

Anisotropic flow: lessons from RHIC and perspectives for LHC

Nicolas BORGHINI

Universität Bielefeld

Anisotropic flow at RHIC and prospects for LHC

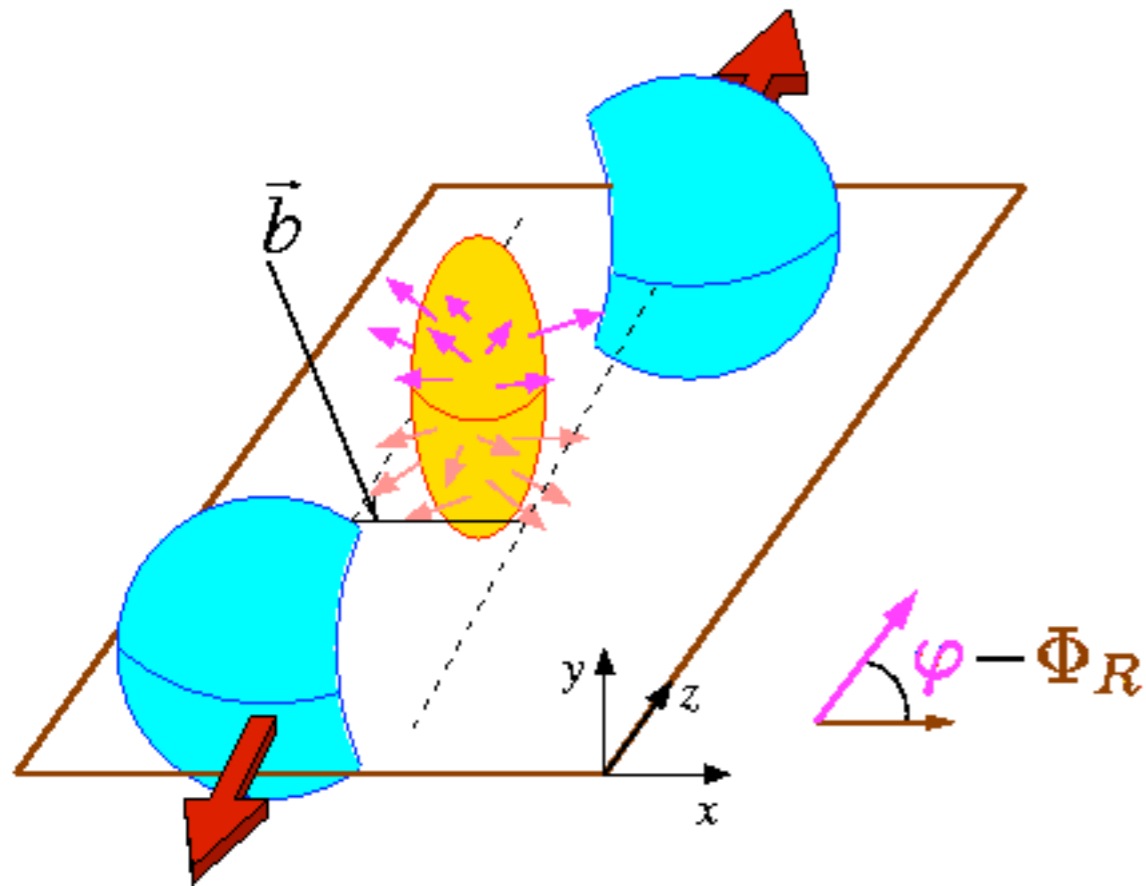
- **Anisotropic flow** at RHIC
 - An **experimental** success story
 - A wealth of **data**
 - As of end of November 2005, 13 PRL & 4 PRC
 - Theoretical challenges
 - Conflicting interpretations of the **data**:
hydrodynamic expansion vs. out-of-equilibrium scenario
- **Anisotropic flow** at LHC
 - Very few theoretical predictions...
 - ... yet measuring **flow** with ALICE should be “easy”

Anisotropic flow at RHIC and prospects for LHC

- Anisotropic flow at RHIC
 - An experimental success story
 - A wealth of data with novel directions
 - As of February 1st, 2007 , 15 PRL & 5 PRC
+ 5 preprints
 - Theoretical challenges
 - Conflicting interpretations of the data:
hydrodynamic expansion vs. out-of-equilibrium scenario
- Anisotropic flow at LHC
 - Very few theoretical predictions... Nihil novum sub sole
 - ... but we can build on RHIC results!

Anisotropic (collective) flow

Consider a **non-central** collision:

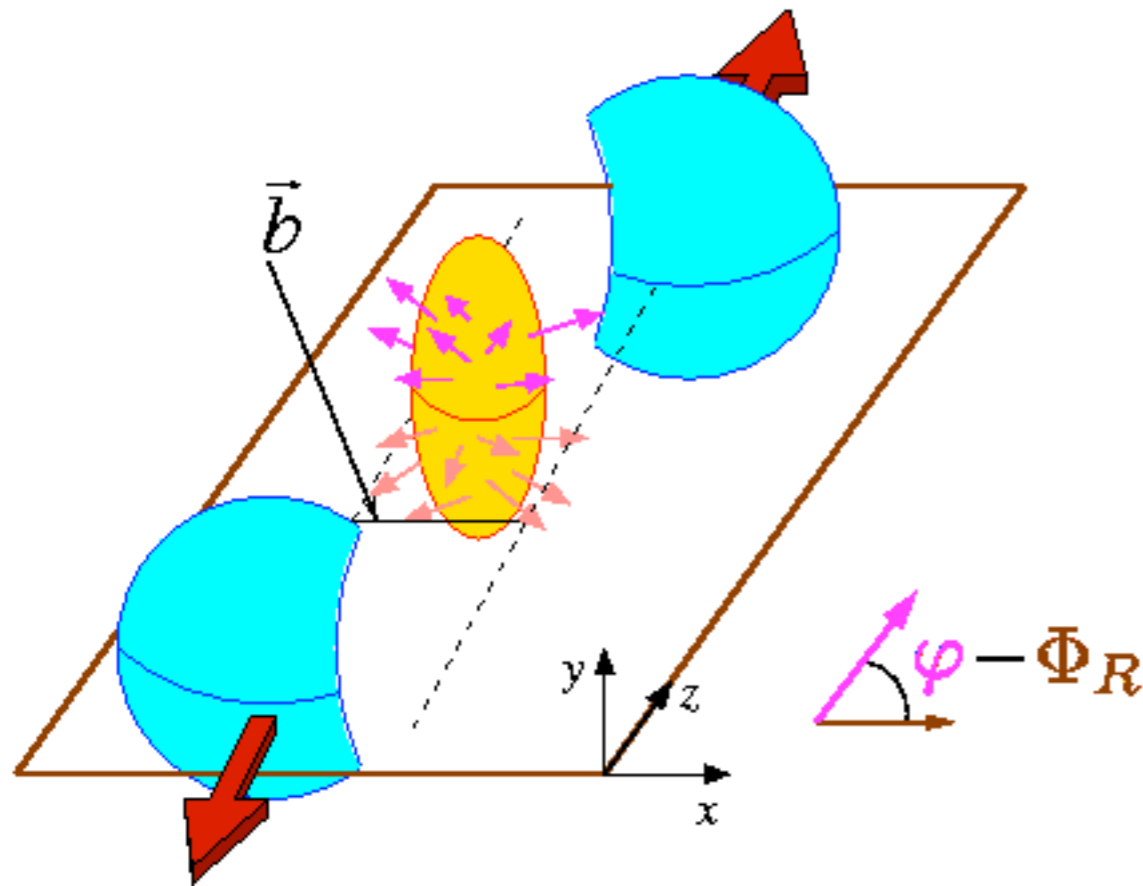


anisotropy of the **source** (in the plane transverse to the beam)

\Rightarrow **anisotropic** pressure gradients
(larger along the **impact parameter**)

Anisotropic (collective) flow

Consider a **non-central** collision:



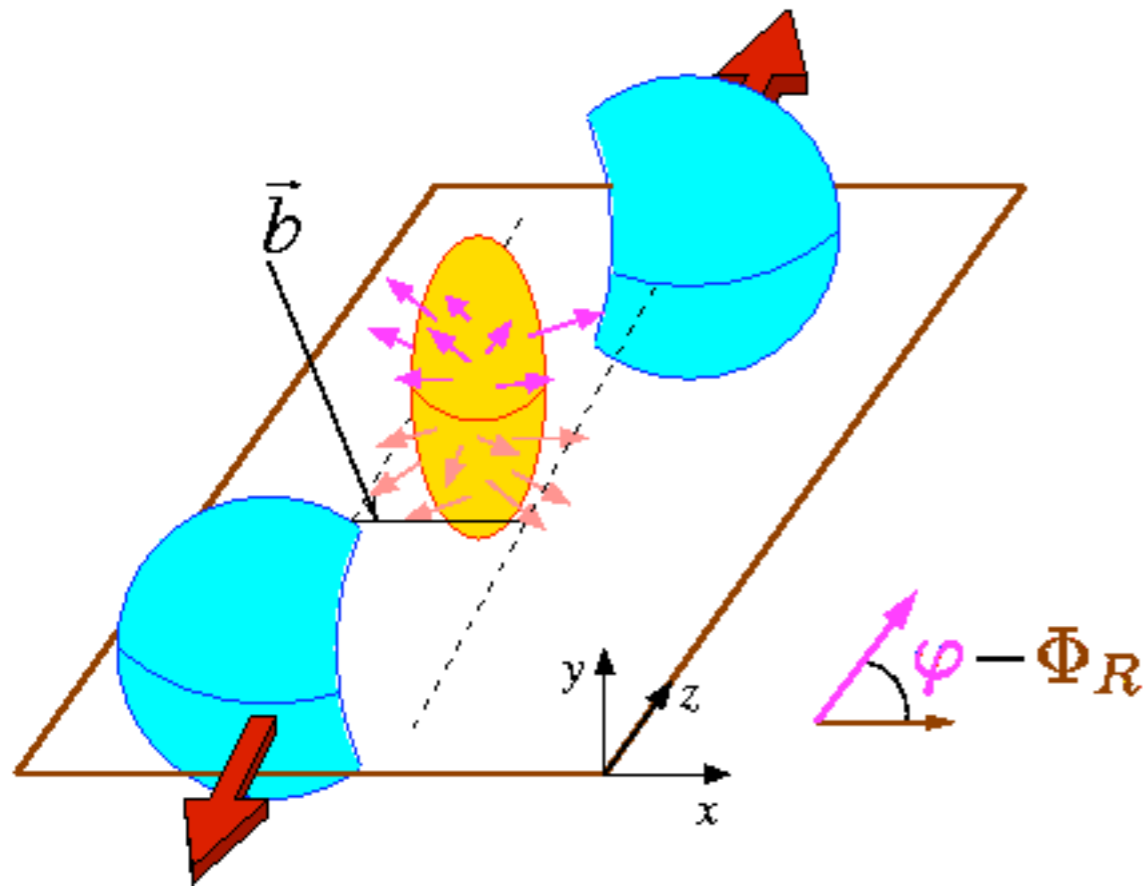
anisotropy of the **source** (in the plane transverse to the beam)

⇒ **anisotropic** pressure gradients
(larger along the **impact parameter**)
push

⇒ **anisotropic** **fluid** velocities
anisotropic emission of particles:
“**anisotropic** collective flow”

Anisotropic (collective) flow

Consider a **non-central** collision:



anisotropy of the **source** (in the plane transverse to the beam)

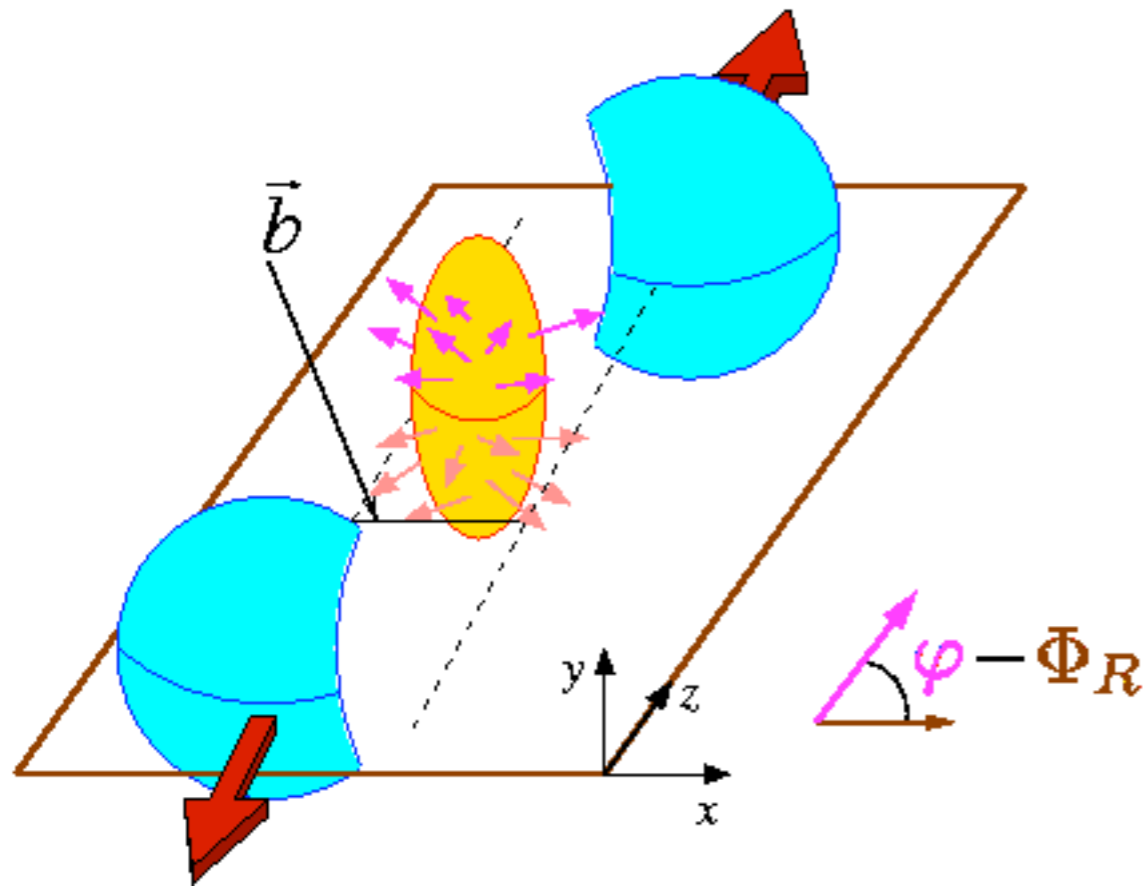
⇒ **anisotropic pressure gradients** (larger along the **impact parameter**)
push

⇒ **anisotropic fluid velocities**
anisotropic emission of particles:
 “**anisotropic collective flow**”

$$E \frac{dN}{d^3\mathbf{p}} \propto \frac{dN}{p_T dp_T dy} [1 + 2v_1 \cos(\varphi - \Phi_R) + 2v_2 \cos 2(\varphi - \Phi_R) + \dots]$$

Anisotropic (collective) flow

Consider a **non-central** collision:



anisotropy of the **source** (in the plane transverse to the beam)

⇒ **anisotropic pressure gradients** (larger along the **impact parameter**)
 push

⇒ **anisotropic fluid velocities**
anisotropic emission of particles:
 “**anisotropic collective flow**”

$$E \frac{dN}{d^3\mathbf{p}} \propto \frac{dN}{p_T dp_T dy} [1 + 2v_1 \cos(\varphi - \Phi_R) + 2v_2 \cos 2(\varphi - \Phi_R) + \dots]$$

More particles along the **impact parameter** ($\varphi - \Phi_R = 0$ or 180°) than perpendicular to it → “**elliptic flow**” $v_2 \equiv \langle \cos 2(\varphi - \Phi_R) \rangle > 0$.

average over **particles** →

Anisotropic (collective) flow



“Flow”, v_n do not imply fluid dynamics...

