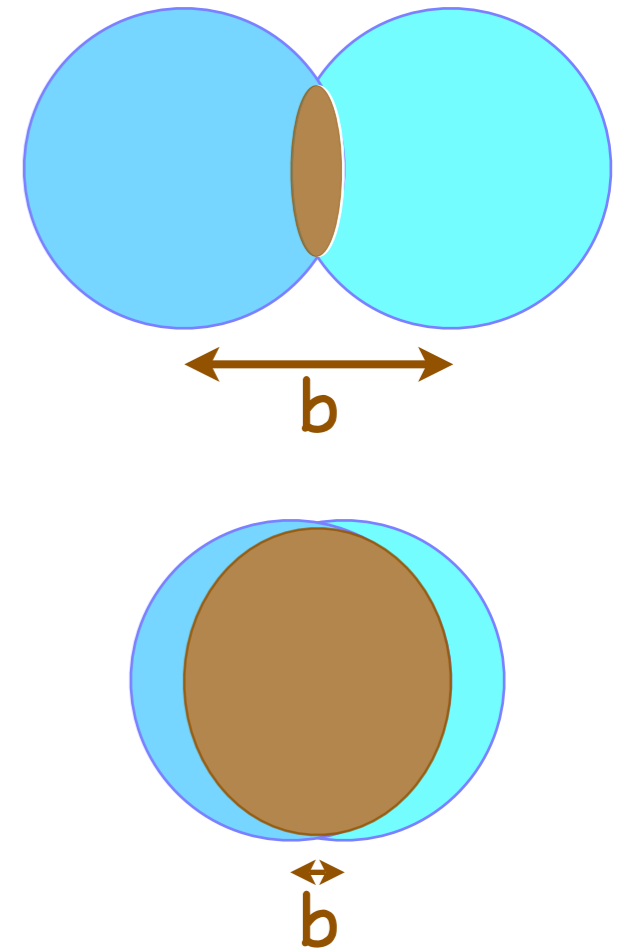
# Heavy-ion collisions: geometry

Heavy nuclei have a finite radius!

👉 In a collision the **impact parameter** plays a role:

🌐 the nuclei might barely graze each other (**large impact parameter**, “peripheral” collisions)

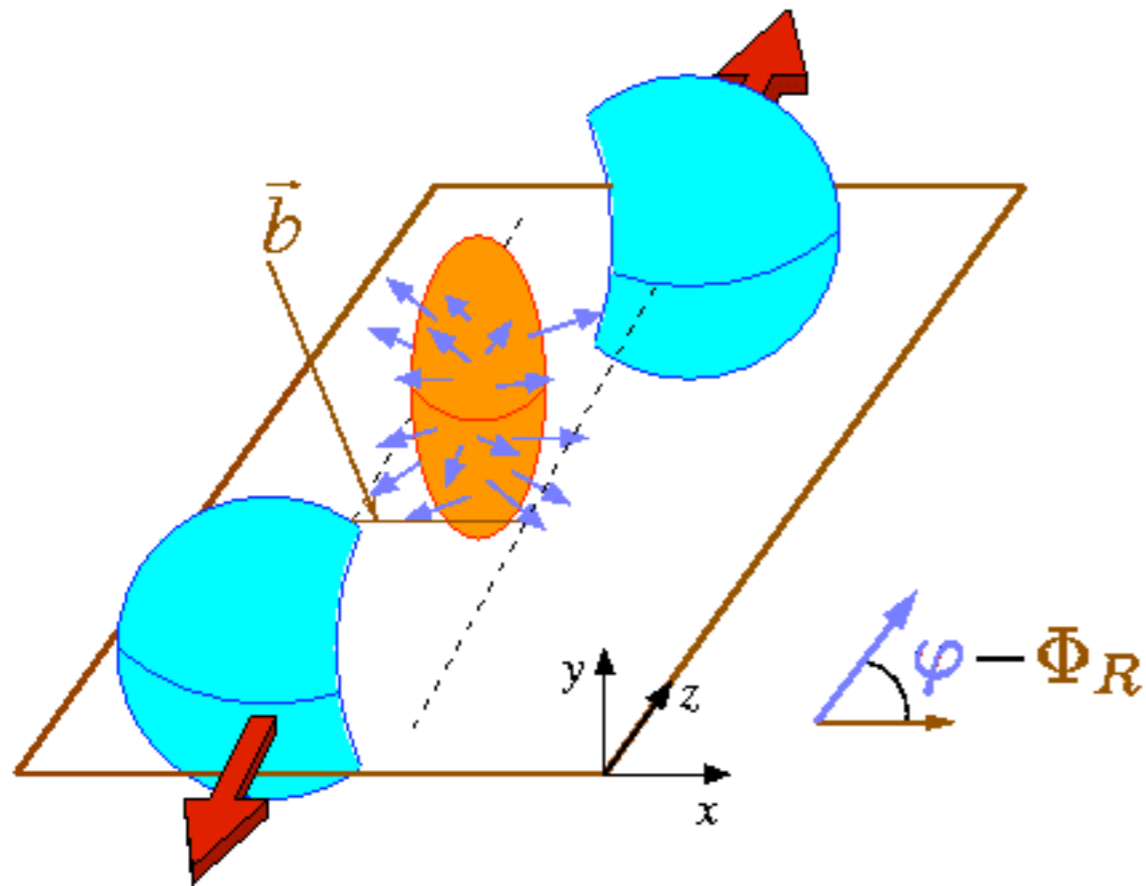
🌐 or the collision might be almost head-on (**small impact parameter**, “central” collision)



