

ELEMENTARY PARTICLE PHYSICS

WS 2016/2017: Exercise sheet 7

23. Starting from the expression for the photon field operator

$$\hat{A}^\mu(x) = \int \frac{d^3k}{(2\pi)^3 \sqrt{2E_k}} \sum_\lambda \epsilon_\lambda^\mu(k) \left(\hat{a}(k) e^{-ikx} + \hat{a}^\dagger(k) e^{ikx} \right)$$

show that the photon's Feynman propagator $\langle 0 | T \{ \hat{A}^\mu(x) \hat{A}^\nu(y) \} | 0 \rangle$ in momentum space is proportional to $\sum_\lambda \epsilon_\lambda^\mu(k) \epsilon_\lambda^\nu(k)$

24. Compute the transition matrix element from an initial $|e^-(k, s) e^+(k', s')\rangle$ state to the final state $\langle \mu^-(p, t) \mu^+(p', t') |$ for a theory with the interacting part of the Hamiltonian as $\mathcal{H}_{int} = g \bar{\chi} \gamma_\mu \chi A^\mu + g \bar{\psi} \gamma_\mu \psi A^\mu$ where χ, ψ denote the muon, electron field resp. and A^μ is the photon field.