(Transverse) anisotropy of the source in a non-central collision

⇒ the amount of matter seen by a high- p_T particle traversing the medium is anisotropic (shorter path along the impact parameter)

⇒ anisotropic jet quenching:
anisotropic distribution of high- p_T particles

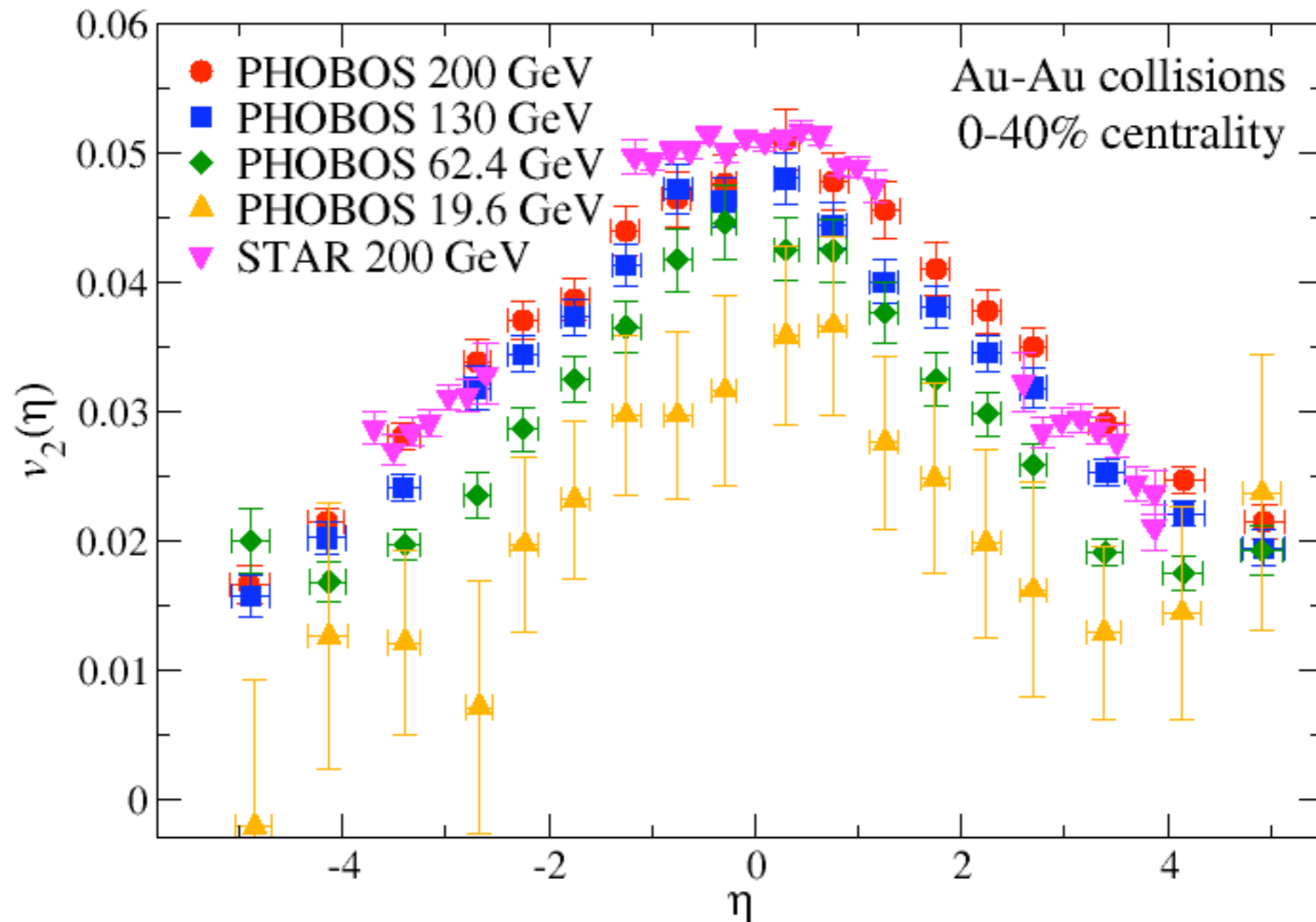
which is best characterized in terms of Fourier harmonics v_n (detector independent; more robust in Monte-Carlo computations)

Anisotropic flow:

what have we learned from RHIC?

Elliptic flow v_2 varies with (pseudo)rapidity

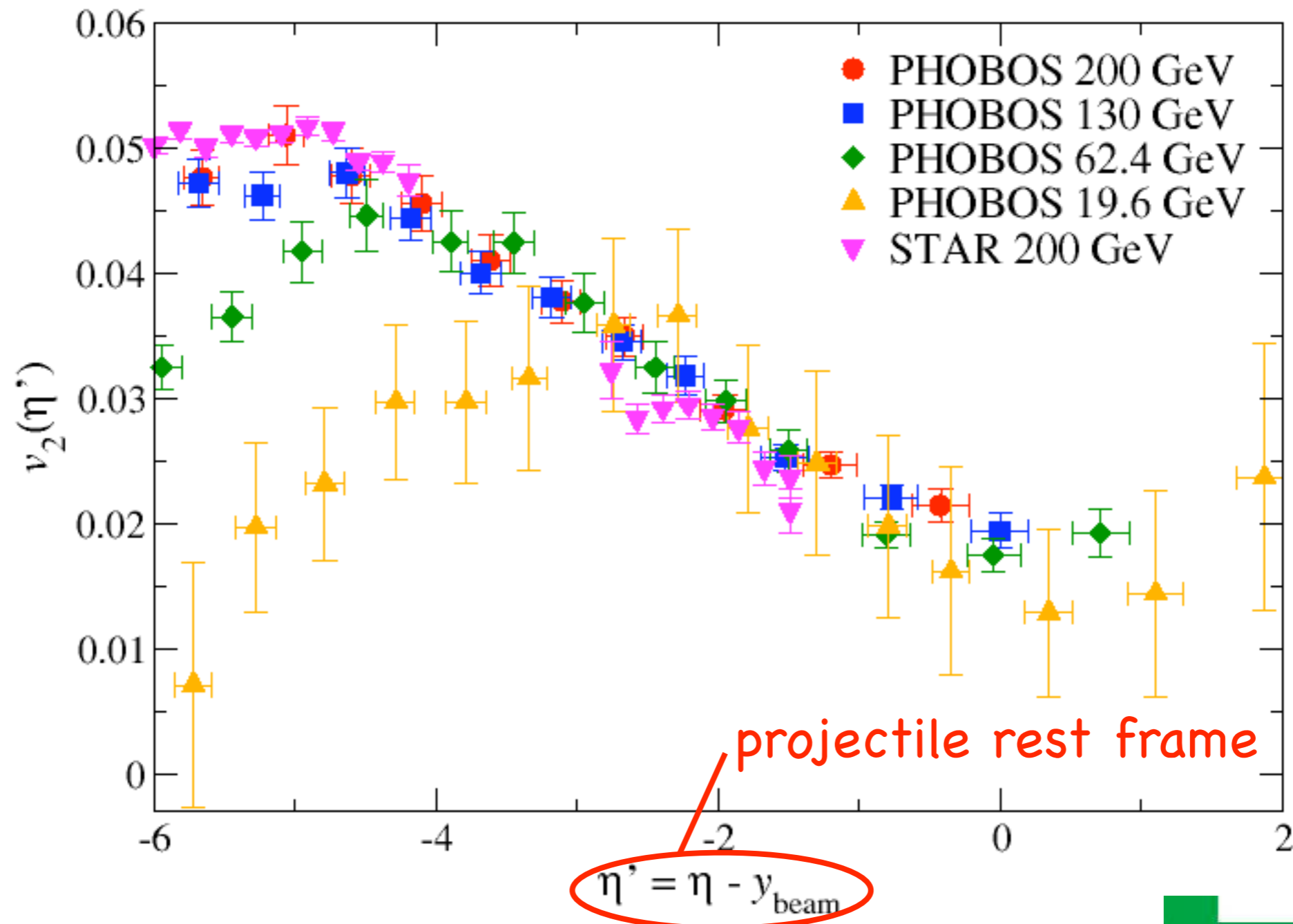
(note: $v_2(\eta) \simeq v_2(y)$)



Anisotropic flow:

what have we learned from RHIC?

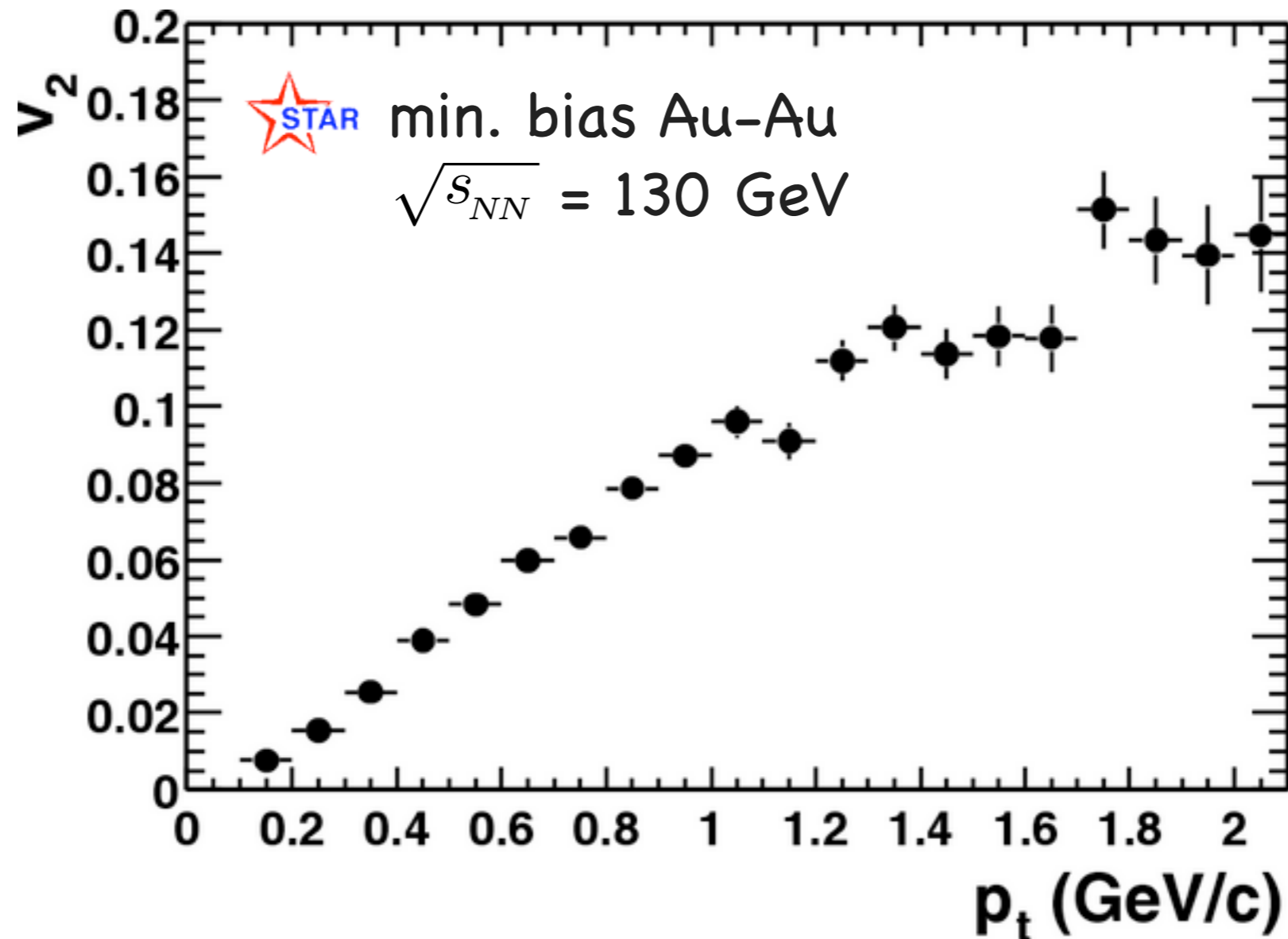
Elliptic flow v_2 varies with (pseudo)rapidity \rightarrow "limiting fragmentation"



Anisotropic flow:

what have we learned from RHIC?

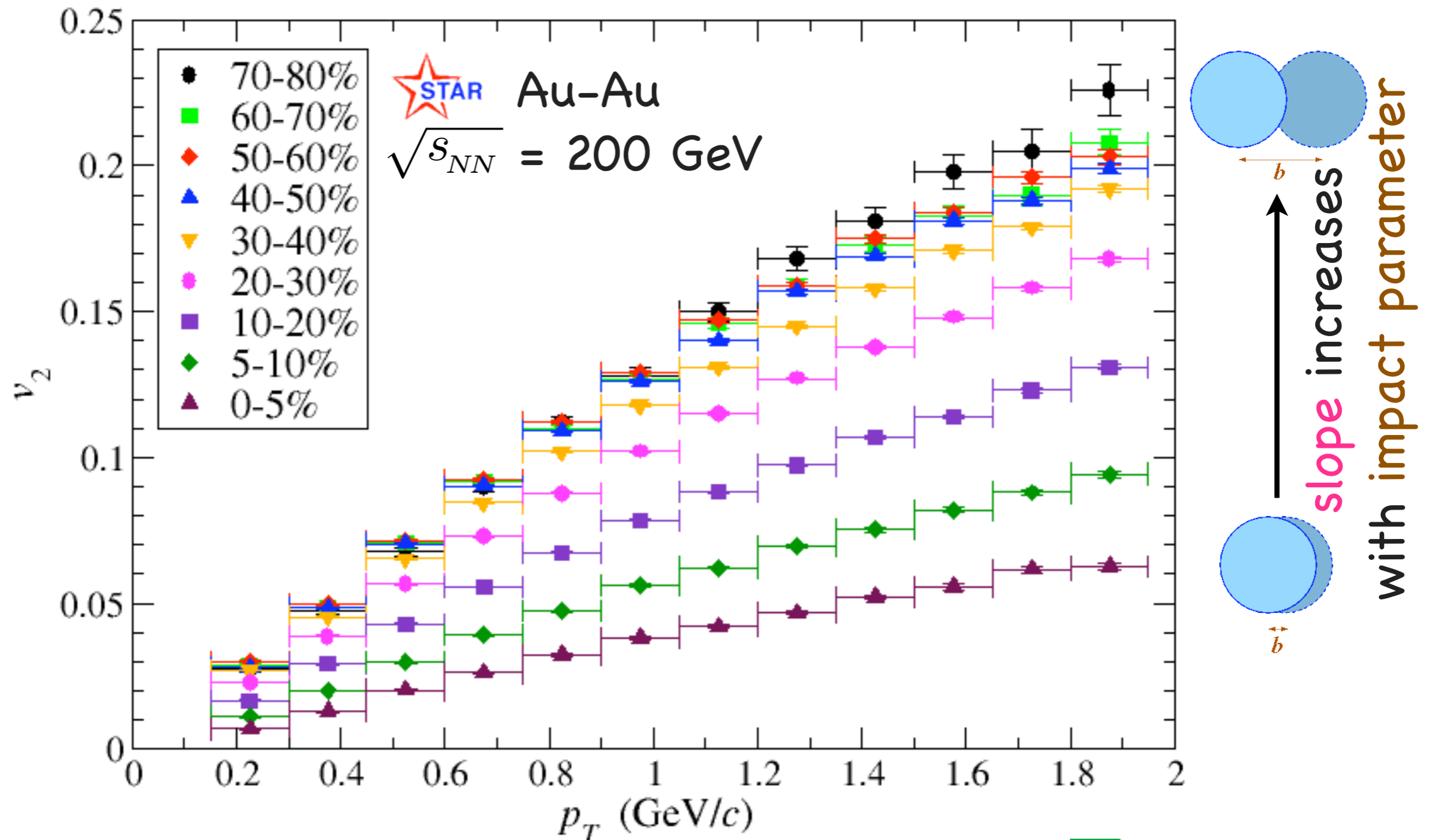
The v_2 of charged hadrons grows linearly with transverse momentum



Anisotropic flow:

what have we learned from RHIC?