The (**almond-shaped**) **overlap regions** of the nuclei are different in either case (**size, eccentricity...**): possible control parameter(s) for the **mean number of collisions  $K_n^{-1}$** .

# Anisotropic (collective) flow

Consider a **non-central** collision:

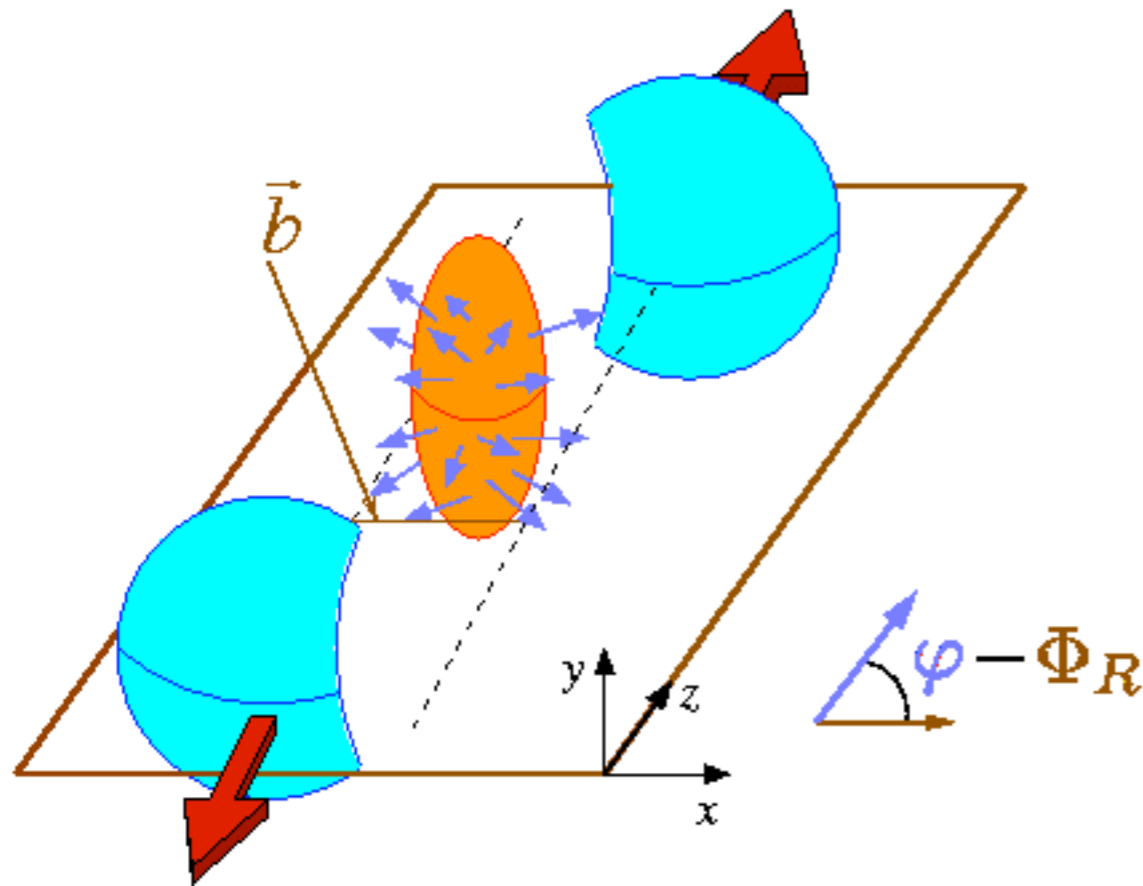


**anisotropy** of the **source** (in the plane transverse to the beam)

$\Rightarrow$  **anisotropic** pressure gradients  
(larger along the **impact parameter**)