The v_2 of charged hadrons grows linearly with transverse momentum

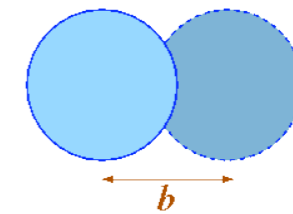
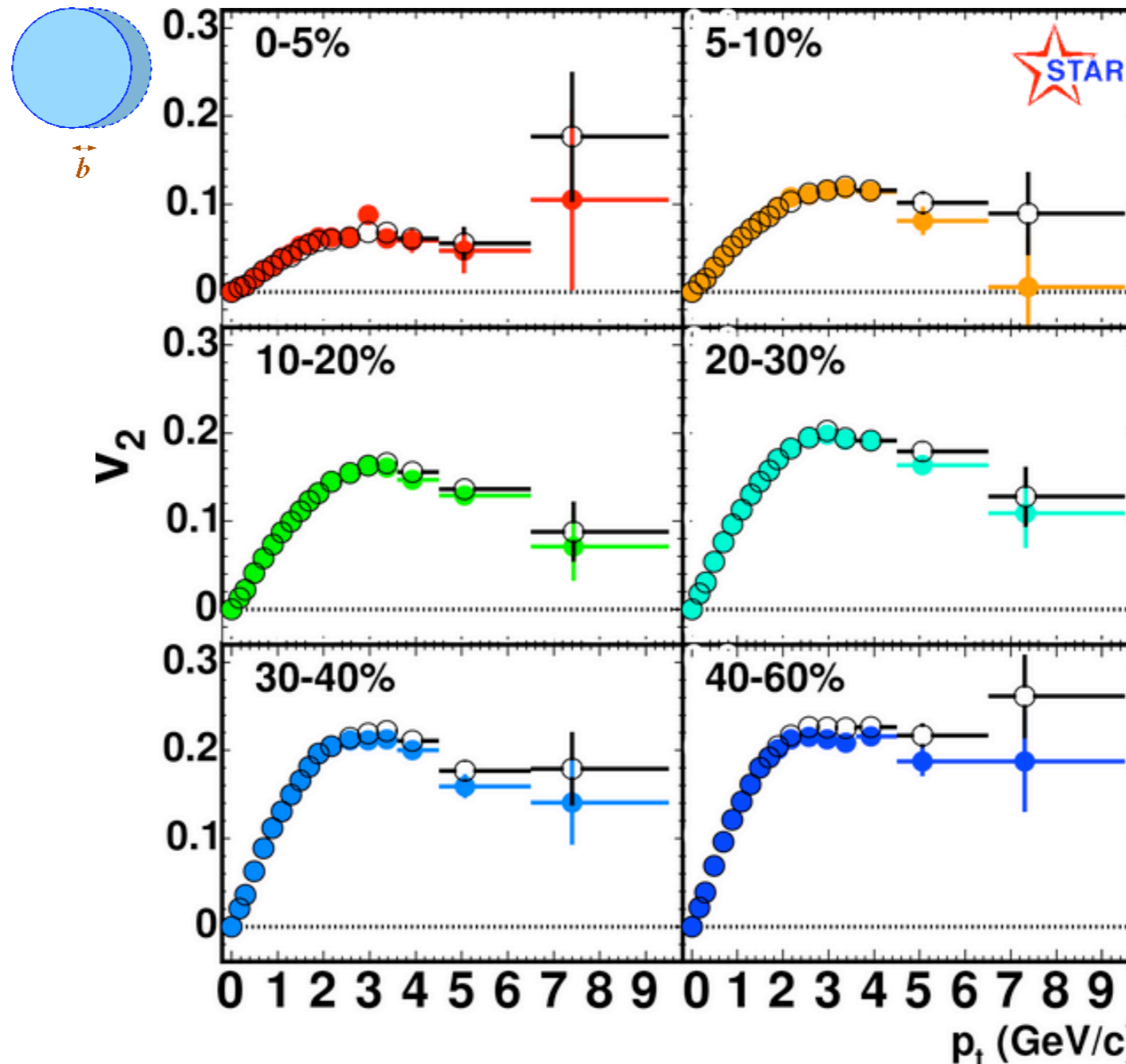


Anisotropic flow:

what have we learned from RHIC?

The v_2 of charged hadrons grows linearly with p_T , then saturates

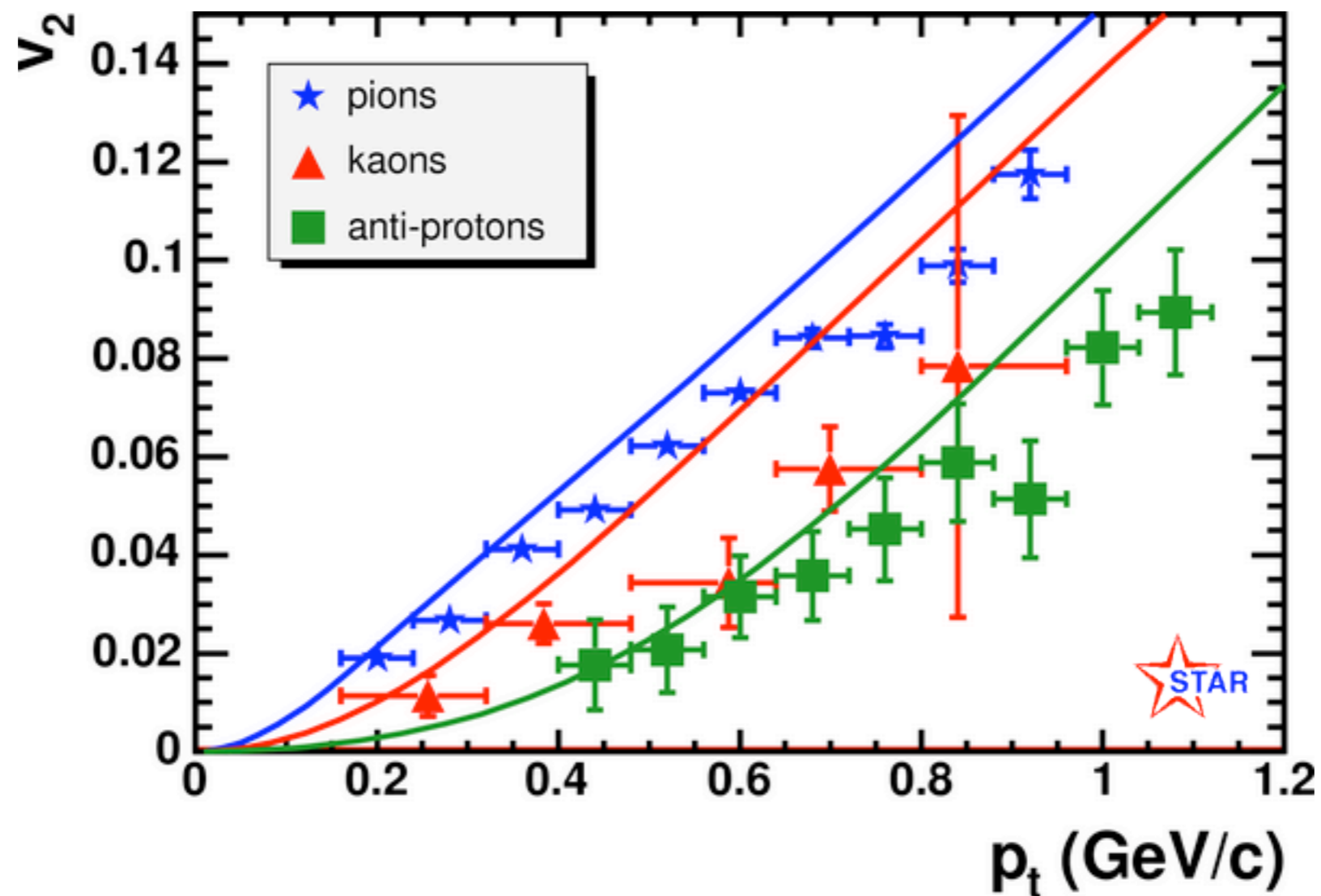
...and drops?



Anisotropic flow:

what have we learned from RHIC?

The $v_2(p_T)$ of identified hadrons show mass ordering

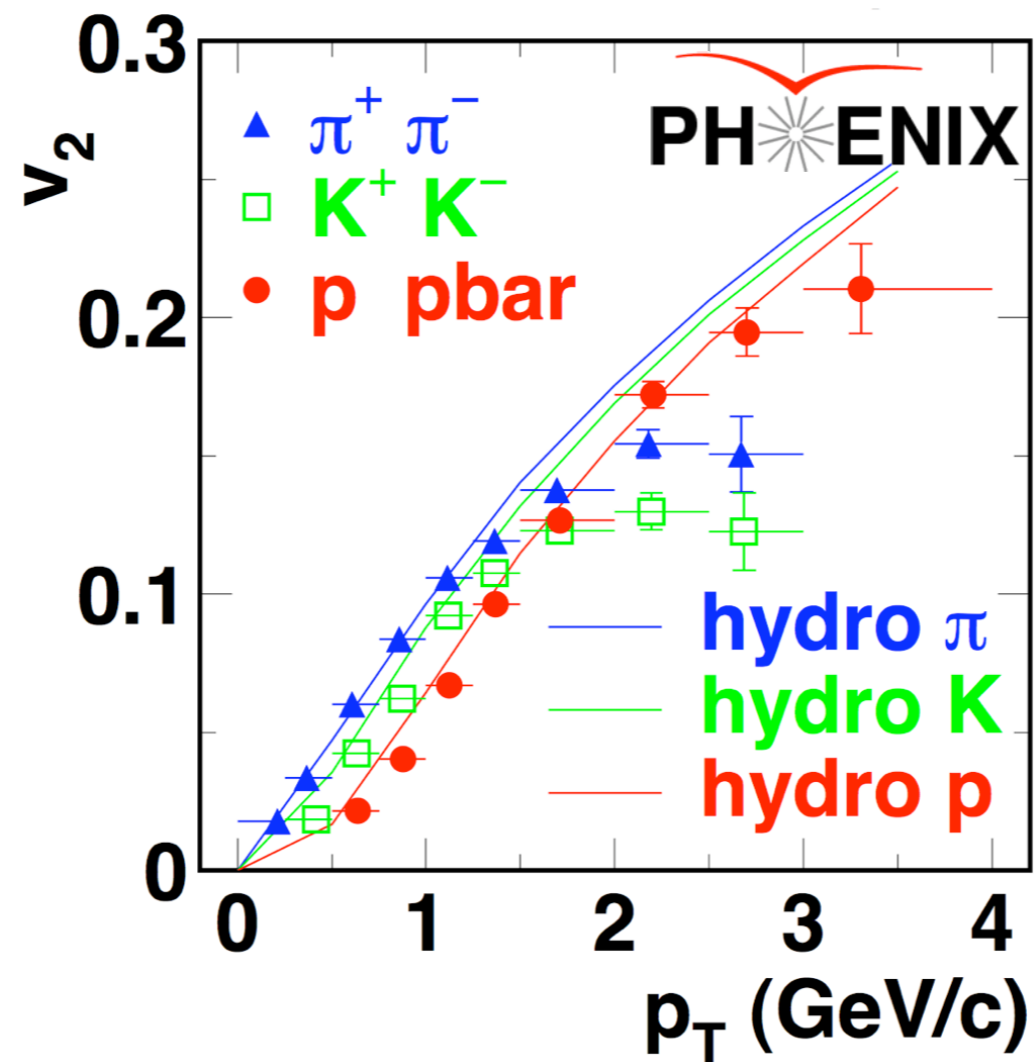


At a given transverse momentum, heavier hadrons have a smaller v_2

Anisotropic flow:

what have we learned from RHIC?

The $v_2(p_T)$ of identified hadrons show **mass ordering** below 1.5 GeV/c

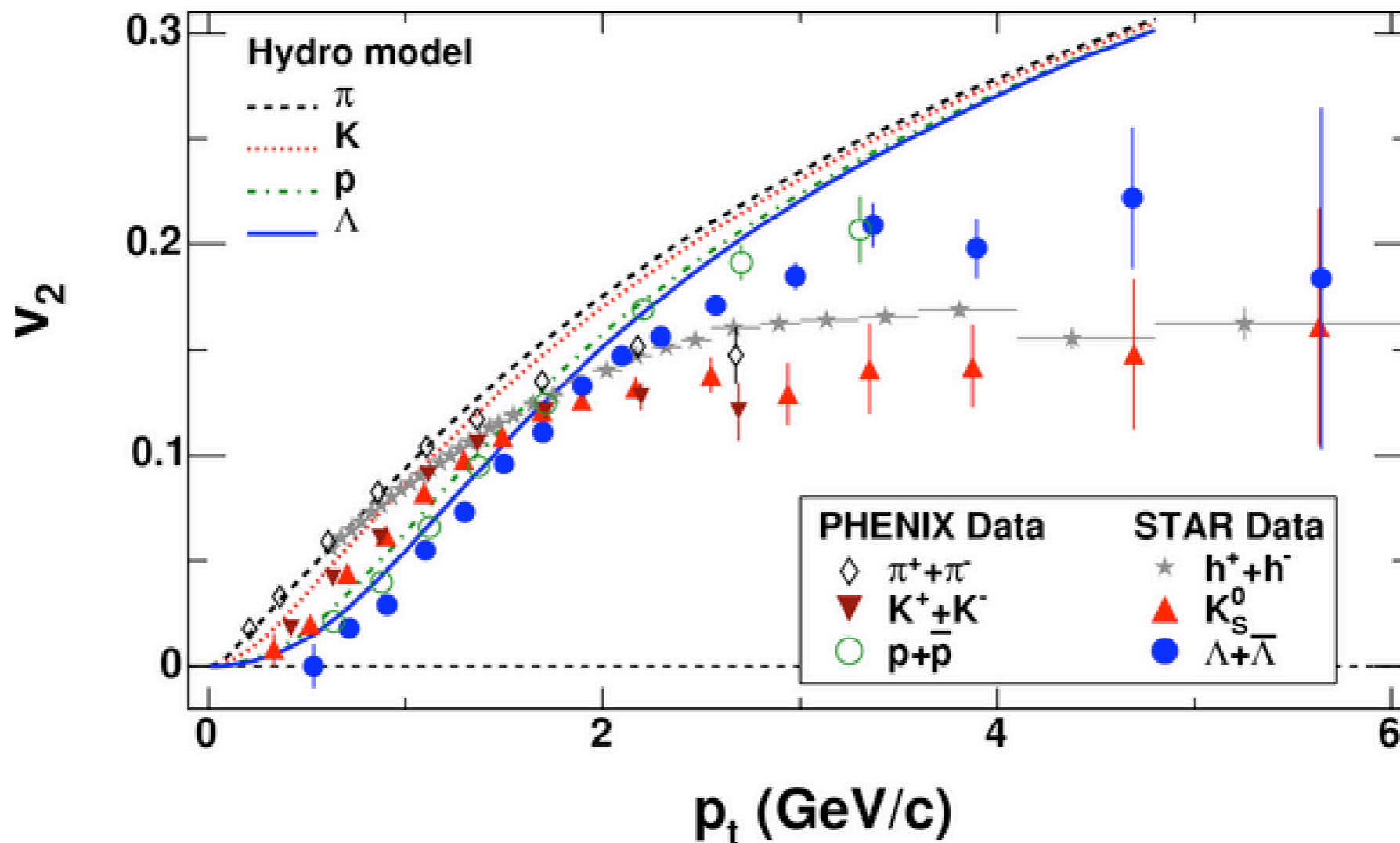


Above, the **ordering** no longer holds

Anisotropic flow:

what have we learned from RHIC?

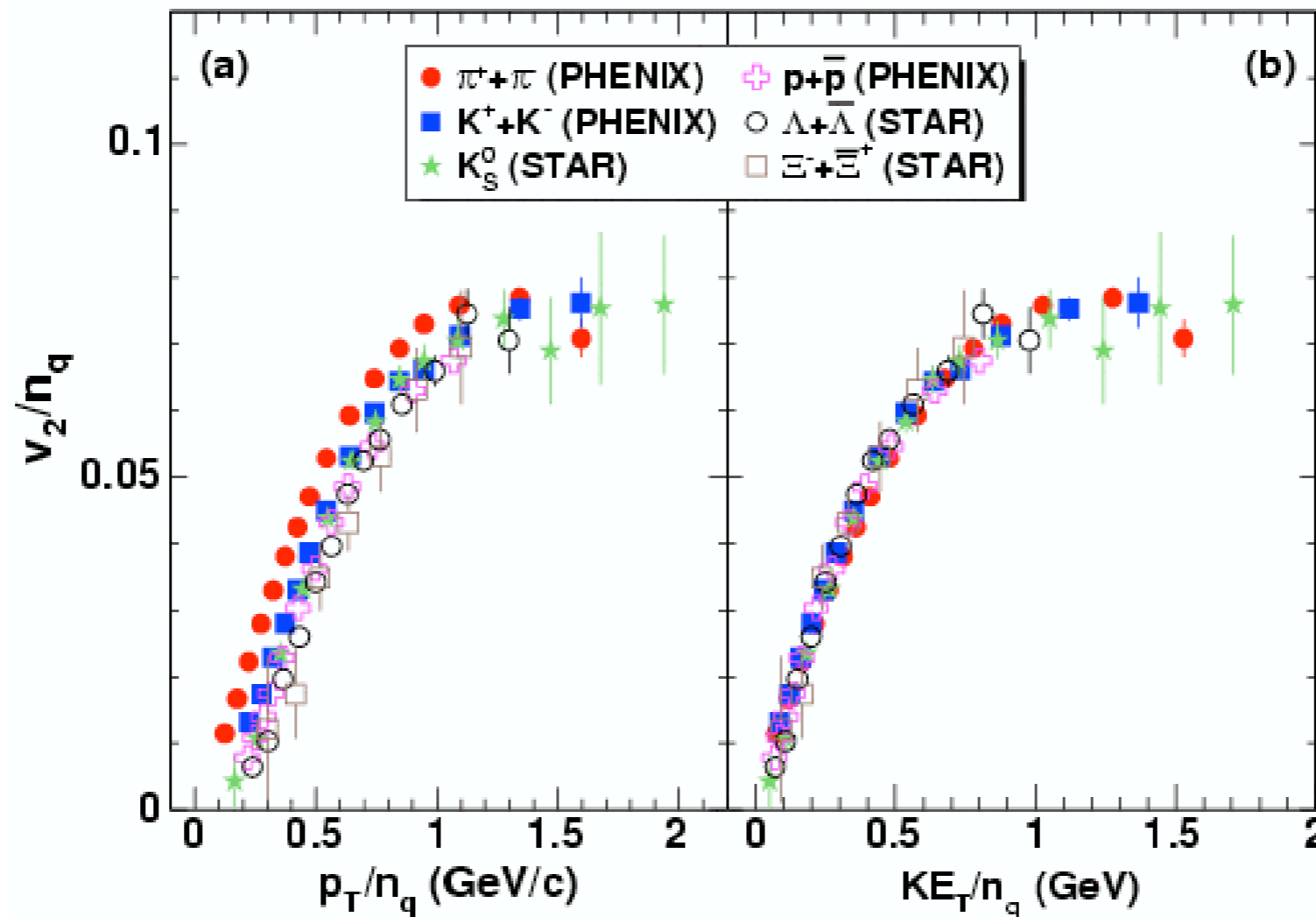
Above $2 \text{ GeV}/c$ there seems to be a **baryon** vs. **meson splitting** of $v_2(p_T)$



Anisotropic flow:

what have we learned from RHIC?

(Various) number-of-constituent-quark scalings can be identified



Anisotropic flow:

what have we learned from RHIC?

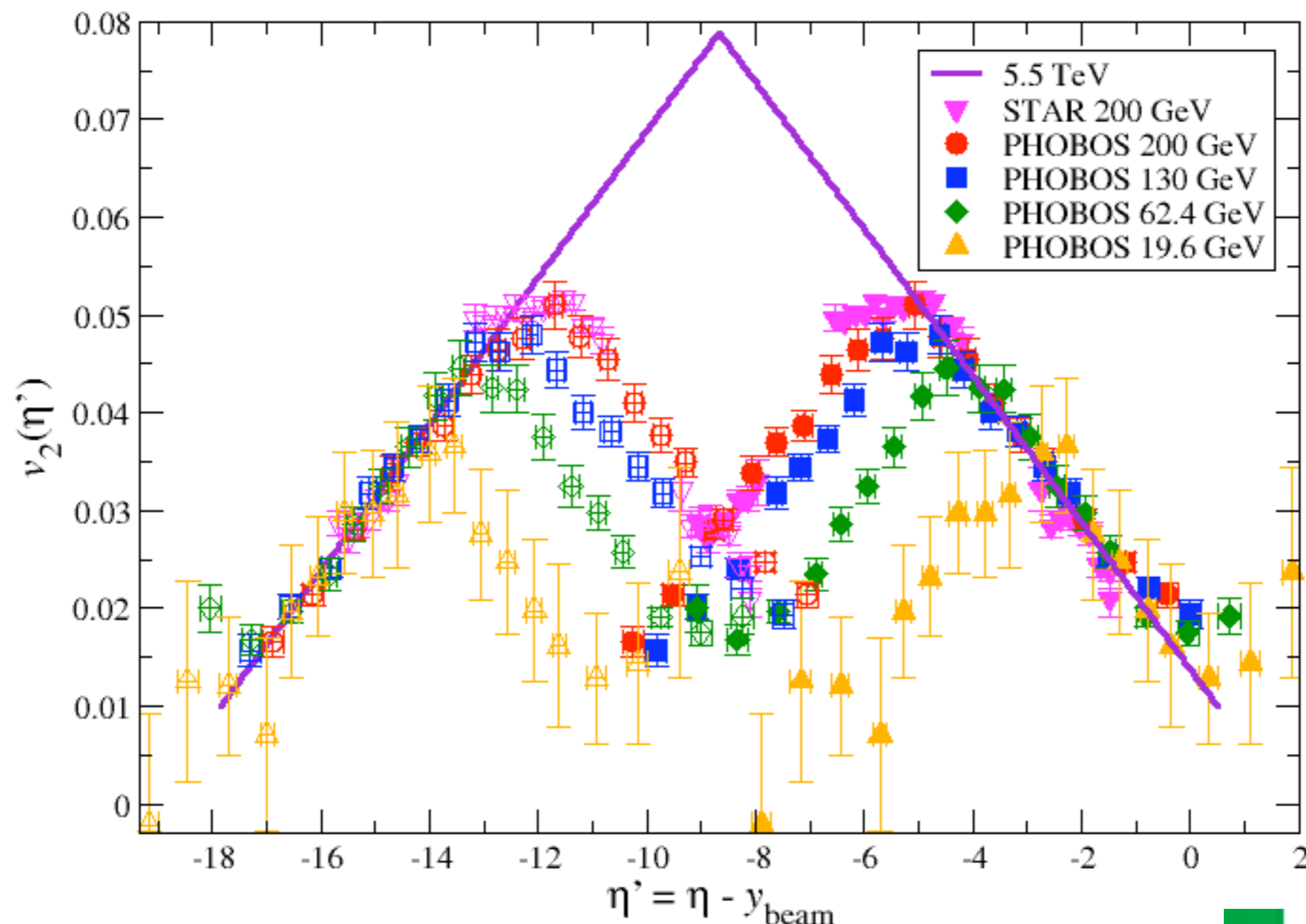
- The p_T -integrated elliptic flow $v_2(\eta)$ shows **extended longitudinal scaling** ("limiting fragmentation") from $\sqrt{s_{NN}} = 20$ to 200 GeV
- At **mid-rapidity**, the $v_2(p_T)$ of **charged hadrons** first **rises linearly** up to $p_T \simeq 2$ GeV/c, then **saturates**
 - in the linear-rise region the **slope** increases with **impact parameter**
- The $v_2(p_T)$ of **identified hadrons** at mid-rapidity
 - show **mass ordering** for $p_T \lesssim 1.5$ GeV/c
 - seem to **scale** with the **number of constituent quarks** above that

$$\frac{1}{n_q} v_2 \left(\frac{p_T}{m} \right), \quad \frac{1}{n_q} v_2 \left(\frac{KE_T}{m} \right) ?$$

Anisotropic flow:

what can we expect at LHC?

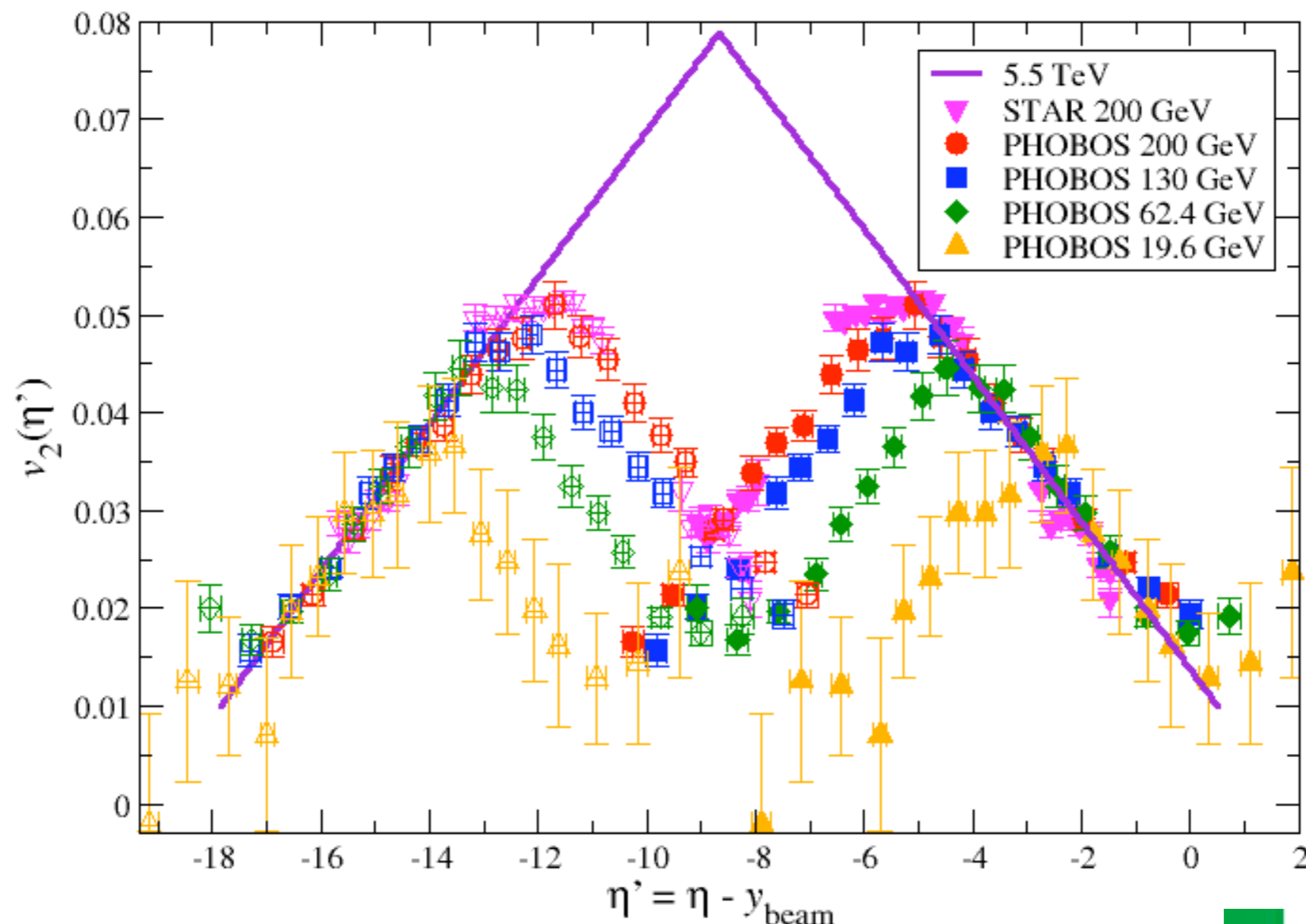
Will the **extended longitudinal scaling** of the p_T -integrated **elliptic flow** $v_2(\eta)$ **persist?**



Anisotropic flow:

what can we expect at LHC?

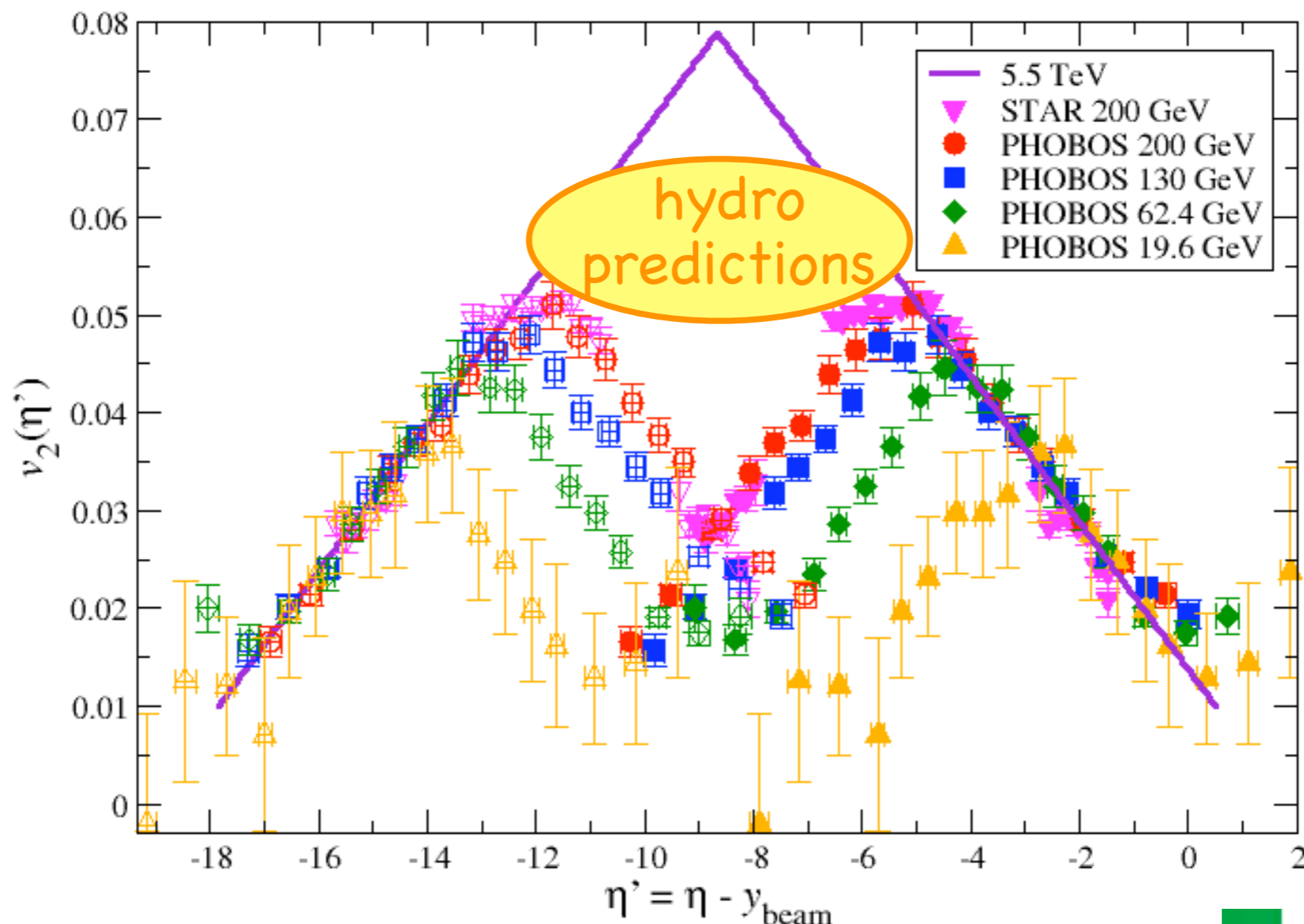
Will the **extended longitudinal scaling** of the p_T -integrated **elliptic flow** $v_2(\eta)$ **persist?**  $v_2(\eta = 0) \approx 0.08$



Anisotropic flow:

what can we expect at LHC?