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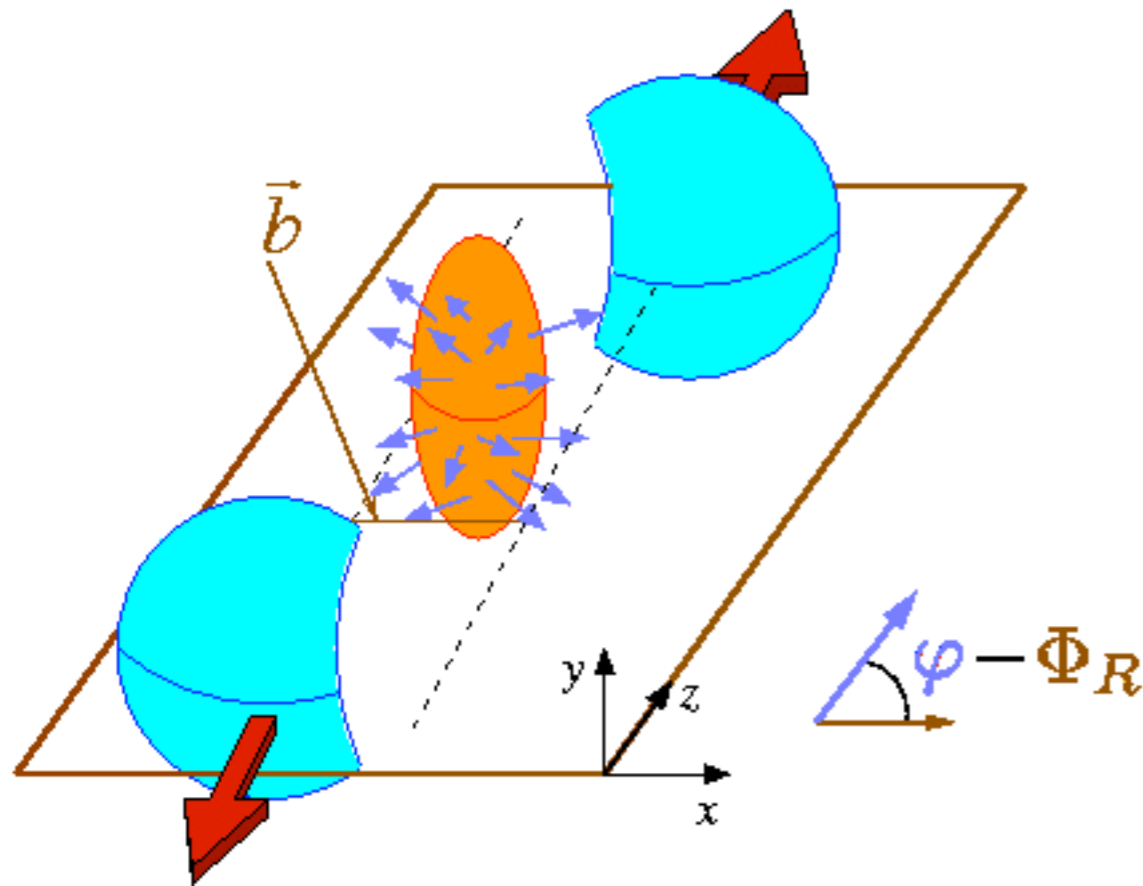
⇒ **anisotropic pressure gradients** (larger along the **impact parameter**)  
 push

⇒ **anisotropic fluid velocities**  
**anisotropic emission of particles:**  
 “**anisotropic collective flow**”

$$E \frac{dN}{d^3\mathbf{p}} \propto \frac{dN}{p_T dp_T dy} [1 + 2v_1 \cos(\varphi - \Phi_R) + 2v_2 \cos 2(\varphi - \Phi_R) + \dots]$$

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More **particles** along the **impact parameter** ( $\varphi - \Phi_R = 0$  or  $180^\circ$ ) than perpendicular to it → “**elliptic flow**”  $v_2 \equiv \langle \cos 2(\varphi - \Phi_R) \rangle > 0$ .

average over **particles** →

# Anisotropic (collective) flow

 Despite the terminology, “flow” does not imply fluid dynamics.

An exact computation of the dependence of  $v_2, v_4$  on the number  $\text{Kn}^{-1}$  of collisions undergone by particles requires a microscopic transport model, yet one can guess the general tendency.