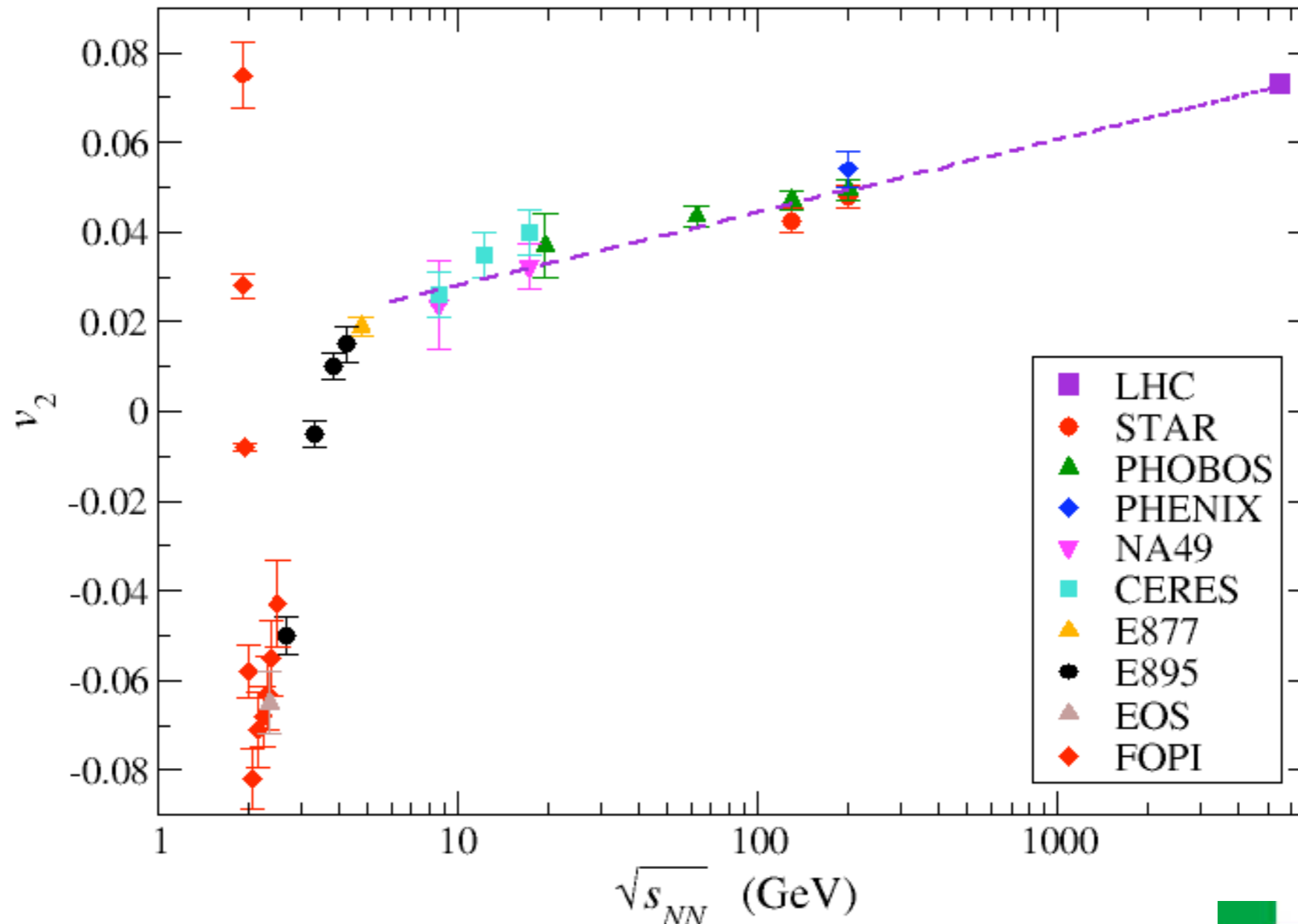
Will the **extended longitudinal scaling** of the p_T -integrated **elliptic flow** $v_2(\eta)$ persist?  $v_2(\eta = 0) \approx 0.08$



Anisotropic flow:

what can we expect at LHC?

Will the **linear rise with $\ln \sqrt{s_{NN}}$** of the p_T -integrated **elliptic flow at midrapidity $v_2(\eta = 0)$** persist?



Anisotropic flow:

what can we expect at LHC?

What if the **extended longitudinal scaling** of the p_T -integrated **elliptic flow** $v_2(\eta)$ **persist**?

• $v_2(\eta = 0) \approx 0.08$ 🖱️ present **ideal-fluid dynamics** approaches will need some revisiting

• the **scaling** will have to be taken seriously!

Anisotropic flow:

what can we expect at LHC?

What if the **extended longitudinal scaling** of the p_T -integrated **elliptic flow** $v_2(\eta)$ **persist**?

• $v_2(\eta = 0) \approx 0.08$  present **ideal-fluid dynamics** approaches will need some revisiting

• the **scaling** will have to be taken seriously!

Up to now, only one attempt* at explaining it, as reflecting the **absence of (kinetic) equilibrium** of the **matter** created in the collision:

longitudinal scaling of $\frac{dN}{dy}$ \Rightarrow **longitudinal scaling** of $v_2(y)$

* three miserable lines in Eur. Phys. J. A **29** (2006) 27

Anisotropic flow: out-of-equilibrium scenario

How does **anisotropic flow** depend on the **number \mathcal{N}** of collisions undergone by **particles**?

Anisotropic flow: out-of-equilibrium scenario

How does **anisotropic flow** depend on the **number \mathcal{N}** of collisions undergone by **particles**?

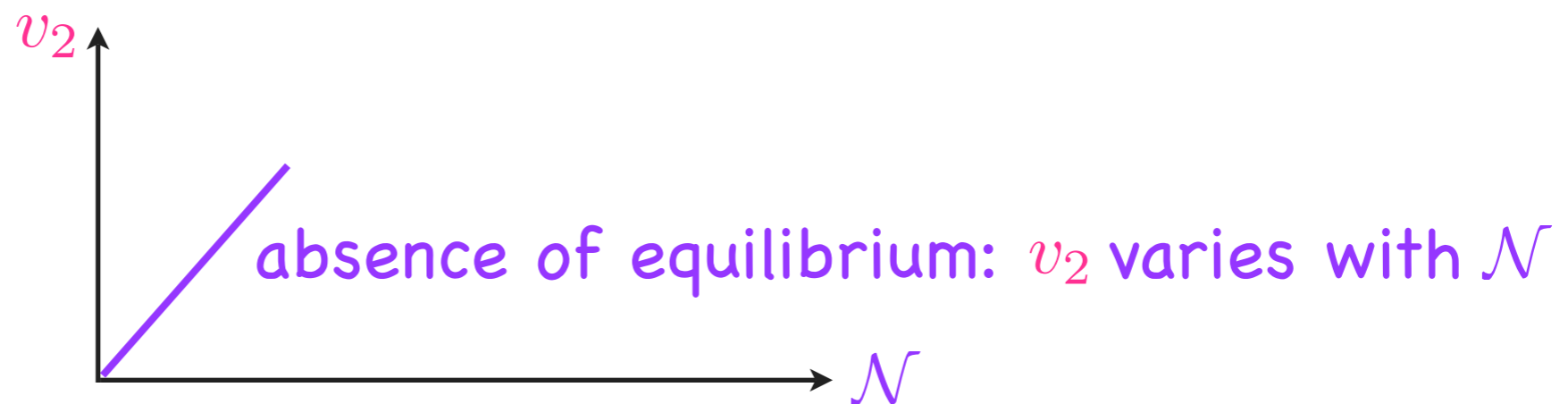
◆ In the absence of **rescatterings** ("gas"), no **flow** develops.



Anisotropic flow: out-of-equilibrium scenario

How does **anisotropic flow** depend on the number \mathcal{N} of collisions undergone by **particles**?

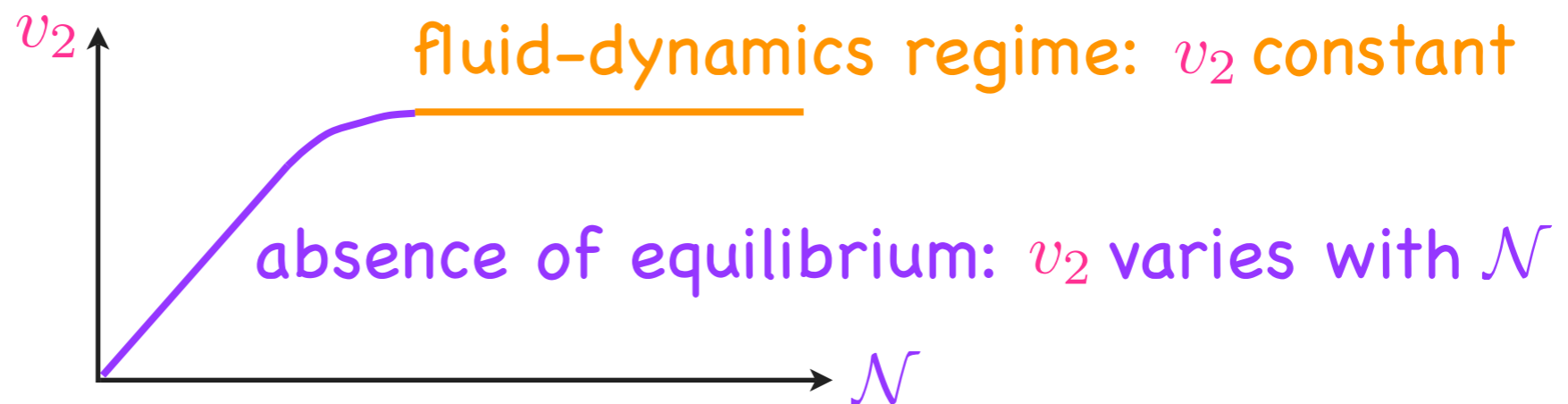
- ◆ In the absence of **rescatterings** ("gas"), no **flow** develops.
- ◆ The more **collisions**, the larger the **flow**.



Anisotropic flow: out-of-equilibrium scenario

How does **anisotropic flow** depend on the **number \mathcal{N}** of collisions undergone by **particles**?

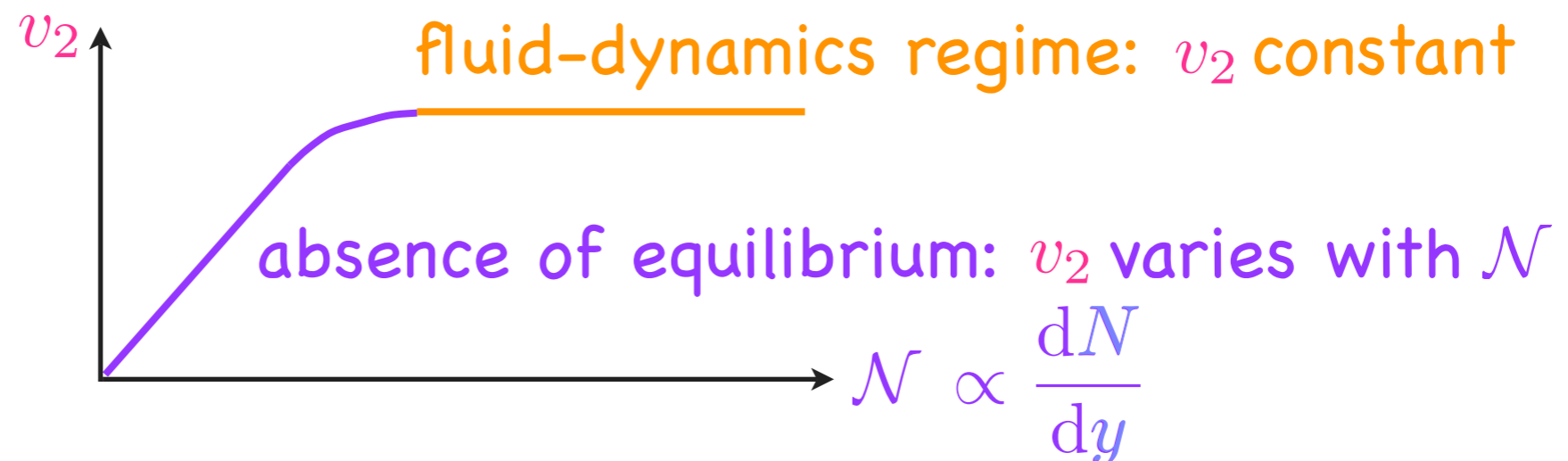
- ◆ In the absence of **rescatterings** ("gas"), no **flow** develops.
- ◆ The more **collisions**, the larger the **flow**.
- ◆ For a given **number of collisions**, the system **thermalizes**: further collisions no longer increase v_2 .



Anisotropic flow: out-of-equilibrium scenario

How does **anisotropic flow** depend on the **number \mathcal{N}** of collisions undergone by **particles**?

- ◆ In the absence of **rescatterings** ("gas"), no **flow** develops.
- ◆ The more **collisions**, the larger the **flow**.
- ◆ For a given **number of collisions**, the system **thermalizes**: further collisions no longer increase v_2 .

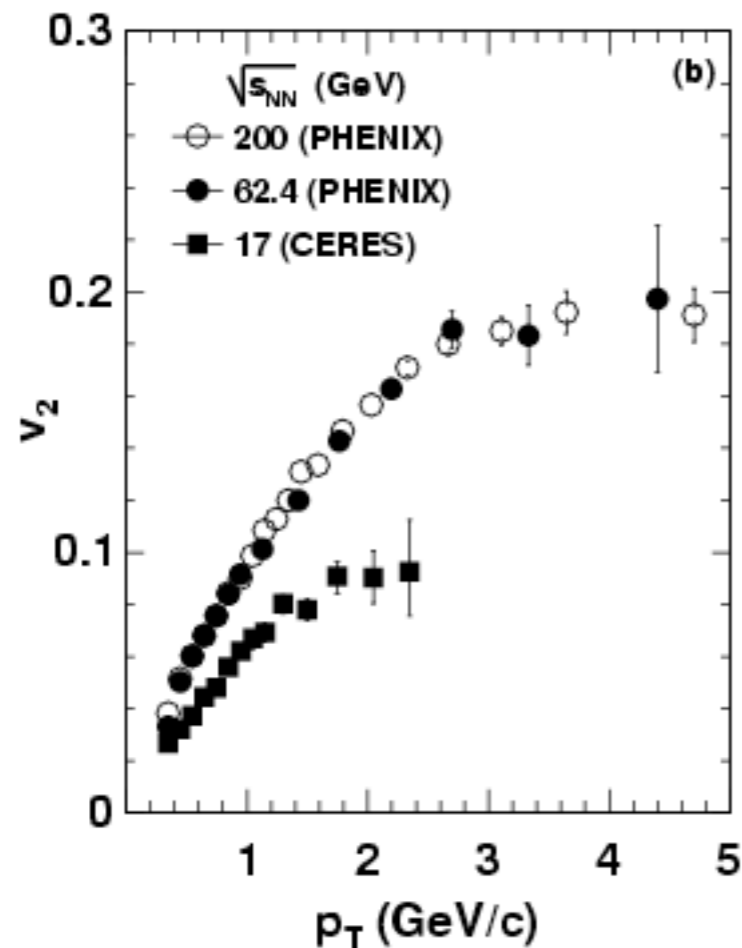


Anisotropic flow:

what can we expect at LHC?

At RHIC, the $v_2(p_T)$ of charged hadrons at mid-rapidity first **rises linearly** up to $p_T \simeq 2 \text{ GeV}/c$

- How does the slope of $v_2(p_T)$ at a given **centrality** evolve with $\sqrt{s_{NN}}$?



The v_2 data for pions and kaons at 62.4 GeV tends to be about 5% smaller than the 200 GeV data (although at $p_T > 1 \text{ GeV}/c$ the difference is within systematic uncertainties). The anti-proton data at 62.4 and 200 GeV are consistent within errors. The data exclude a proton v_2 variation between 62.4 and 200 GeV greater than approximately 15%.

⋮

Appreciable differences are seen between the 17.3 GeV and 62.4 GeV data.

(slight disagreement)

What drives the increase of the p_T -integrated v_2 ? The rise in $\langle p_T \rangle$?

Anisotropic flow:

what can we expect at LHC?

At RHIC, the $v_2(p_T)$ of charged hadrons at mid-rapidity first rises linearly up to $p_T \simeq 2 \text{ GeV}/c$, then saturates.

• How does the slope of $v_2(p_T)$ at a given centrality evolve with $\sqrt{s_{NN}}$?

👉 What drives the increase of the p_T -integrated v_2 ?

• How does the position of the breaking point* in the $v_2(p_T)$ shape evolve? (with centrality, with $\sqrt{s_{NN}}$)

👉 “natural” expectation: the p_T of the breaking point should increase with centrality, with $\sqrt{s_{NN}}$, and with the size of the colliding nuclei, and decrease with rapidity

(It is far from obvious that the PHENIX data support this expectation)

* has to be defined properly...

Anisotropic flow:

what can we expect at LHC?

At SPS and RHIC the $v_2(p_T)$ of identified hadrons at mid-rapidity show mass ordering for $p_T \lesssim 1.5 \text{ GeV}/c$... and that should persist at LHC!

- Will the ordering be in quantitative agreement with hydro?

All slow particles ($p_T/m < \text{max fluid velocity}$) have the same $v_n\left(\frac{p_T}{m}, y\right)$ since they originate from the same fluid cell;

for fast particles, $v_2(p_T) \propto (p_T - m_T v_{\text{max}})$. PLB 642 (2006) 227

Qualitative agreement is not satisfactory... If (!) hydrodynamics is the large-number-of-collisions limit of the out-of-equilibrium case, then not too far from equilibrium, the mass ordering should already be present.

see QGSM: PLB 631 (2005) 109 and RQMD/UrQMD: JPG 32 (2006) 1121

Anisotropic flow:

what can we expect at LHC?

At SPS and RHIC the $v_2(p_T)$ of identified hadrons at mid-rapidity show **mass ordering** for $p_T \lesssim 1.5 \text{ GeV}/c$... and that should **persist** at LHC!

- Will the **ordering** be in **quantitative agreement** with **hydro**?

All slow particles ($p_T/m < \text{max fluid velocity}$) have the **same** $v_n\left(\frac{p_T}{m}, y\right)$ since they originate from the same **fluid cell**;

for fast particles, $v_2(p_T) \propto (p_T - m_T v_{\text{max}})$.

PLB 642 (2006) 227

- Till which p_T does the **ordering** hold? (same expectations as above: the position should increase with **centrality**, with $\sqrt{s_{NN}}$, and with the **size** of the colliding nuclei, and decrease with **rapidity**)

Anisotropic flow:

what can we expect at LHC?

At SPS and RHIC the $v_2(p_T)$ of identified hadrons at mid-rapidity show mass ordering for $p_T \lesssim 1.5 \text{ GeV}/c$... and that should persist at LHC!

- Will the ordering be in quantitative agreement with hydro?

All slow particles ($p_T/m < \text{max fluid velocity}$) have the same $v_n\left(\frac{p_T}{m}, y\right)$ since they originate from the same fluid cell;

for fast particles, $v_2(p_T) \propto (p_T - m_T v_{\text{max}})$. PLB 642 (2006) 227

- Till which p_T does the ordering hold? (same expectations as above: the position should increase with centrality, with $\sqrt{s_{NN}}$, and with the size of the colliding nuclei, and decrease with rapidity)

- What happens above the mass-ordering region?
number-of-constituent-quark scaling?

cf. Peter Lévai's talk(?)

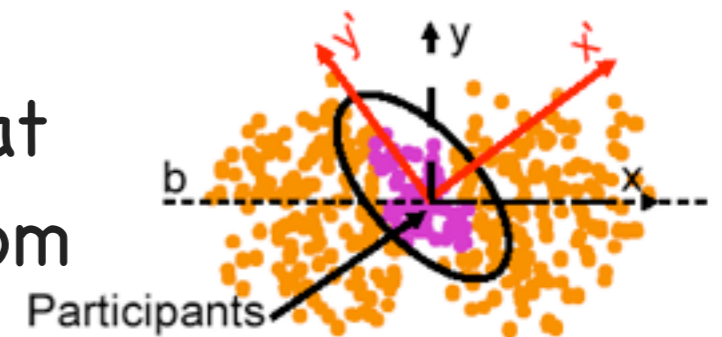
Anisotropic flow:

what have we learned from RHIC?

PHOBOS and STAR (+ theorists) have made huge progress in demonstrating the importance of **fluctuations**, in particular when comparing collisions with different **centralities**.

- Old vision: one should compare v_2 / ϵ (which is constant in **hydro**)
“geometrical” eccentricity
(ellipsis with the shorter axis along the **impact parameter**)

- The nuclei cross each other fast: the nucleons in the **overlap region** are frozen in a configuration that differs from the geometrical picture (and varies from event to event)

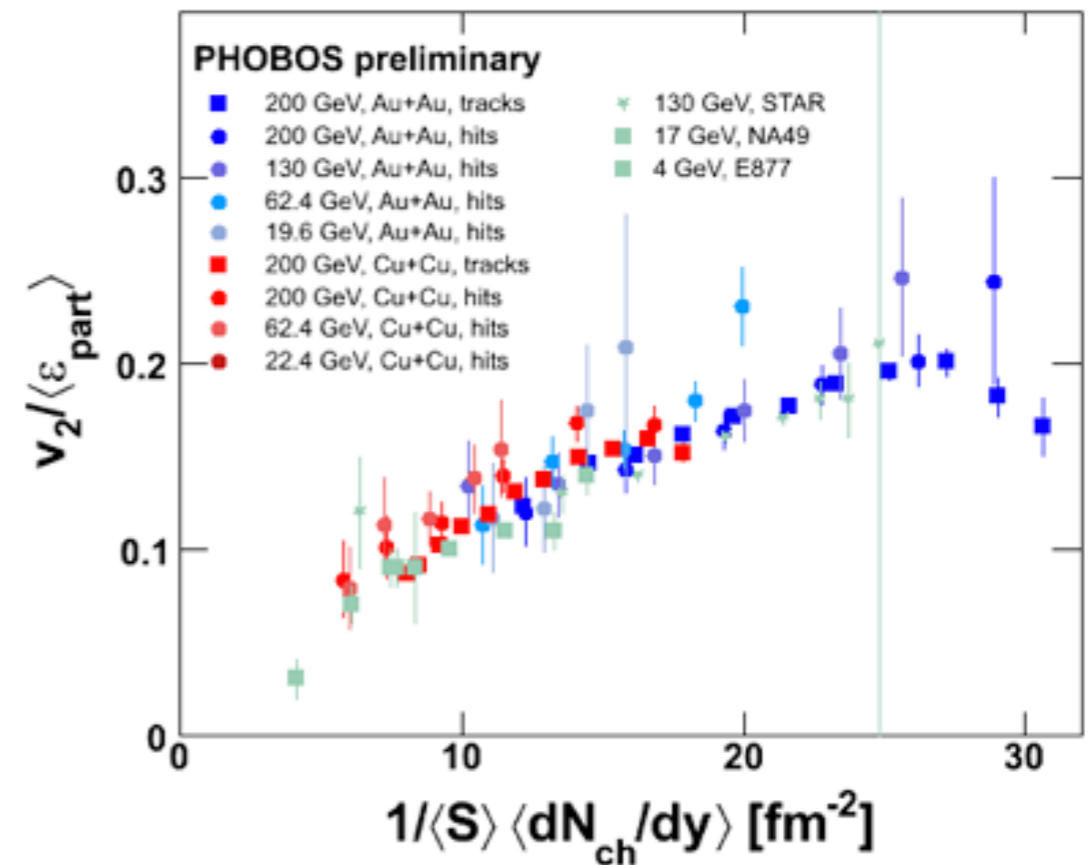
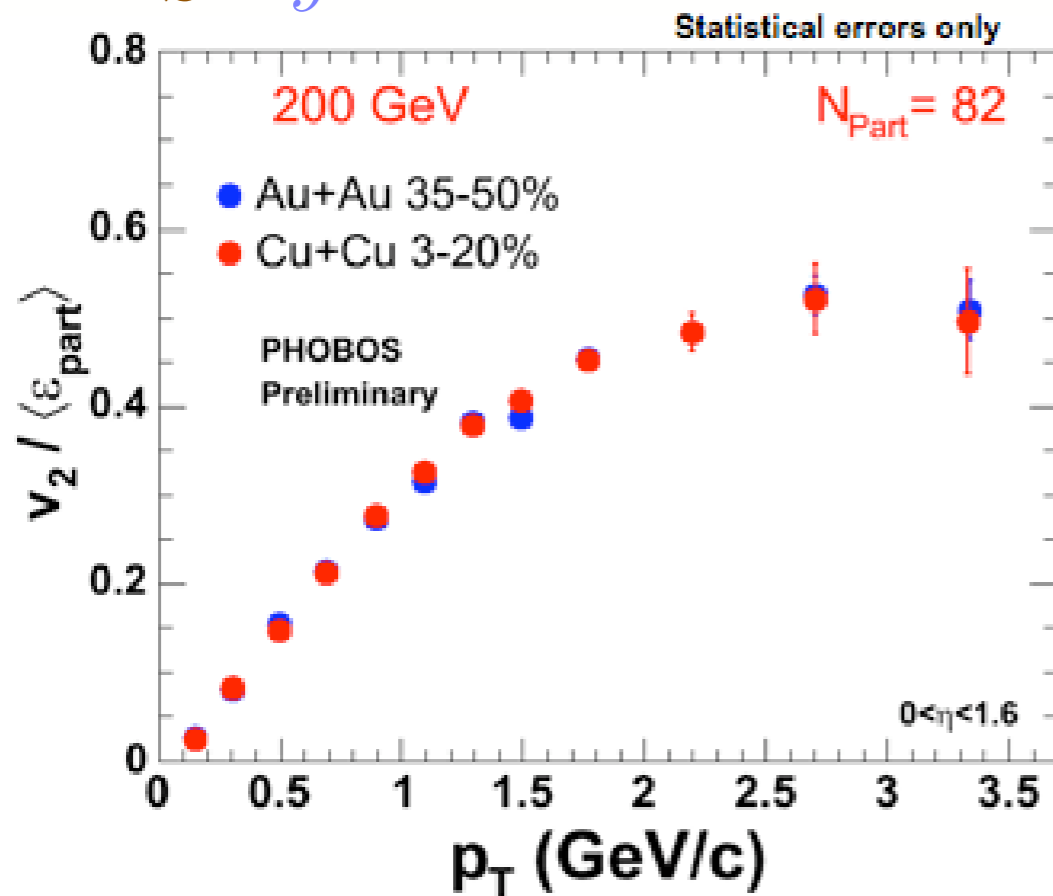


- the proper scaling is rather with the “**participant eccentricity**” ϵ_{part}

Anisotropic flow:

what have we learned from RHIC?