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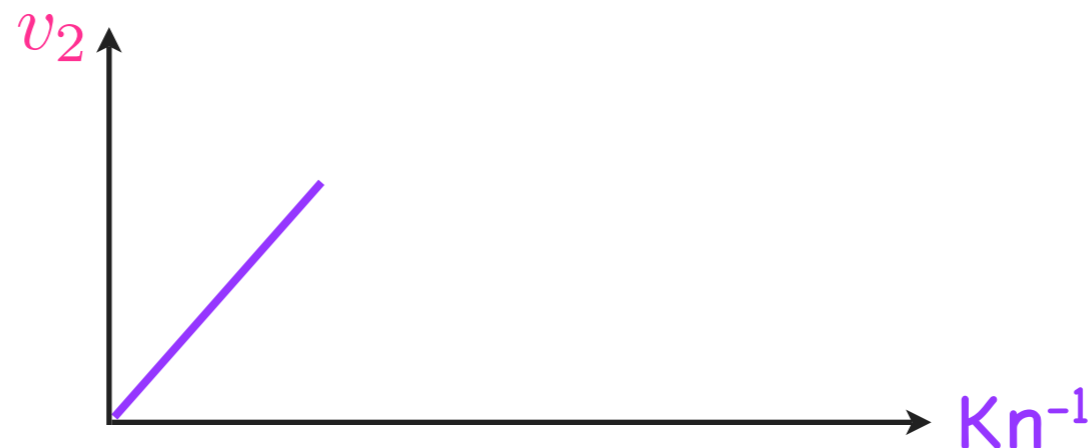


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- The more collisions, the larger the flow.

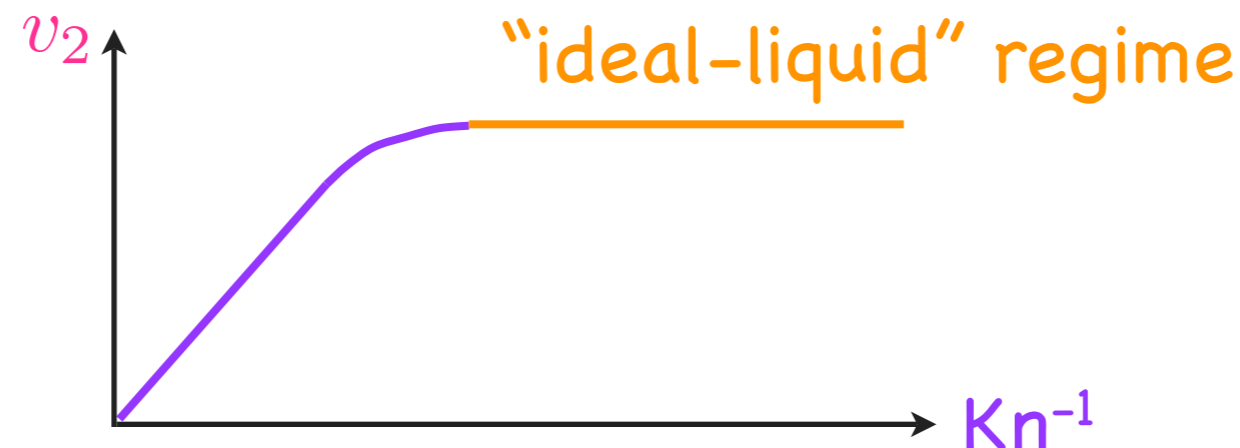


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- In the absence of rescatterings (“gas”), no flow develops.
- The more collisions, the larger the flow.
- For a given number of collisions, the system thermalizes: further collisions no longer increase  $v_2$ .



R.S.Bhalerao, J.-P.Blaizot, NB, J.-Y.Ollitrault, PLB 627 (2005) 49



# Anisotropic (collective) flow

Possible **experimental** control knobs for the **mean number of collisions per particle  $K_n^{-1}$** :



- **centrality** of the collisions
- **size** of the colliding nuclei
- center-of-mass energy of the collisions
- **transverse momentum / rapidity** of the **emitted particles**

# Anisotropic (collective) flow

Possible **experimental** control knobs for the **mean number of collisions per particle**  $Kn^{-1}$ :

- **centrality** of the collisions
- **size** of the colliding nuclei
- center-of-mass energy of the collisions
- **transverse momentum / rapidity** of the **emitted particles**

However, the “absolute size” of the **signal** (the **hydro**-regime value) can also depend on these handles:

- **centrality** of the collisions   $v_2^{\text{hydro}} = \text{const} \times \epsilon$  (**eccentricity**), where the constant depends on  $c_s$
- the center-of-mass energy of the collisions influences the initial conditions in the **overlap region**  entropy density, **eccentricity**...

# Probes of high-energy heavy-ion collisions

## Physical aspects

- Theoretical hints (in particular from lattice QCD) that the relevant degrees of freedom for the description of bulk nuclear matter may change when the temperature increases.
- Time evolution of an ultra-relativistic heavy-ion collision: several stages, all of them contributing to the signal in the detectors.
- Hard probes: quarkonium suppression, jet quenching...
- Collective probes: anisotropic flow...
- Many omitted interesting topics!