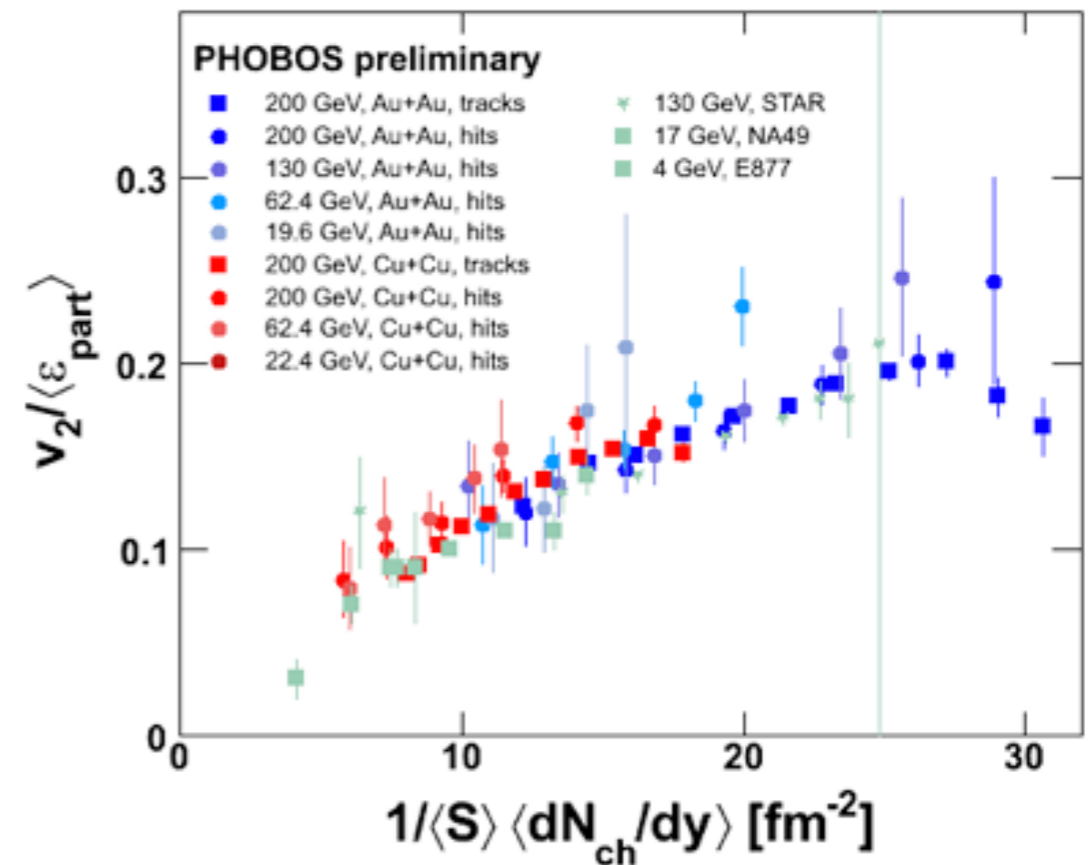
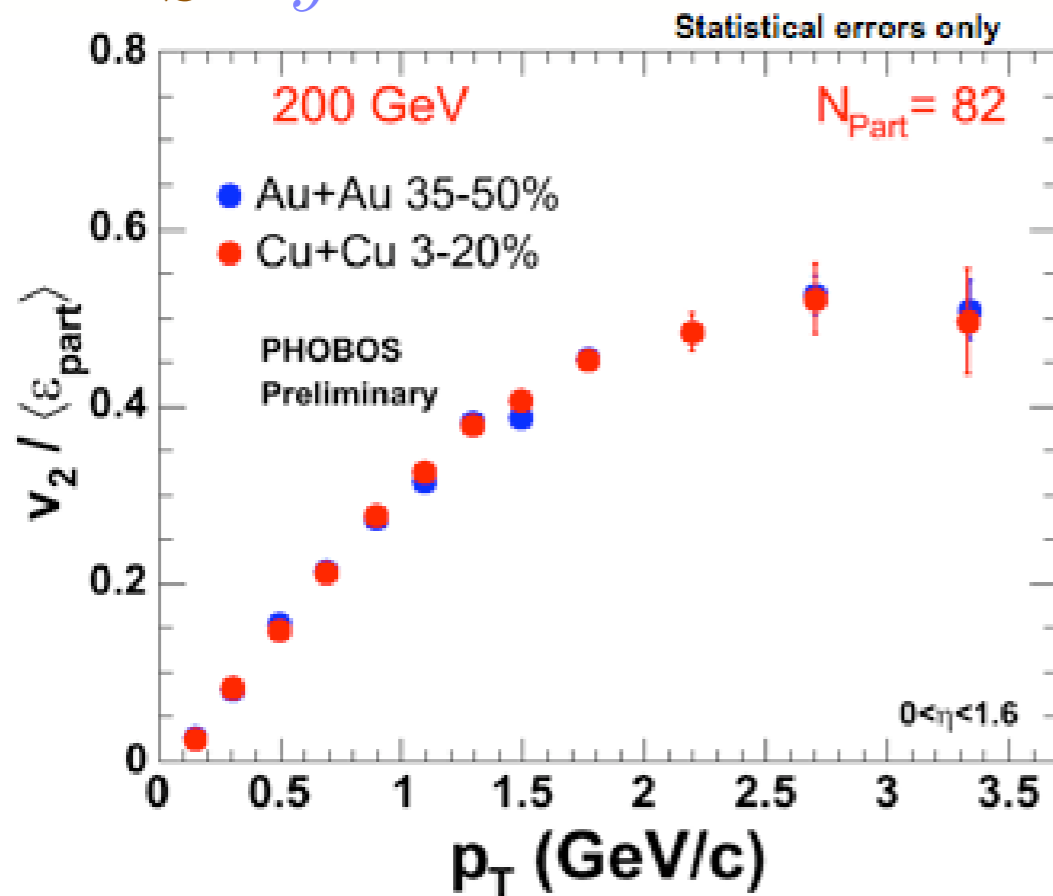
Using the "participant eccentricity" ϵ_{part} , Cu-Cu and Au-Au data at a given $\frac{1}{S} \frac{dN}{dy}$ fall on the same curves [predicted in PLB 627 (2005) 49]



Anisotropic flow:

what have we learned from RHIC?

Using the "participant eccentricity" ϵ_{part} , Cu-Cu and Au-Au data at a given $\frac{1}{S} \frac{dN}{dy}$ fall on the same curves [predicted in PLB 627 (2005) 49]

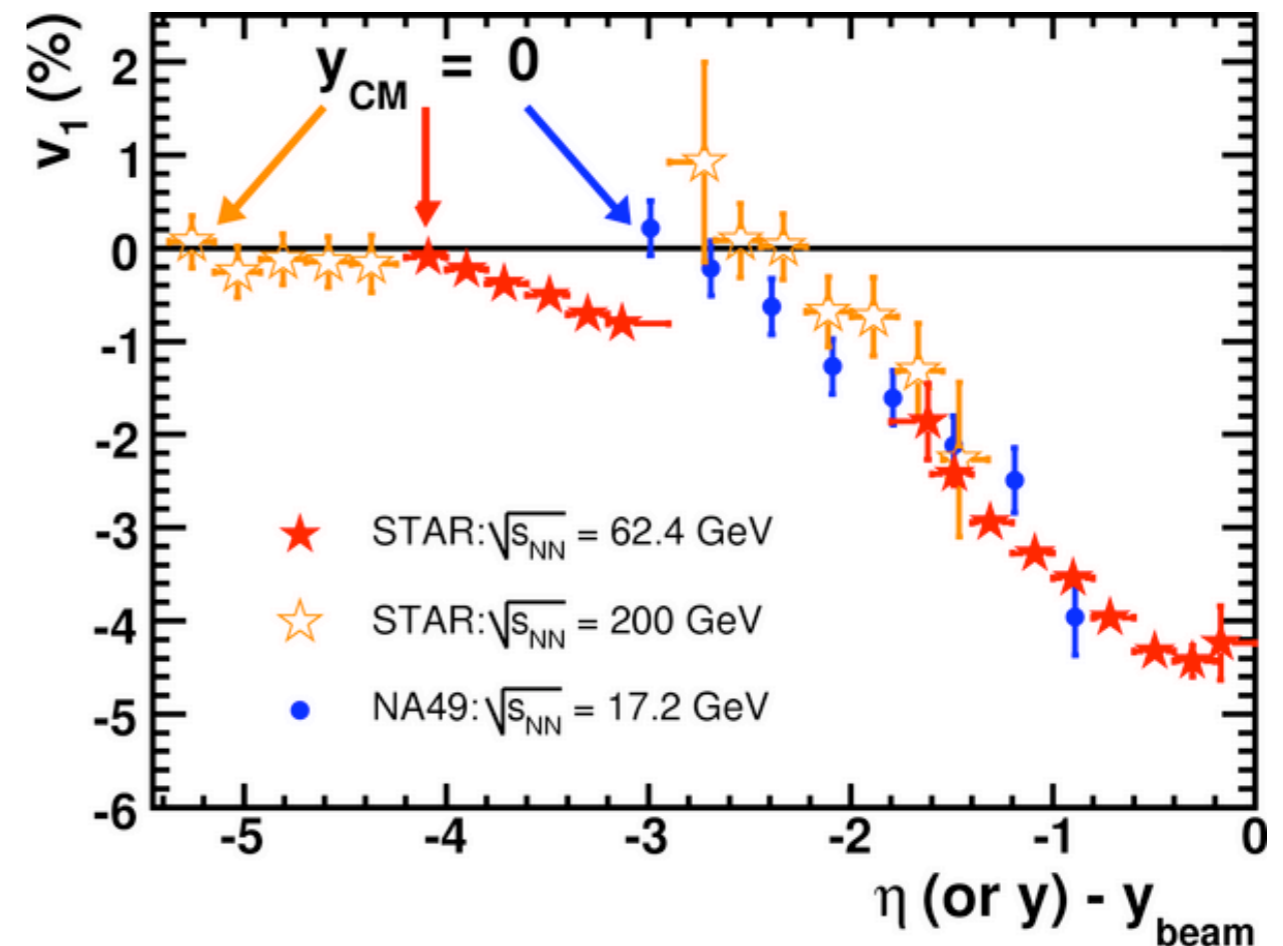
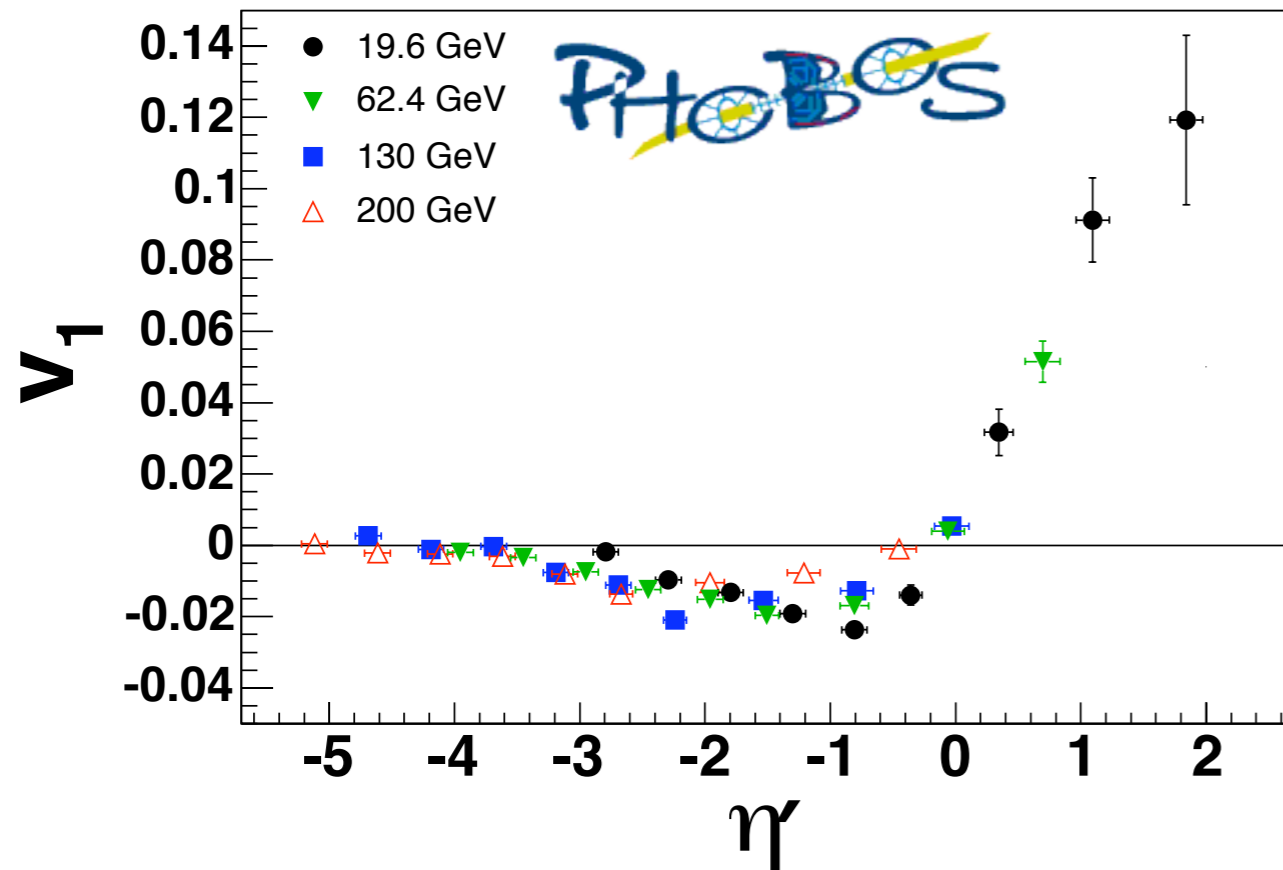


Temptation: **extrapolate** to LHC!

But beware, the underlying model for the **eccentricity** might change (here, Glauber model; CGC-inspired calculation yields **larger** ϵ)

Anisotropic flow: from RHIC to LHC

The p_T -integrated directed flow $v_1(\eta)$ shows extended longitudinal scaling ("limiting fragmentation") from $\sqrt{s_{NN}} = 20$ to 200 GeV...



... but that cannot be true over the whole y range ($v_1(y = 0) = 0$),
Unless v_1 vanishes in an extended region!

Yet, expect a very small v_1 up to $y \approx 5$ at LHC.

Anisotropic flow: from RHIC to LHC

STAR has also measured the **fourth anisotropic-flow harmonic** v_4 , as a function of p_T , y , particle type, at $\sqrt{s_{NN}} = 62.4$ and 200 GeV
cf. Raimond Snellings in a few moments

Within **ideal-fluid dynamics prediction**, to leading order in the **fluid-velocity anisotropies**, $v_4(p_T, y) = \frac{1}{2} v_2(p_T, y)^2$ for each **type of fast particle**.
PLB 642 (2006) 227

Whereas in the **out-of-equilibrium scenario** v_2 , v_4 are proportional to the number of collisions $\mathcal{N} \Rightarrow \frac{v_4}{v_2^2} \propto \frac{1}{\mathcal{N}}$, **minimum at equilibrium**.

👉 in the **non-equilibrium scenario** $\frac{v_4(p_T, y)}{v_2(p_T, y)^2} > \frac{1}{2}$ (≈ 1.2 at RHIC).

Expect a smaller $\frac{v_4}{v_2^2}$ at LHC... (but v_4 will still be sizable)

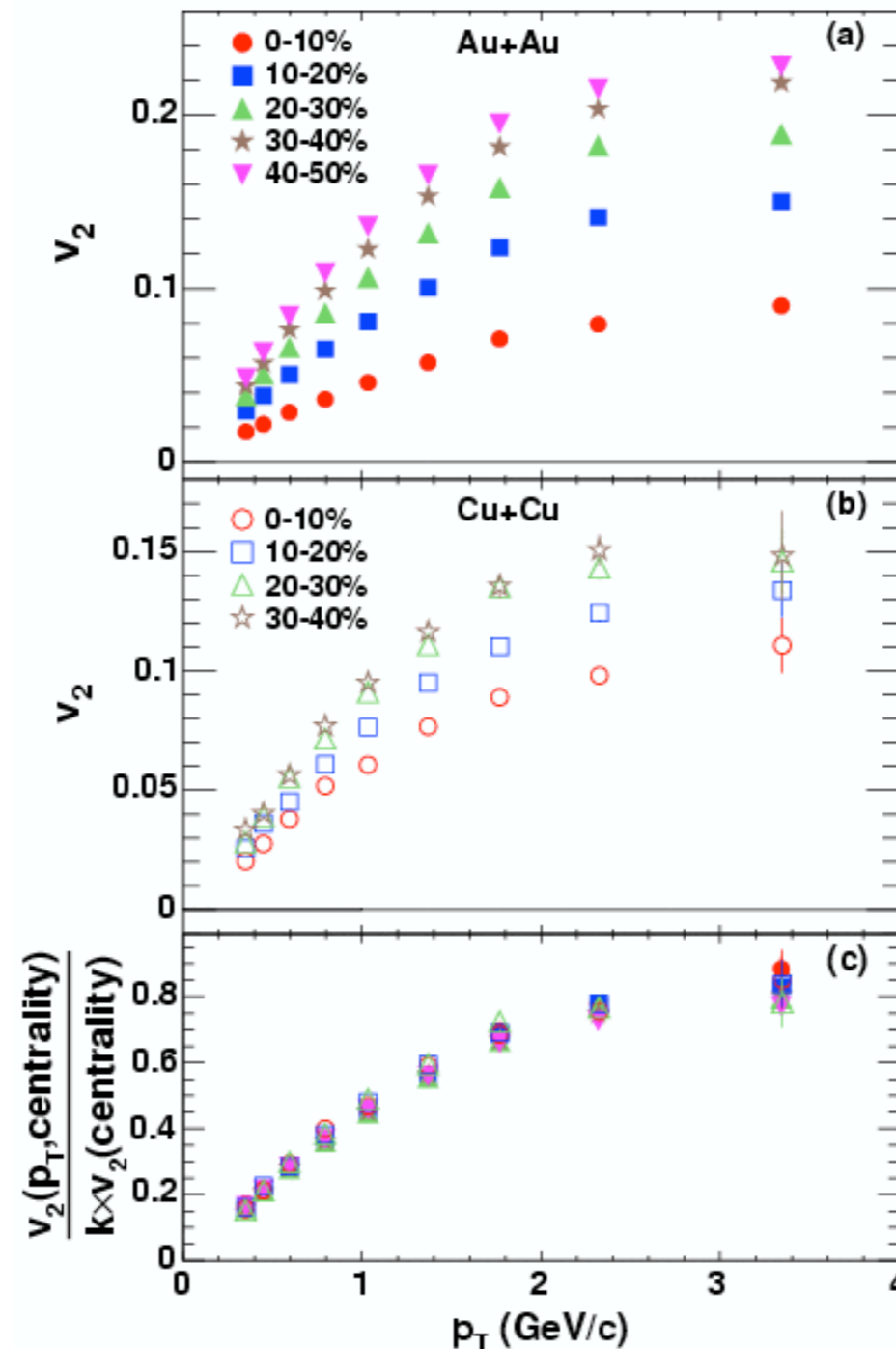
Anisotropic flow: ^{my?} questions for LHC

- Extended longitudinal scaling of the p_T -integrated elliptic flow?
- If the $v_2(p_T)$ of charged hadrons at mid-rapidity rises linearly at low transverse momentum
 - how does the slope compare to lower beam energies?
 - where does the linear rise stop? Systematics wanted.
 - does $v_2(p_T)$ goes down to 0 at some (high p_T) point?
- Regarding the $v_2(p_T)$ of identified hadrons at mid-rapidity
 - mass ordering at low p_T ? (Quantitative results wanted!) Till where?
 - (not mentioned here): $v_2(p_T)$ of charm / beauty?
- v_4 will also be instructive! (at least, if theorists care...)

Extra slides

Anisotropic flow: p_T -dependence

The “natural” expectation is that the p_T of the **breaking point** in the $v_2(p_T)$ shape should increase with **centrality**, with $\sqrt{s_{NN}}$, and with the **size** of the colliding nuclei, and decrease with **rapidity**



Heavy-ion collisions: fluid-dynamics description

At freeze-out, each fluid cell emits particles according to thermal distributions (Bose-Einstein, Fermi-Dirac):

$$E \frac{dN}{d^3\mathbf{p}} = C \int_{\Sigma} \exp\left(-\frac{p^\mu u_\mu(x)}{T_{f.o.}}\right) p^\mu d\sigma_\mu$$

Heavy-ion collisions: fluid-dynamics description

At freeze-out, each fluid cell emits particles according to thermal distributions (Bose-Einstein, Fermi-Dirac):

$$E \frac{dN}{d^3\mathbf{p}} = C \int_{\Sigma} \exp\left(-\frac{p^\mu u_\mu(x)}{T_{f.o.}}\right) p^\mu d\sigma_\mu$$

fluid cell velocity

$p^\mu d\sigma_\mu$

particle momentum

freeze-out hypersurface

Heavy-ion collisions: fluid-dynamics description

At freeze-out, each fluid cell emits particles according to thermal distributions (Bose-Einstein, Fermi-Dirac):

$$E \frac{dN}{d^3\mathbf{p}} = C \int_{\Sigma} \exp\left(-\frac{p^\mu u_\mu(x)}{T_{f.o.}}\right) p^\mu d\sigma_\mu$$

freeze-out hypersurface \rightarrow Σ \leftarrow fluid cell velocity $u_\mu(x)$ \leftarrow particle momentum p^μ

A consistent ideal-hydrodynamics picture requires that $T_{f.o.} \ll T_{in.}$

\Leftrightarrow

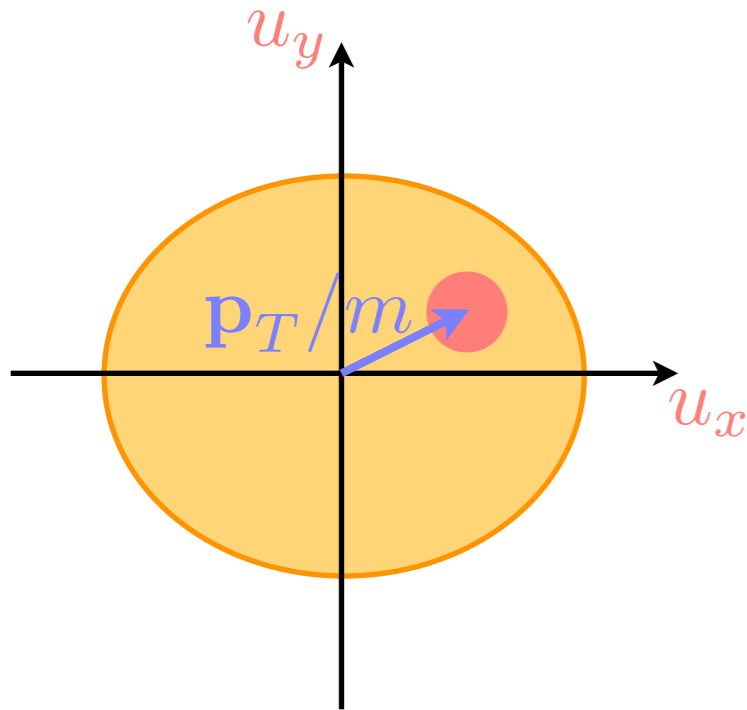
ideal-fluid limit = small- $T_{f.o.}$ limit

👉 one can compute the particle distribution in a model-independent, analytic way (using a saddle-point approximation).

N.Borghini, J.-Y.Ollitrault PLB 642 (2006) 227

Ideal fluid-dynamics: analytical results

Slow particles ($p_T/m < u_{\max}(\frac{\pi}{2})$) move together with the fluid.



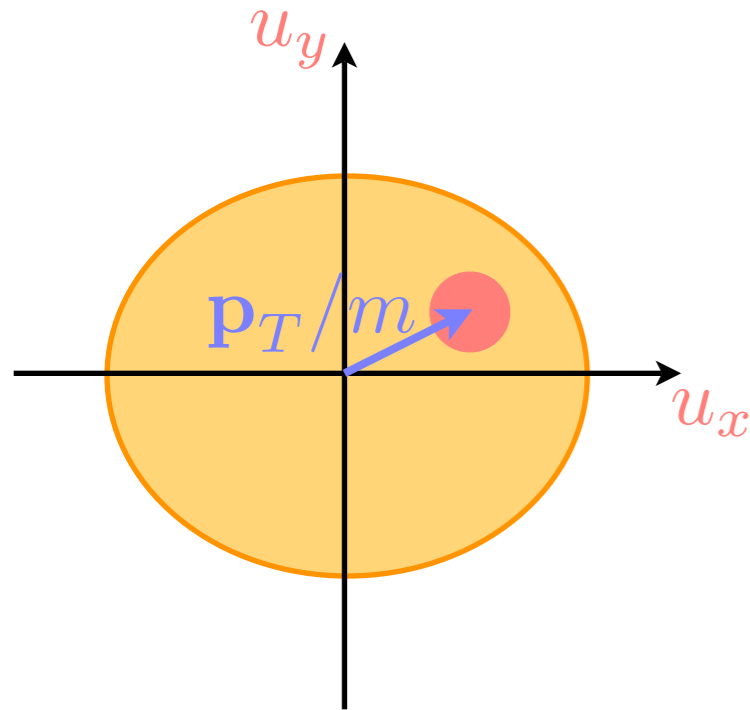
There exists a fluid cell whose velocity equals the particle velocity: minimizes $p^\mu u_\mu$.

👉 Integrand in the Cooper-Frye spectrum is Gaussian, with width $\propto 1/\min(\sqrt{p^\mu u_\mu}) = 1/\sqrt{m}$.

saddle-point approximation!

Ideal fluid-dynamics: analytical results

Slow particles ($p_T/m < u_{\max}(\frac{\pi}{2})$) move together with the fluid.



There exists a fluid cell whose velocity equals the particle velocity: minimizes $p^\mu u_\mu$.

Integrand in the Cooper-Frye spectrum is Gaussian, with width $\propto 1/\min(\sqrt{p^\mu u_\mu}) = 1/\sqrt{m}$.

saddle-point approximation!

$$m \gg T_{f.o.}$$

Similar momentum distributions for different particles

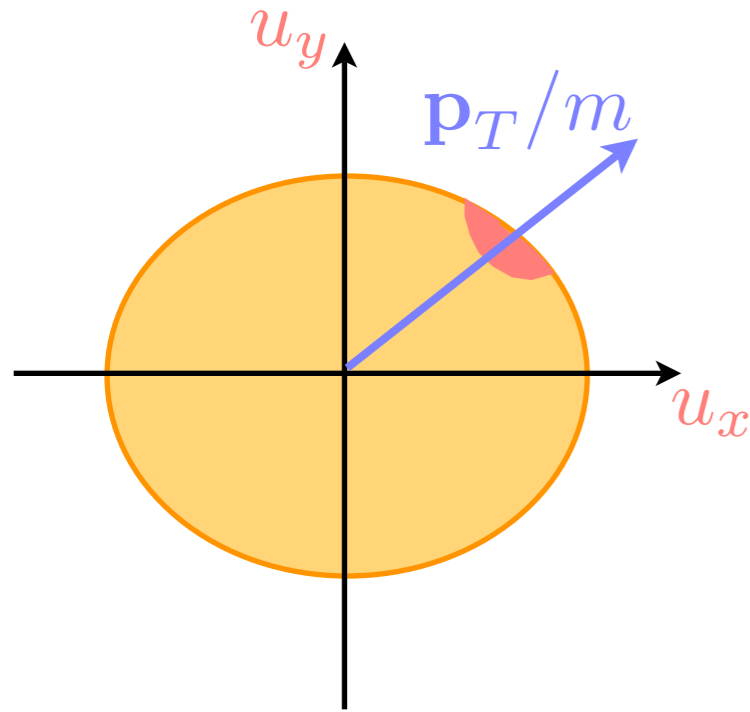
$$E \frac{dN}{d^3\mathbf{p}} = c^h(m) f\left(\frac{p_T}{m}, y, \varphi\right)$$

$v_n\left(\frac{p_T}{m}, y\right)$ identical for all particles!

\Rightarrow mass-ordering of $v_2(p_T, y)$, $\frac{v_4}{v_2}\left(\frac{p_T}{m}, y\right)$ universal

Ideal fluid-dynamics: analytical results

Fast particles ($p_T/m > u_{\max}(0)$) move faster than the **fluid**.

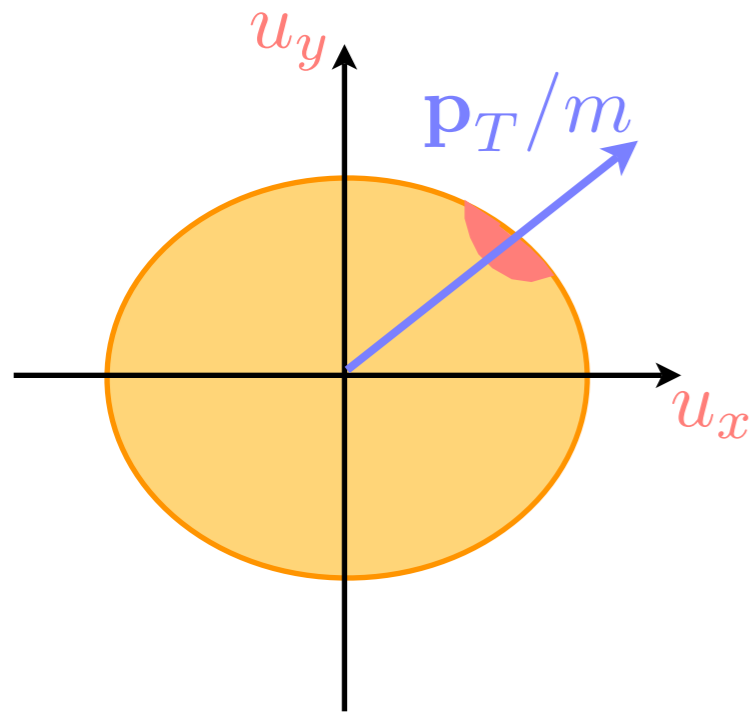


Such a **particle** was emitted by a **cell** along the direction of its **velocity** where the **fluid** is **fastest** (often, close to the edge of the **fluid**).

Saddle-point expansion of the **Cooper-Frye formula** around the minimum of $p^\mu u_\mu$.

Ideal fluid-dynamics: analytical results

Fast particles ($p_T/m > u_{\max}(0)$) move faster than the **fluid**.



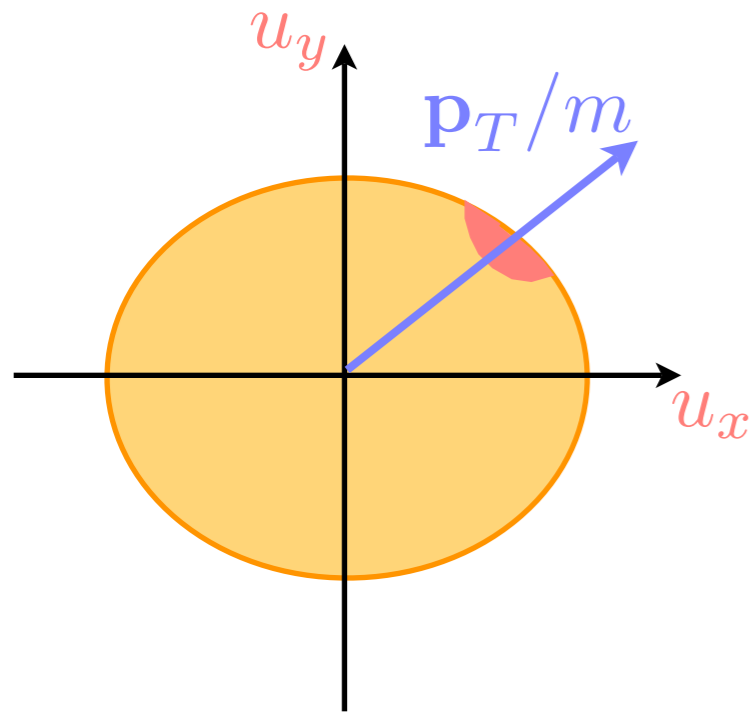
Such a **particle** was emitted by a **cell** along the direction of its **velocity** where the **fluid** is **fastest** (often, close to the edge of the **fluid**).

Saddle-point expansion of the **Cooper-Frye formula** around the minimum of $p^\mu u_\mu$.

check the domain of validity!

Ideal fluid-dynamics: analytical results

Fast particles ($p_T/m > u_{\max}(0)$) move faster than the **fluid**.



Such a **particle** was emitted by a **cell** along the direction of its **velocity** where the **fluid** is **fastest** (often, close to the edge of the **fluid**).

Saddle-point expansion of the **Cooper-Frye formula** around the minimum of $p^\mu u_\mu$.

check the domain of validity!

- Momentum distribution $\propto \exp\left(\frac{p_T u_{\max} - m_T u_{\max}^0}{T_{\text{f.o.}}}\right)$
- To leading order in the **fluid-velocity anisotropies** V_n :

$$v_2(p_T) = \frac{V_2 u_{\max}}{T_{\text{f.o.}}}(p_T - m_T v_{\max}):$$
mass-ordering of $v_2(p_T, y)$ persists;
- Assuming additionally that $V_4 \ll V_2$, one finds for p_T large enough:

$$\frac{v_4(p_T, y)}{v_2(p_T, y)^2} = \frac{1}{2}$$